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## WELCOME TO THE PHYSICS LABORATORY

Physics is our human attempt to explain the workings of the world. The success of that attempt is evident in the technology of our society. You have already developed your own physical theories to understand the world around you. Some of these ideas are consistent with accepted theories of physics while others are not. This laboratory manual is designed, in part, to help you recognize where your ideas agree with those accepted by physics and where they do not. It is also designed to help you become a better physics problem solver.

You are presented with contemporary physical theories in lecture and in your textbook. In the laboratory you can apply the theories to real-world problems by comparing your application of those theories with reality. You will clarify your ideas by: answering questions and solving problems before you come to the lab room, performing experiments and having discussions with classmates in the lab room, and occasionally by writing lab reports after you leave. Each laboratory has a set of problems that ask you to make decisions about the real world. As you work through the problems in this laboratory manual, remember: the goal is not to make lots of measurements. The goal is for you to examine your ideas about the real world.

The three components of the course - lecture, discussion section, and laboratory section-serve different purposes. The laboratory is where physics ideas, often expressed in mathematics, meet the real world. Because different lab sections meet on different days of the week, you may deal with concepts in the lab before meeting them in lecture. In that case, the lab will serve as an introduction to the lecture. In other cases the lecture will be a good introduction to the lab.

The amount you learn in lab will depend on the time you spend in preparation before coming to lab.
Before coming to lab each week you must read the appropriate sections of your text, read the assigned problems to develop a fairly clear idea of what will be happening, and complete the prediction and method questions for the assigned problems.

Often, your lab group will be asked to present its predictions and data to other groups so that everyone can participate in understanding how specific measurements illustrate general concepts of physics. You should always be prepared to explain your ideas or actions to others in the class. To show your instructor that you have made the appropriate connections between your measurements and the basic physical concepts, you will be asked to write a laboratory report. Guidelines for preparing lab reports can be found in the lab manual appendices and in this introduction. An example of a good lab report is shown in Appendix E. Please do not hesitate to discuss any difficulties with your fellow students or the lab instructor.

Relax. Explore. Makemistakes. Ask lots of questions, and havefun.

## WHAT TO DO TO BE SUCCESSFULIN THIS LAB:

## Safety comes first in any laboratory.

If in doubt about any procedure, or if it seems unsafe to you, STOP. Ask your lab instructor for help.

## A. What to bring to each laboratory session:

1. Bring an 8" by 10" graph-ruled lab journal, to all lab sessions. Your journal is your "extended memory" and should contain everything you do in the lab and all of your thoughts as you are
going along. Your lab journal is a legal document; you should never tear pages from it. Your lab journal must be bound (as University of $M$ innesota 2077-S) and must not allow pages to be easily removed (as spiral bound notebooks).
2. Bring a "scientific" calculator.
3. Bring this lab manual.
B. Prepare for each laboratory session:

Each laboratory consists of a series of related problems that can be solved using the same basic concepts and principles. Sometimes all lab groups will work on the same problem, other times groups will work on different problems and share results.

1. Before beginning a new lab, carefully read the Introduction, Objectives and Preparation sections. Read sections of the text specified in the Preparation section.
2. Each lab contains several different experimental problems. Before you come to a lab, complete the assigned Prediction and $M$ ethod Questions. The Method Questions help you build a prediction for the given problem. It is usually helpful to answer the M ethod Questions before making the prediction. These individual predictions will be checked (graded) by your lab instructor immediately at the beginning of each lab session.
This preparation is crucial if you are going to get anything out of your laboratory work. There are at least two other reasons for preparing:
a) There is nothing duller or more exasperating than plugging mindlessly into a procedure you do not understand.
b) The laboratory work is a group activity whereevery individual contributes to the thinking process and activities of the group. Other members of your group will be unhappy if they must consistently carry the burden of someone who isn't doing his/ her share.

## C. Laboratory Reports

At the end of every lab (about once every two weeks) you will be assigned to write up one of the experimental problems. Your report must present a clear and accurate account of what you and your group members did, the results you obtained, and what the results mean. A report must not be copied or fabricated. (That would be scientific fraud.) Copied or fabricated lab reports will be treated in the same manner as cheating on a test, and will result in a failing grade for the course and possible expulsion from the University. Your lab report should describe your predictions, your experiences, your observations, your measurements, and your conclusions. A description of the lab report format is discussed at the end of this introduction. Each lab report is due, without fail, within two days of the end of that lab.

## D. Attendance

Attendance is required at all labs without exception. If something disastrous keeps you from your scheduled lab, contact your lab instructor immediately. The instructor will arrange for you to attend another lab section that same week. There are no make-up labs in this course.

## E. Grades

Satisfactory completion of the lab is required as part of your course grade. Those not completing all lab assignments by the end of the quarter at a $60 \%$ level or better will receive a quarter grade of F for the entire course. The laboratory grade makes up $15 \%$ of your final course grade. Once again, we emphasize that each lab report is due, without fail, within two days of the end of that lab.

There are two parts of your grade for each laboratory: (a) your laboratory journal, and (b) your formal problem report. Your laboratory journal will be graded by the lab instructor during the laboratory sessions. Your problem report will be graded and returned to you in your next lab session.

If you have made a good-faith attempt but your lab report is unacceptable, your instructor may allow you to rewrite parts or all of the report. A rewrite must be handed in again within two days of the return of the report to you by the instructor.
F. The laboratory class forms a local scientific community. There are certain basic rules for conducting business in this laboratory.

1. In all discussions and group work, full respect for all people is required. All disagreements about work must stand or fall on reasoned arguments about physics principles, the data, or acceptable procedures, never on the basis of power, loudness, or intimidation.
2. It is OK to make a reasoned mistake. It is in fact, one of the most efficient ways to learn.

This is an academic laboratory in which to learn things, to test your ideas and predictions by collecting data, and to determine which conclusions from the data are acceptable and reasonable to other people and which are not.

What do we mean by a "reasoned mistake"? We mean that after careful consideration and after a substantial amount of thinking has gone into your ideas you simply give your best prediction or explanation as you see it. Of course, there is always the possibility that your idea does not accord with the accepted ideas. Then someone says, "N o, that's not the way I see it and here's why." Eventually persuasive evidence will be offered for one viewpoint or the other.
"Speaking out" your explanations, in writing or vocally, is one of the best ways to learn.
3. It is perfectly okay to share information and ideas with colleagues. M any kinds of help are okay. Since members of this class have highly diverse backgrounds, you are encouraged to help each other and learn from each other.

## H owever, it is never okay to copy the work of others.

Helping others is encouraged because it is one of the best ways for you to learn, but copying is inappropriate and unacceptable. Write out your own calculations and answer questions in your own words. It is okay to make a reasoned mistake; it is wrong to copy.
||No credit will be given for copied work. It is also subject to University rules about plagiarism and cheating, and may result in dismissal from the course and the University. See the ||University course catalog for further information.
4. H undreds of other students use this laboratory each week. A nother class probably follows directly after you are done. Respect for the environment and the equipment in the lab is an important part of making this experience a pleasant one.

Thelab tables and floors should be clean of any paper or "garbage." Please clean up your area before you leave the lab. The equipment must be either returned to the lab instructor or left neatly at your station, depending on the circumstances.

## A note about Laboratory equipment:

At times equipment in the lab may break or may be found to be broken. If this happens you should inform your TA and report the problem to the equipment specialist using the Problem Report Form found on the desktop. To use the Problem Report Form you will have to login using your University ID and password. Describe the problem, including any identifying aspects of the equipment, and be sure to include your lab room number.

## If equipment appears to be broken in such a way as to cause a danger do not use the equipment and inform your TA immediately.

In summary, the key to making any community work is RESPECT.
Respect yourself and your ideas by behaving in a professional manner at all times.
Respect your colleagues (fellow students) and their ideas.

Respect your lab instructor and his/ her effort to provide you with an environment in which you can learn.

Respect the laboratory equipment so that others coming after you in the laboratory will have an appropriate environment in which to learn.

## WHAT IS EXPECTED IN A LAB REPORT? HOW IS IT HANDLED?

1. Before you leave the laboratory, have the instructor assign the problem you will write up and initial your cover sheet.
2. A cover sheet for each problem must be placed on top of each problem report handed in to the instructor. A cover sheet can be found at the end of every lab. It gives you a general outline of what to include in a report.
3. A problem report is always due within two days of the end of the lab.
4. A problem report should be an organized, coherent display of your thoughts, work, and accomplishments. It should be written neatly (word processor recommended) in English that is clear, concise, and correct. It may help you to imagine that hundreds of people will read your report and judge you by it. Communication is the goal of the report. In many cases, communication can be aided greatly by use of tables and graphs.
5. Sample reports are included in A ppendix E. Listed below are the major headings which most laboratory reports use.

## MAJOR PARTS OF A LABORATORY REPORT:

## COVER SHEET

See page 11 of this introduction for a sample cover sheet.

## TITLE

Write a descriptive title with your name, name of partners, date performed and TA name.

## STATEMENT OF THE PROBLEM

State the problem you were trying to solve, and how you went about it. Describe the general type of physical behavior explored and provide short summary of experiment.

## PREDICTION

This is a part of the lab where you try to the outcome of the experiment based on the general knowledge of Physics. Generally, you start from fundamental laws or principles and derive the theoretical expression for the measured quantity. Later you are going to use your prediction to compare with experimental results.

## EXPERIMENT AND RESULTS

Following the Prediction is an Experiment and Results section, containing a detailed description of how you made your measurements and what results you obtained. This usually involves an organized and coherent display of labeled diagrams, tables of measurements, tables of calculated quantities, and graphs. Explanations of all results must occur in correct grammatical English that would allow a reader to repeat your procedure. Also, include all information necessary to repeat your experiment.

Mathematical calculations connecting fundamental physics relationships to the quantities measured should be given. Any interesting behavior should be explained. Difficulties performing the experiment should be described as well as any subtleties in the analysis.

All data presented must be clearly identified and labeled. Calculated results should be clearly identified. Anybody should be able to distinguish between quantities you measured, those you calculated, and those you included from other sources. Clearly assign uncertainties to ALL measured values -- without uncertainties, the data is nearly meaningless.

## CONCLUSIONS

The Conclusions section should include your answers to the following questions: What generalized behavior did you observe? Was it different from what you expected? Why? (E.g.: What were the possible sources of uncertainties? Did you have any major experimental difficulties?) How do your results compare with the theory presented in your textbook or during lectures? Can you think of any other ways to check your theory with your data?

## REFERENCES

List books, journals or any other resources that you used to write your lab report.

# SAM PLE COVER SHEET <br> PHYSICS 1301LABORATORY REPORT Laboratory I 

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :---: |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |

PROBLEM REPORT:
ORGANIZATION
(clear and readable; logical progression from problem statement through conclusions; pictures provided where necessary; correct grammar and spelling; section headings provided; physics stated correctly)
DATA AND DATA TABLES
(clear and readable; units and assigned uncertainties clearly stated)
RESULTS
(results clearly indicated; correct, logical, and well-organized calculations with uncertainties indicated; scales, labels and uncertainties on graphs; physics stated correctly)

CONCLUSIONS
(comparison to prediction \& theory discussed with physics stated correctly ; possible sources
of uncertainties identified; attention called to experimental problems)
TOTAL(incorrect or missing statement of physics will result in a maximum of $60 \%$ of the total points achieved; incorrect grammar or spelling will result in a maximum of $70 \%$ of the total points achieved)

BONUS POINTS FOR TEAMWORK
(as specified by course policy)
An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.

## INTRODUCTORY LABORATORY O: DETERMINING AN EQUATION FROM A GRAPH

Throughout this course, you will use computer programs to graph physical quantities. Before measuring, you enter equations to represent predictions for the quantities to be measured. After measuring, you determine the equations that best represent (fit) the measured data, and compare the resulting Fit Equations with your Prediction Equations. This activity will familiarize you with the procedure for fitting equations to measured data.

## EXPLORATION

Log on to the computer. Open the PracticeFit program by doubleclicking its icon on the desktop. The "Instruction" box provides instructions that change as you progress. Holding the mouse over a button or the graph also provides some help.

You will try to fit equations to data generated by a Mystery Function. There are several sets of " Mystery Functions" to choose from; ranging from simpler (1) to more varied and complicated (10). The parameters, and in some cases the function types, are randomly chosen; you can try each Mystery Function several times until you are comfortable with it.

Follow the instructions on the screen until you are asked to select a "Fit Function" to approximate the Mystery Function data graphed on the screen. (You may need to change the graph's axis limits to locate the Mystery Function data!) The curve graphed for the Fit Function will change to match parameters you select; try to find the equation that gives the best possible fit to the Mystery Function data. The Warm Up Questions below are designed to help. Once you are satisfied with an equation, press "Accept Fit Function" to reveal the equation of the M ystery Function.

## Warm Up

The following questions should help you determine the equation that best matches the curve:

1. Determine the type of Fit Function that can best approximate the Mystery Function data. Examine the data's graph. Is it a straight line? If the graph bends, does it have a parabolic shape, an exponential shape, or a repeating pattern? Use your knowledge of functions to select the best equation type from the choices offered by P racticeF it.
2. Next you need to determine the constants in the equation. Examine the graph where the horizontal coordinate is zero:

- At this point, what is the value of the vertical coordinate of the graph? What constant in the Fit Function equation is represented by this vertical coordinate?
- At this same point, what is the slope of the graph, and what constant does it represent? (If you have taken some calculus, you will know that the derivative of a function represents the slope of its graph.)

If there are more constant parameters to determine for the Fit Function, you must look at other points on the graph; your knowledge of functions and calculus will help. You might examine points on the horizontal axis, points with zero slope, and/ or the graph's asymptotic behavior. It may also be useful to consider the derivative of theFit Function.

During the rest of this physics course, you will deal with real physical situations. You can usually determine the form of the best Fit Function and estimate its constant parameters based on your physics knowledge and what you observe in the laboratory; this can greatly simplify the fitting process.

## Conclusion

How close was your equation to the Mystery Function used to generate theeach curve? If your equation was not exactly the same as the actual equation, how would you determine what would be an acceptable degree of difference?

If the horizontal axis represents time and the vertical axis represents position, what type of motion might this curve represent?

## LABORATORY I: DESCRIPTION OF MOTION IN ONE DIMENSION

In this laboratory you will measure and analyze onedimensional motion; that is, motion along a straight line. With digital videos, you will measure the positions of moving objects at regular time intervals. You will investigate relationships among quantities useful for describing objects' motion. Determining these kinematics quantities (position, time, velocity, and acceleration) under different conditions allows you to develop an intuition about relationships among them. In particular, you should identify which relationships are only valid in some situations and which apply to all situations.

There are many possibilities for onedimensional motion of an object. It might move at a constant speed, speed up, slow down, or exhibit some combination of these. When making measurements, you must quickly understand your data to decide if the results make sense. If they don't make sense to you, then you have not set up the situation properly to explore the physics you desire, you are making measurements incorrectly, or your ideas about the behavior of objects in the physical world are incorrect. In any of the above cases, it is a waste of time to continue making measurements. You must stop, determine what is wrong, and fix it.

If your ideas are wrong, this is your chance to correct them by discussing the inconsistencies with your partners, rereading your text, or talking with your instructor. Remember, one of the reasons for doing physics in a laboratory setting is to help you confront and overcome your incorrect ideas about physics, measurements, calculations, and technical communications. Pinpointing and working on your own difficulties will help you in other parts of this physics course, and perhaps in other courses. Because people are faster at recognizing patterns in pictures than in numbers, the computer will graph your data as you go along.

## Objectives:

After you successfully completethis laboratory, you should be able to:

- Describe completely the motion of any object moving in one dimension using position, time, velocity, and acceleration.
- Distinguish between average quantities and instantaneous quantities for the motion of an object.
- Write the mathematical relationships among position, time, velocity, average velocity, acceleration, and average acceleration for different situations.
- Graphically analyze the motion of an object.
- Begin using technical communication skills such as keeping a laboratory journal and writing a laboratory report.


## Preparation:

Read Paul M. Fishbane: Chapter 2. Also read A ppendix D, the instructions for doing video analysis. Before coming to the lab you should be ableto:

- Define and recognize the differences among these concepts:
- Position, displacement, and distance.
- Instantaneous velocity and average velocity.
- Instantaneous acceleration and average acceleration.
- Find the slope and intercept of a straight-line graph. If you need help, see A ppendix C.
- Determine the slope of a curve at any point on that curve. If you need help, see A ppendix C.
- Determine the derivative of a quantity from the appropriate graph.
- Use the definitions of $\sin$ ?, $\cos$ ?, and $\tan$ ? for a right triangle.


## PROBLEM \#1: CONSTANT VELOCITY MOTION

Since this physics laboratory design may be new to you, this first problem, and only this one, contains both the instructions to explore constant velocity motion and an explanation of the various parts of the instructions. The explanation of the instructions is in this font and is preceded by the double, vertical lines seen to the left.
|These laboratory instructions may be unlike any you have seen before. You will not find worksheets or step-by-step instructions. Instead, each laboratory consists of a set of problems that you solve before coming to the laboratory by making an organized set of decisions (a problem solving strategy) based on your initial knowledge. The prediction and warm up questions are designed to help you examineyour thoughts about physics. These labs are your opportunity to compare your ideas about what "should" happen with what really happens. The labs will have little value in helping you learn physics unless you take time to predict what will happen before you do something.

While in the laboratory, take your time and try to answer all the questions in this lab manual. In particular, answering each of the exploration questions can save you time and frustration later by helping you understand the behavior and limitations of your equipment before you make measurements. Make sure to completethelaboratory problem, including all analysis and conclusions, before moving on to the next one.

The first paragraphs of each lab problem describe a real-world situation. Before coming to lab, you will solve a physics problem to predict something about that situation. The measurements and analysis you perform in lab will allow you to test your prediction against the behavior of the real world.

You have an internship managing a network of closed-circuit "Freeway cameras" for MnDOT Metro Traffic Engineering, Freeway Operations. Your boss wants to use images from those cameras to determine velocities of cars, particularly during unusual circumstances such as traffic accidents. Your boss knows that you have taken physics and asks you to prepare a presentation. During the presentation, you must demonstrate possibilities for determining a car's average vel ocity from graphs of its position vs. time, instantaneous velocity vs. time, and instantaneous acceleration vs. time. You decide to model the situation with a small digital camera and a toy car that moves at a constant velocity.

## EQUIPMENT

|This section contains abrief description of the apparatus you can use to test your prediction. Working through the exploration section will familiarize you with the details.

For this problem, you will use a motorized toy car, which moves with a constant velocity on an aluminum track. You will al so have a stopwatch, a meter stick, a video camera and a computer with video analysis applications written in LabVIEWTM (VideoRECORDER and VideoTOOL, described in A ppendix D ) to help you analyze the motion.

If equipment is missing or broken, please submit a problem report using the icon on the lab computer desktop. If you are unable to, please ask your TA to submit a problem report.

## Prediction

||Everyone has "personal theories" about the way the world works. One purpose of this lab is to help you clarify your conceptions of the physical world by testing the predictions of your personal theory against what really happens. For this reason, you will always predict what will happen before collecting and analyzing the data. Your prediction should be completed and written in your lab journal before you come to lab. The "Warm Up Questions" in the next section are designed to help you make your prediction and should also be completed before you come to lab. This may seem a little backwards. Although the "Prediction" section appears before the warm up questions, you should complete the warm up questions before making the prediction. The "Prediction" section merely |helps you identify the goal of the lab problem.
||Spend thefirst few minutes at the beginning of the lab session comparing your prediction with those of your partners. Discuss the reasons for differences in opinion. It is not necessary that your predictions |are correct, but it is absolutely crucial that you understand the basis of your prediction.

Sketch graphs of position vs. time, instantaneous velocity vs. time, and instantaneous acceleration vs. timefor the toy car. How could you determine the speed of the car from each graph?
||Sometimes your prediction is an "educated guess" based on your knowledge of the physical world. In these problems exact calculation is too complicated and is beyond this course. However, for every problem it's possible to come up with a qualitative prediction by making some plausible simplifications. For other problems, you will be asked to use your knowledge of the concepts and principles of physics to calculate a mathematical relationship between quantities in the experimental |problem.

## Warm Up

|Warm Up Questions are a series of questions intended to help you solve the problem stated in the opening paragraphs. They may help you make the prediction, help you plan how to analyze data, or help you think through the consequences of a prediction that is an educated guess. Warm Up questions should be answered and written in your lab journal before you come to lab and time |should be taken to complete the labSims before each lab period.

Read: Fishbane Chapter 2. Sections 2.1-2.4
To find schemes for determining a car's velocity, you need to think about representing its motion. The following questions should help.

1. How would you expect an instantaneous velocity vs. time graph to look for an object with constant velocity? Make a rough sketch and explain your reasoning. Assign appropriate labels and units to your axes. Write an equation that describes this graph. What is the
meaning of each quantity in your equation? In terms of the quantities in your equation, what is the velocity?
2. How would you expect an instantaneous acceleration vs. time graph to look for an object moving with a constant velocity? Make a rough sketch and explain your reasoning. Remember axis labels and units. Write down an equation that describes this graph. In this case, what can you say about the velocity?
3. How would you expect a position vs. timegraph to look for an object moving with constant velocity? Make a rough sketch and explain your reasoning. What is the relationship between this graph and the instantaneous velocity versus time graph? Write down an equation that describes this graph. What is the meaning of each quantity in your equation? In terms of the quantities in your equation, what is the velocity?
4. Use the simulation "Lab1Sim" to approximate the conditions of the cart's motion. (See A ppendix F for a brief explanation of how to use the simulations.) Look at the graphs produced by the simulation. You will need to experiment with he settings to find conditions that will produce a similar constant velocity motion. (See Appendix F for an introduction to the Simulation Programs.) The simulations allow you to create real time graphs that will help you understand the relationships between velocity, position, acceleration and time further. Produce simulated position vs. time and velocity vs. time graphs of constant velocity motion, and verify that they meet your expectations. Add a small amount of uncertainty to the position measurements by pressing "A dd Error" in the "Graph frame." N ote the effect of error in the position vs. time graph and in the velocity vs. time graph.

## EXPLORATION

||This section is extremely important—many instructions will not make sense, or you may be led astray, if you fail to carefully explore your experimental plan.
|| In this section you practice with the apparatus and carefully observe the behavior of your physical system before you make precise measurements. You will also explore the range over which your apparatus is reliable. Remember to always treat the apparatus with care and respect Students in the next lab section will use the equipment after you are finished with it. If you are unsure about how equipment works, ask your lab instructor. If at any time during the course of this lab you find a piece of equipment is broken, please submit a problem report using the icon on the desktop.

Most equipment has a range in which its operation is simple and straightforward. This is called its range of reliability. Outside that range, complicated corrections are needed. Be sure your planned measurements fall within the range of reliability. You can quickly determine the range of reliability by making qualitative observations at the extremes of your measurement plan. Record these observations in your lab journal. If the apparatus does not function properly for the ranges you plan to measure, you should modify your plan to avoid the frustration of useless measurements.
|At the end of the exploration you should have a plan for doing the measurements that you need. (Record your measurement plan in your journal.

## This exploration section is much longer than most. You will record and analyze digital videos several times during the semester.

Place one of the metal tracks on your lab bench and place the toy car on the track. Turn on the car and observe its motion. Qualitatively determine if it actually moves with a constant velocity. Use the meter stick and stopwatch to determine the speed of the car. Estimate the uncertainty in your speed measurement.

Turn on the video camera and look at the motion as seen by the camera on the computer screen. Go to A ppendix $D$ for instructions about using the VideoRECORDER software.

Do you need to focus the camera to get a clean image? Move the camera closer to the car. How does this affect the video image? Try moving it farther away. Raise the height of the camera tripod. How does this affect the image? Decide where you want to place the camera to get the most useful image.

Practice taking videos of the toy car. You will make and analyzemany videos in this course! Write down the best situation for taking a video in your journal for future reference. When you have the best movie possible, save it in the Lab Data folder on the desktop.

Quit VideoRECORDER and open VideoTOOL to analyze your movie.
Although the directions to analyze a video are given during the procedure in a box with the title "INSTRUCTIONS", the following is a short summary of them that will be useful to do the exploration for this and any other lab video (for more reference you should read at least once the A ppendix D ).

W arning: Be very careful in following these steps, if you make a mistake you may not be able to go backwards; you might need to restart from the first step.

1. Open the video that you are interested in by clicking the "Open Video" button.
2. Select "Begin calibration" and advance the video with the "Step >" button to the frame where the first data point will be taken. This step is very important because it sets up the origin of your time axis ( $\mathrm{t}=0$ ).
3. To tell the analysis program the real size of the video images, select some object in the plane of motion that you can measure. Drag the green cursor, located in the top left corner of the video display, to one end of the calibration object. Click the " $x 0, y 0$ " button when the green cursor is in place. Move the green cursor to the other end and select "x1, y 1 ". Enter the length of the object in the "Length" box and specify the "Units". Select the "OK" button twice to complete the calibration sequence.
4. Enter your prediction equations of how you expect the position to behave. Notice that the symbols used by the equations in the program are dummy letters, which means that you have to identify those with thequantities involved in your prediction. In order to do the best guess you will need to take into account the scale and the values from your practice trials using the stopwatch and the meter stick. Once that your x-position prediction is ready, select "A ccept $x$-prediction" and repeat the previous procedure for the y-position.
5. To start your data collection, click the "Acquire data" button. Select a specific point on the object whose motion you are analyzing. Drag the green cursor over this point and click the "Accept Data Point" button and you will see the data on the appropriate graph on your computer screen, after this the video will advance one frame. Drag again the green cursor over the same point selected on the object and accept the data point. Keep doing this until you have enough data.
6. Click the "AnalyzeData" button and fit your data. Decide which equation and constants are the best approximations for your data and accept your "x-fit" and " $y$-fit".
7. At this level the program will ask you to enter your predictions for velocity in $x$ and $y$ directions. Choose the appropriate equations and give your best approximations for the constants. Accept your $\mathrm{v}_{\mathrm{x}}$ - and $\mathrm{v}_{\mathrm{y}}$-predictions and you will see the data on the last two graphs.
8. Fit your data for these vel ocities in the same way that you did for position. Accept your fit and click the "Print Results" button to get a hard copy of your graphs.

Now you are ready to answer some questions that will be helpful for planning your measurements.

What would happen if you calibrate with an object that is not on the plane of the motion?
What would happen if you use different points on your car to get your data points?

## Measurement

|Now that you have predicted the result of your measurement and have explored how your apparatus behaves, you are ready to make careful measurements. To avoid wasting time and effort, make the minimal measurements necessary to convince yourself and others that you have solved the laboratory problem.

1. Record the time the car takes to travel a known distance. Estimate the uncertainty in time and distance measurements.
2. Take a good video of the car's motion. Analyze the video with VideoTOOL to predict and fit functions for position vs. time and velocity vs. time.

If possible, every member of your group should analyze a video. Record your procedures, measurements, prediction equations, and fit equations in a neat and organized manner so that you can understand them a month from now. Some future lab problems will require results from earlier ones.

## Analysis

|Data by itself is of very limited use. Most interesting quantities are those derived from the data, not direct measurements themselves. Your predictions may bequalitatively correct but quantitatively very wrong. To see this you must process your data.
|Always complete your data processing (analysis) before you take your next set of data. If something is going wrong, you shouldn't waste time taking a lot of useless data. After analyzing the first data, you may need to modify your measurement plan and re-do the measurements. If you do, be sure to record the changes in your plan in your journal.

Calculate the average speed of the car from your stopwatch and meter stick measurements. Determine if the speed is constant within your measurement uncertainties.

As you analyze data from a video, be sure to write down each of the prediction and fit equations for position and velocity.

When you have finished making a fit equation for each graph, rewrite the equations in a table but now matching the dummy letters with the appropriate kinetic quantities. If you have constant values, assign them the correct units.

## Conclusions

|After you have analyzed your data, you are ready to answer the experimental problem. State your result in the most general terms supported by your analysis. This should all be recorded in your journal in one place before moving on to the next problem assigned by your lab instructor. M ake sure you compare your result to your prediction.

Compare the car's speed measured with video analysis to the measurement using a stopwatch. Did your measurements and graphs agree with your answers to the Warm Up Questions? If not, why? Do your graphs match what you expected for constant velocity motion? What are the limitations on the accuracy of your measurements and analysis?

## SIM ULATION

If your graphs did not perfectly represent what you expect for constant velocity motion, use the simulation "Lab1Sim" (SeeA ppendix F for an introduction to the Simulation Programs) to see the effects of uncertainty in position measurement.

In VideoTOOL and "Lab1Sim", how do you think the computer generates data for a velocity graph? How is this related to the effect of measurement uncertainty on velocity (compared to position) graphs? Why is there one less data point in a velocity vs. time graph than in the corresponding position vs. time graph?

## PROBLEM \#2: <br> MOTION DOWN AN INCLINE

You have a job working with a team studying accidents for the state safety board. To investigate one accident, your team needs to determine the acceleration of a car rolling down a hill without any brakes. Everyone agrees that the car's velocity increases as it rolls down the hill but your team's supervisor believes that the car's acceleration also increases uniformly as it rolls down the hill. To test your supervisor's idea, you determine the acceleration of a cart as it moves down an inclined track in the laboratory.

## EQUIPMENT

For this problem you will have a stopwatch, a meter stick, an end stop, a wood block, a video camera and a computer with a video analysis application written in LabVIEWTM (VideoRECORDER and VideoTOOL applications.) You will also have a cart to roll down an inclined track.

Remember that if you have broken or missing equipment, submit a problem report using the icon on the lab computer desktop.


Consider the questions printed in italics, below, to make a rough sketch of how you expect the acceleration vs. time graph to look for a cart under the conditions given in the problem. Explain your reasoning.

D o you think the cart's acceleration changes as it moves down the track? If so, how does the acceleration change (increase or decrease)? Or, do you think the acceleration is constant (does not change) as the cart moves down the track?

## Warm Up

Read: FishbaneChapter 2. Sections 2.1-2.4
The following questions should help you to explore three different scenarios involving the physics given in the problem.

1. How would you expect an instantaneous acceleration vs. time graph to look for a cart moving with a constant acceleration? With a uniformly increasing acceleration? With a uniformly decreasing acceleration? Make a rough sketch of the graph for each possibility and explain your reasoning. To make the comparison easier, it is useful to draw these graphs next to each other. Remember to assign labels and units to your axes. Write down an equation for
each graph. Explain what the symbols in each of the equations mean. What quantities in these equations can you determine from your graph?
2. Write down the relationship between the acceleration and the velocity of the cart. Use that relationship to construct an instantaneous velocity versus time graph just below each of your acceleration versus time graphs from question 1 , with the same scale for each time axis. Write down an equation for each graph. Explain what the symbols in each of the equations mean. What quantities in these equations can you determine from your graph?
3. Write down the relationship between the velocity and the position of the cart. Use that relationship to construct a position versus time graph just below each of your velocity versus time graphs from question 2 , with the same scale for each time axis. Write down an equation for each graph. Explain what the symbols in each of the equations mean. What quantities in these equations can you determine from your graph?
4. Use the simulation "Lab1Sim" to approximate the conditions of the cart's motion. (See A ppendix F for a brief explanation of how to use the simulations.) Look at the graphs produced by the simulation. In the real world, friction or air resistance may affect your results. Try increasing and decreasing the friction and air resistance. Uncertainty in position measurements may affect your results. Try increasing and decreasing the measurement uncertainty. Use the simulation to compare the results with and without measurement uncertainties. Looking at these graphs, will reasonable uncertainty affect your ability to test the supervisor's statement?

## Exploration

In order to have an incline you will use the wood block and the aluminum track. This set up will give you an angle with respect to the table. How are you going to measure this angle? Hint: Think trigonometry!

Start with a small angle and with the cart at rest near the top of the track. Observe the cart as it moves down the inclined track. Try a range of angles. BE SURE TO CATCH THE CART BEFORE IT HITS THE END STOP! If the angle is too large, you may not get enough video frames, and thus enough position and time measurements, to measure the acceleration accurately. If the angle is too small the acceleration may be too small to measure accurately with the precision of your measuring instruments. Select the best angle for this measurement.

Where is the best place to release the cart so it does not damage the equipment but has enough of its motion captured on video? Be sure to catch the cart before it collides with the end stop.

When placing the camera, consider which part of the motion you wish to capture. Try different camera positions until you get the best possible video. Make sure you have a good object in your video to calibrate with.

Hint: Y our video may be easier to analyze if the motion on the video screen is purely horizontal. W hy? It could be useful to rotate the camera!

What is the total distance through which the cart rolls? How much time does it take? These measurements will help you set up the graphs for your computer data taking.

You may wish to follow the steps given in the "Exploration" section of problem 1 to work with your video. Write down your measurement plan.

## Measurement

Follow the measurement plan you wrote down.

When you have finished making measurements, you should have printouts of position and velocity graphs and good records (including uncertainty) of: your determination of the incline angle, the time it takes the cart to roll a known distance down the incline starting from rest, the length of the cart, and prediction and fit equations for position and velocity.
$M$ ake sure that every one gets the chance to oper ate the computer.
Record all of your measurements; you may be able to reuse some of them in other lab problems.

N ote: Be sure to record your measurements with the appropriate number of significant figures (see A ppendix A) and with your estimated uncertainty ( $\sec A$ ppendix $B$ ). O therw ise, the data is nearly meaningless.

## Analysis

Calculate the cart's average acceleration from the distance and time measurements you made with a meter stick and stopwatch.

Look at your graphs and rewrite all of the equations in a table but now matching the dummy letters with the appropriate kinetic quantities. If you have constant values, assign them the correct units, and explain their meaning.

From the velocity vs. time graph, determine if the acceleration is constant, increasing, or decreasing as the cart goes down the ramp. Use the function representing the velocity vs. time graph to calculate the acceleration of the cart as a function of time. Make a graph of that function. Is the average acceleration of the cart equal to its instantaneous acceleration in this case?

Compare the accelerations for the cart you found with your video analysis to your acceleration measurement using a stopwatch.

## CONCLUSION

How do the graphs of your measurements compare to your predictions?
Was your boss right about how a cart accelerates down a hill? If yes, state your result in the most general terms supported by your analysis. If not, describe how you would convince your boss of your conclusions. What are the limitations on the accuracy of your measurements and analysis?

Address (or re-address if you have already considered them) the following questions. In VideoTOOL and "Lab1Sim", how do you think the computer generates data for a velocity graph? How is this related to the effect of measurement uncertainty on velocity (compared to position) graphs? Why is there one less data point in a velocity vs. time graph than in the corresponding position vs. time graph?

## PROBLEM \#3: <br> MOTION UP AND DOWN AN INCLINE

A proposed ride at the Valley Fair amusement park launches a roller coaster car up an inclined track. Near the top of the track, the car reverses direction and rolls backwards into the station. A s a member of the safety committee, you have been asked to describe the acceleration of the car throughout the ride. (The launching mechanism has been well tested. You are only concerned with the roller coaster's trip up and back down.) To test your expectations, you decide to build a laboratory model of the ride.

## EQUIPMENT

For this problem you will have a stopwatch, a meter stick, an end stop, a wood block, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\text {™ }}$ (VideoRECORDER and VideoTOOL applications). You will also have a cart to roll up an inclined track.

Remember that if you have broken or missing equipment, submit a problem report using the icon on the lab computer desktop.


Make a rough sketch of how you expect the acceleration vs. time graph to look for a cart with the conditions discussed in the problem. The graph should be for the entire motion of going up the track, reaching thehighest point, and then coming down the track.

D o you think the acceleration of the cart moving up an inclined track will be greater than, less than, or the same as the acceleration of the cart moving down the track? What is the acceleration of the cart at its highest point? Explain your reasoning.


Read: FishbaneChapter 2. Sections 2.1-2.4

The following questions should help you examine the consequences of your prediction.

1. Sketch a graph of theinstantaneous acceleration vs. timegraph you expect for the cart as it rolls up and then back down the track after an initial push. Sketch a second instantaneous acceleration vs. timegraph for a cart moving up and then down the track with the direction of a constant acceleration always down along the track after an initial push. On each graph, label the instant where the cart reverses its motion near the top of the track. Explain your reasoning for each graph. Write down the equation(s) that best represents each graph. If
there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs?
2. Write down the relationship between the acceleration and the velocity of the cart. Use that relationship to construct an instantaneous velocity vs. time graph just below each of acceleration vs. time graph from question 1, with the same scale for each time axis. (The connection between the derivative of a function and the slope of its graph will be useful.) On each graph, label the instant where the cart reverses its motion near the top of the track. Write an equation for each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of the constants be determined from the constants in the equation representing the acceleration vs. time graphs?
3. Write down the relationship between the velocity and the position of the cart. Use that relationship to construct an instantaneous position vs. time graph just below each of your velocity vs. time graphs from question 2 , with the same scale for each time axis. (The connection between the derivative of a function and the slope of its graph will be useful.) On each graph, label the instant where the cart reverses its motion near the top of the track. Write down an equation for each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of the constants be determined from the constants in the equations representing velocity vs. time graphs?
4. Which graph do you think best represents how position of the cart will change with time? Adjust your prediction if necessary and explain your reasoning.
5. Use the simulation "Lab1Sim" to approximate the conditions of the cart's motion. (See A ppendix F for a brief explanation of how to use the simulations.) Look at the graphs produced by the simulation. If you believe friction or air resistance may affect your results, explore the effects of each with the simulation. If you believe that uncertainty in position measurements may affect your results, use the simulation to compare the results with and without error. Note the difference in the effect in the position vs. time and velocity vs. time graph. Remember to check for the effects of measurement uncertainty in your VideoTOOL measurements later in lab.

## EXPLORATION

What is the best way to change the angle of the inclined track in a reproducible way? How are you going to measure this angle with respect to the table? (Think about trigonometry.)

Start the cart up the track with a gentle push. BE SURE TO CATCH THE CART BEFORE IT HITS
THE END STOP ON ITS WAY D OWN! Observe the cart as it moves up the inclined track. At the instant the cart reverses direction, what is its velocity? Its acceleration? Observe the cart as it moves down the inclined track. Do your observations agree with your prediction? If not, discuss it with your group.

Where is the best place to put the camera? Which part of the motion do you wish to capture?

Try different angles. Be sure to catch the cart before it collides with the end stop at the bottom of the track. If the angle is too large, the cart may not go up very far and will give you too few video frames for the measurement. If the angle is too small it will be difficult to measure the acceleration. Take a practice video and play it back to make sure you have captured the motion you want (see the "Exploration" section in Problem 1, and appendix D, for hints about using the camera and VideoRECORDER / VideoTOOL.) Hint: To analyze motion in only one dimension (like in the previous problem) rather than two dimensions, it could be useful to rotate the camera!

What is the total distance through which the cart rolls? Using your stopwatch, how much time does it take? These measurements will help you set up the graphs for your computer data taking, and can providefor a check on your video analysis of the cart's motion.

Write down your measurement plan.

## Measurement

Follow your measurement plan to make a video of the cart moving up and then down the track at your chosen angle. Record the timeduration of the cart's trip, and the distance traveled. Make sure you get enough points for each part of the motion to determine the behavior of the acceleration. Don't forget to measure and record the angle (with estimated uncertainty).

Work through the complete set of calibration, prediction equations, and fit equations for a single (good) video before making another video.
$M$ ake sure everyone in your group gets the chance to operate the computer.

## AnAlysis

From the time given by the stopwatch and the distance traveled by the cart, calculate its average acceleration. Estimate the uncertainty.

Look at your graphs and rewrite all of the equations in a table but now matching the dummy letters with the appropriate kinetic quantities. If you have constant values, assign them the correct units, and explain their meaning.

Can you tell from your graph where the cart reaches its highest point?
From thevelocity vs. time graph determine if the acceleration changes as the cart goes up and then down the ramp. Use the function representing the velocity vs. time graph to calculate the acceleration of the cart as a function of time. Make a graph of that function. Can you tell from this instantaneous acceleration vs. time graph where the cart reaches its highest point? Is the average acceleration of the cart equal to its instantaneous acceleration in this case?

Compare the acceleration function you just graphed with the average acceleration you cal culated from the time on the stopwatch and the distance the cart traveled.

## CONCLUSION

How do your position vs. time, velocity vs. time graphs compare with your answers to the warm up questions and the prediction? What are the limitations on the accuracy of your measurements and analysis?

Did the cart have the same acceleration throughout its motion? Did the acceleration change direction? Was the acceleration zero at the top of its motion? Describe the acceleration of the cart through its entire motion after the initial push. Justify your answer with kinematics arguments and experimental results. If there are any differences between your predictions and your experimental results, describe them and explain why they occurred.

If your data did not match your expectations, you should go back and use the simulation to explore what could have happened. A scheme for doing so is outlined at the end of Problem 2 in this lab.

## PROBLEM \#4: <br> MOTION DOWN AN INCLINE WITH NON-ZERO INITIAL VELOCITY

Because of your physics background, you have a summer job with a company that is designing a new bobsled for the U.S. team to use in the next Winter Olympics. You know that the success of the team depends crucially on the initial push of the team members - how fast they can push the bobsled before they jump into the sled. You need to know in more detail how that initial velocity affects the motion of the bobsled. In particular, your boss wants you to determine if the initial velocity of the sled affects its acceleration down the ramp. To solve this problem, you decide to model the situation using a cart moving down an inclined track.

## EqUIPMENT

You will have a stopwatch, a meter stick, an end stop, a wood block, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\text {TM }}$. You will also have a cart to roll down an inclined track.

Remember that if you have broken or missing equipment to submit a problem report using the icon on the lab computer desktop.


Do you think the cart launched down the inclined track will have a larger acceleration, smaller acceleration, or the same acceleration as the cart released from rest?

## Warm Up

Read: FishbaneChapter 2. Read carefully Sections 2-3, 2-4 and Examples 2-7, 2-8.
The following questions should help you (a) understand the consequences of your prediction and (b) interpret your measurements.

1. Sketch a graph of instantaneous acceleration vs. time graph when the cart rolls down the track after an initial push (your graph should begin after the initial push.) Compare this to an instantaneous acceleration vs. time graph for a cart released from rest (To make the comparison easier, draw the graphs next to each other.) Explain your reasoning for each graph. Write down the equation(s) that best represents each of the graphs. If there are constants in your equations, what kinematics quantities do they represent? How would you determine the constants from your graphs?
2. Write down the relationship between the acceleration and the velocity of the cart. Use that relationship to construct an instantaneous velocity vs. time graph, after an initial push, just
below each of your acceleration vs. timegraphs from question 1. Use the same scale for your time axes. (The connection between the derivative of a function and the slope of its graph will be useful.) Write down the equation that best represents each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine the constants from your graphs? Can any of the constants be determined from the equations representing the acceleration vs. time graphs?
3. Write down the relationship between the velocity and the position of the cart. Use that relationship to construct a position vs. time graph, after an initial push, just below each velocity vs. time graph from question 2 . Use the same scale for your time axes. (The connection between the derivative of a function and the slope of its graph will be useful.) Write down the equation that best represents each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of these constants be determined from the equations representing the velocity vs. timegraphs?
4. Use the simulation "Lab1Sim" to explore the approximate the conditions of your experiment. Use a range of initial velocities and check the affect on the graphs. If you believe air resistance or friction affected the results, explore the effects of each with the simulation. If you believe that uncertainty in position measurements may affect your results, use the simulation to compare the results with and without error. Remember to check for the effects of measurement uncertainty in your VideoTOOL measurements later in lab.

## Exploration

Slant the track at an angle. (Hint: Is there an angle that would allow you to reuse some of your measurements and calculations from other lab problems?)

Determine the best way to gently launch the cart down the track in a consistent way without breaking the equipment. BE SURE TO CATCH THE CART BEFOREIT HITS THE END STOP!

Where is the best place to put the camera? Is it important to have most of the motion in the center of the picture? Which part of the motion do you wish to capture? Try taking some videos before making any measurements. Be sure to catch the cart before it collides with the end stop at the bottom of the track.

What is the total distance through which the cart rolls? How much time does it take? These measurements will help you set up the graphs for your computer data taking.

Write down your measurement plan. Make sure everyone in your group gets the chance to operate the camera and the computer.


Using the plan you devised in the exploration section, make a video of the cart moving down the track at your chosen angle. Make sure you get enough points for each part of the motion to determine the behavior of the acceleration. D on't forget to measure and record the angle (with estimated uncertainty).

Choose an object in your picture for calibration. Choose your coordinate system. Is a rotated coordinate system the easiest to use in this case?

Why is it important to click on the same point on the car's image to record its position? Estimate your accuracy in doing so.

Make sure you set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the cart travels and total time to determine the maximum and minimum value for each axis before taking data.

## Analysis

Choose a function to represent the position vs. time graph. How can you estimate the values of the constants of the function from the graph? You may waste a lot of time if you just try to guess the constants. What kinematics quantities do these constants represent?

Choose a function to represent the vel ocity versus time graph. How can you calculate the values of the constants of this function from the function representing the position versus time graph? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematics quantities do these constants represent?

From the velocity versus time graph, determine the acceleration as the cart goes down the ramp after the initial push. Use the function representing the velocity versus time graph to calculate the acceleration of the cart as a function of time. Make a graph of that function.

As you analyze your video, make sure everyone in your group gets the chance to operate the computer.

## Conclusions

Look at the graphs you produced through video analysis. How do they compareto your answers to the warm up questions and your predictions? Explain any differences. What are the limitations on the accuracy of your measurements and analysis?

What will you tell your boss? Does the acceleration of the bobsled down the track depend on the initial velocity the team can give it? Does the velocity of the bobsled down the track depend on the initial velocity the team can give it? State your result in the most general terms supported by your analysis.

If your data did not match your expectations, you should use the simulation to explore what could have happened. A scheme for doing so is outlined at the end of Problem 2 in this lab.

## PROBLEM \#5: MASS AND MOTION DOWN AN INCLINE

Your neighbors' child has asked for your help in constructing a soapbox derby car. In the soapbox derby, two cars are released from rest at the top of a ramp. The one that reaches the bottom first wins. The child wants to make the car as heavy as possible to give it the largest acceleration. Is this plan reasonable?

## EQUIPMENT

You will have a stopwatch, a meter stick, an end stop, a wood block, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\top 1}$. You will also have a cart to roll down an inclined track and additional cart masses to add to the cart. Submit any problems using the icon on the desktop of the lab computers.

## Prediction

Do you think that increasing the mass of the cart increases, decreases, or has no effect on the cart's acceleration?

## Warm Up

Read: FishbaneChapter 2. Read carefully Sections 2-3, 2-4 and Examples 2-7, 2-8.
The following questions should help you (a) understand the consequences of your prediction and (b) interpret your measurements.

1. Make a sketch of the acceleration vs. time graph for a cart released from rest on an inclined track. On the same axes sketch an acceleration vs. time graph for a cart on the same incline, but with a much larger mass. Explain your reasoning. Write down the equations that best represent each of these accelerations. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs?
2. Write down the relationship between the acceleration and the velocity of the cart. Use that relationship to construct an instantaneous velocity vs. time graph for each case. (The connection between the derivative of a function and the slope of its graph will be useful.) Write down the equation that best represents each of these velocities. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of these constants be determined from the equations representing the accelerations?
3. Write down the relationship between the velocity and the position of the cart. Use that relationship to construct a position vs. time graph for each case. The connection between the derivative of a function and the slope of its graph will be useful. Write down the equation that best represents each of these positions. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of these constants be determined from the equations representing the velocities?
4. Use the simulation "Lab1Sim" to explore the approximate the conditions of your experiment. Use a range of values for the mass of the cart and check the affect on the graph.


Slant the track at an angle. (Hint: Is there an angle that would allow you to reuse some of your measurements and calculations from other lab problems?)

Observe the motion of several carts of different mass when released from rest at the top of the track. BE
SURE TO CATCH THE CART BEFORE IT HITS THE END STOP! From your estimate of the size of the effect, determine the range of mass that will give the best results in this problem. Determine the first two masses you should use for the measurement.

How do you determine how many different masses do you need to use to get a conclusive answer? How will you determine the uncertainty in your measurements? How many times should you repeat these measurements? Explain.

What is the total distance through which the cart rolls? How much time does it take? These measurements will help you set up the graphs for your computer data taking.

Write down your measurement plan.
$M$ ake sure everyone in your group gets the chance to operate the camera and the computer.

## Measurement

Using the plan you devised in the exploration section, make a video of the cart moving down the track at your chosen angle. Make sure you get enough points for each part of the motion to determine the behavior of the acceleration. D on't forget to measure and record the angle (with estimated uncertainty).

Choose an object in your picture for calibration. Choose your coordinate system. Is a rotated coordinate system the easiest to use in this case?

Why is it important to click on the same point on the car's image to record its position? Estimate your accuracy in doing so.

Make sure you set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the cart travels and the total time to determine the maximum and minimum value for each axis beforetaking data.

Make several videos with carts of different mass to check your qualitative prediction. If you analyze your data from the first two masses you use before you make the next video, you can determine which mass to use next. A s usual you should minimize the number of measurements you need.


Choose a function to represent the position vs. time graph. How can you estimate the values of the constants of the function from the graph? You may waste a lot of time if you just try to guess the constants. What kinematics quantities do these constants represent?

Choose a function to represent the velocity vs. time graph. How can you calculate the values of the constants of this function from the function representing the position vs. time graph? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematics quantities do these constants represent?

From the velocity vs.time graph determine the acceleration as the cart goes down the ramp. Use the function representing the velocity-versus-time graph to calculate the acceleration of the cart as a function of time.

Make a graph of the cart's acceleration down the ramp as a function of the cart's mass. Do you have enough data to convince others of your conclusion about how the acceleration of the cart depends on its mass?

As you analyzeyour video, make sure everyone in your group gets the chance to operate the computer.

## Conclusion

Did your measurements of the cart's motion agree with your initial predictions? Why or why not? What are the limi tations on the accuracy of your measurements and analysis?

What will you tell the neighbors' child? Does the acceleration of the car down its track depend on its total mass? Does the velocity of the car down its track depend on its mass? State your result in the most general terms supported by your analysis.

If your data did not match your expectations, you should use the simulation to explore what could have happened. A scheme for doing so is outlined at the end of Problem 2 in this lab.

## PROBLEM \#6:

## MOTION ON A LEVEL SURFACE WITH AN ELASTIC CORD

You are helping a friend design a new ridefor the State Fair. In this ride, a cart is pulled from rest along a long straight track by a stretched elastic cord (like a bungee cord). Before building it, your friend wants to you to determine if this ride will be safe. Since sudden changes in velocity can lead to whiplash, you decide to find out how the acceleration of the cart changes with time. In particular, you want to know if the greatest acceleration occurs when the sled is moving the fastest or at some other time. To test your prediction, you decide to model the situation in the laboratory with a cart pulled by an elastic cord along a level surface.

## EQUIPMENT

You will have a stopwatch, a meter stick, a scissor, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\mathrm{TM}}$. You will also have a cart to roll on a level track. You can attach one end of an elastic cord to the cart and the other end of the elastic cord to an end stop on the track. Submit any problems using the icon on the lab computers desktop.

## Prediction

Make a qualitative sketch of how you expect the acceleration vs. time graph to look for a cart pulled by an elastic cord. Just below that graph make a qualitative graph of the velocity vs. time on the same time scale. Identify on each graph where the velocity is largest and where the acceleration is largest.

## Warm UP

Read: Fishbane Chapter 2. Read carefully Section 2-4.
The following questions should help you (a) understand the consequences of your prediction and (b) interpret your results.

1. Make a qualitative sketch of how you expect an acceleration vs. time graph to look for a cart pulled by an elastic cord. Explain your reasoning. For a comparison, make an acceleration vs. time graph for a cart moving with constant acceleration. Point out the differences between the two graphs.
2. Write down the relationship between the acceleration and the velocity of the cart. Use that relationship to construct a qualitative velocity vs. time graph for each case. (The connection between the derivative of a function and the slope of its graph will be useful.) Point out the differences between the two velocity vs. time graphs.
3. Write down the relationship between the velocity and the position of the cart. Use that relationship to construct a qualitative position vs. time graph for each case. (The connection between the derivative of a function and the slope of its graph will be useful.) Point out the differences between the two graphs.

## EXPLORATION

Test that the track is level by observing the motion of the cart. Attach an elastic cord to the cart and track. Gently move the cart along the track to stretch out the elastic. Be careful not to stretch the elastic too tighty. Start with a small stretch and release the cart. BE SURE TO CATCH THE CART BEFORE IT HITS THE END STOP! Slowly increase the starting stretch until the cart's motion is long enough to get enough data points on the video, but does not cause the cart to come off the track or snap the elastic.

Practice releasing the cart smoothly and capturing videos.

Write down your measurement plan.
$M$ ake sure everyone in your group gets the chance to operate the camera and the computer.

## Measurement

Using the plan you devised in the exploration section, make a video of the cart's motion. Make sure you get enough points to determine the behavior of the acceleration.

Choose an object in your picture for calibration. Choose your coordinate system.
Why is it important to click on the same point on the car's image to record its position? Estimate your accuracy in doing so.

Make sure you set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the cart travels and total time to determine the maximum and minimum value for each axis before taking data.


Can you fit your position-versus time data with an equation based on constant acceleration? Do any other functions fit your data better?

From the position vs. time graph or your fit equation for it, predict an equation for the velocity vs. time graph of the cart.

From the velocity vs. time graph, sketch an acceleration vs. time graph of the cart. Can you determine an equation for this acceleration vs. time graph from the fit equation for the vel ocity vs. timegraph?

Do you have enough data to convince others of your conclusion?

As you analyze your video, make sure everyone in your group gets the chance to operate the computer.

## CONCLUSION

How does your acceleration-versus-time graph compare with your predicted graph? Are the position-versus-time and the velocity-versus-time graphs consistent with this behavior of acceleration? What is the difference between the motion of the cart in this problem and its motion along an inclined track? What are the similarities? What are the limitations on the accuracy of your measurements and analysis?

What will you tell your friend? Is the acceleration of the cart greatest when the velocity is the greatest? How will a cart pulled by an elastic cord accelerate along a level surface? State your result in the most general terms supported by your analysis.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING:

1. Suppose you are looking down from a helicopter at three cars traveling in the same direction along the freeway. The positions of the three cars every 2 seconds are represented by dots on the diagram below. The positive direction is to the right.

a. At what clock reading (or time interval) do Car A and Car B have very nearly the same speed? Explain your reasoning.
b. At approximately what clock reading (or readings) does one car pass another car? In each instance you cite, indicate which car, $A, B$ or $C$, is doing the overtaking. Explain your reasoning.
c. Suppose you calculated the average velocity for Car B between $\mathrm{t}_{1}$ and $\mathrm{t}_{5}$. Where was the car when its instantaneous velocity was equal to its average velocity? Explain your reasoning.
d. Which graph below best represents the position vs. time graph of Car A? Of Car B? Of car C? Explain your reasoning.
e. Which graph below best represents the instantaneous velocity vs. time graph of Car A? Of Car B? Of car C? Explain your reasoning. (HINT: Examine the distances traveled in successivetime intervals.)
f. Which graph below best represents the instantaneous acceleration vs. time graph of Car A? Of Car B? Of car C? Explain your reasoning.

(a)


(g)

(b)

(e)

(h)




## $\square$ CHECK YOUR UNDERSTANDING

2. A cart starts from rest at the top of a hill, rolls down the hill, over a short flat section, then back up another hill, as shown in the diagram above. Assume that the friction between the wheels and the rails is negligible. The positive direction is to the right.

a. Which graph below best represents the position vs. time graph for the motion along the track? Explain your reasoning. (Hint: Think of motion as onedimensional.)
b. Which graph below best represents the instantaneous velocity vs. timegraph? Explain your reasoning.
c. Which graph below best represents the instantaneous acceleration vs. timegraph? Explain your reasoning.

(a)

(d)


(b)

(e)

(h)



$\qquad$

## PHYSICS 1301LABORATORY REPORT <br> Laboratory I

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readable; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics <br> stated correctlyy |  |
| DATA AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly ; possible sources <br> of uncertainties identified; attention called to experimental problems) |  |
| TOTAL(incorrect or missing statement of physics will result in a maximum of 60\% of the <br> total points achievdi incorrect grammar or spelling will result in a maximum of 70\% of the <br> total points achieved) |  |
| BONUS aOINTS FOR TEAMWORK <br> (as specified by course policy) |  |

* An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORY II DESCRIPTION OF MOTION IN TWO DIMENSIONS

In this laboratory you continue the study of accelerated motion in more situations. The carts you used in Laboratory I moved in only one dimension. Objects don't always move in a straight line. However, motion in two and three dimensions can be decomposed into a set of onedimensional motions; what you learned in the first lab can be applied to this lab. You will also need to think of how air resistance could affect your results. Can it always be neglected? You will study the motion of an object in free fall, an object tossed into the air, and an object moving in a circle. As always, if you have any questions, talk with your fellow students or your instructor.

## Objectives:

After successfully completing this laboratory, you should be able to:

- Determine the motion of an object in freefall by considering what quantities and initial conditions affect the motion.
- Determine the motion of a projectile from its horizontal and vertical components by considering what quantities and initial conditions affect the motion.
- Determine the motion of an object moving in a circle from its horizontal and vertical components by considering what quantities and initial conditions affect the motion.


## Preparation:

Read Paul M. Fishbane: Chapter 3. Review your results and procedures from Laboratory I. Before coming to the lab you should be able to:

- Determine instantaneous velocities and accelerations from video images.
- A nalyze a vector in terms of its components al ong a set of perpendicular axes.
- Add and subtract vectors.

After completing this laboratory seeA ppen dix E (Sample Lab Report 1) for some suggestions on how to improve your lab reports.

## PROBLEM \#1:

MASS AND ACCELERATION OF A FALLING BALL

You have a job with the National Park Service. Your task is to investigate the effectiveness of spherical canisters filled with fire-retarding chemicals to help fight forest fires. The canisters would be dropped by low-flying planes or helicopters. They are specifically designed to split open when they hit the ground, showering the nearby flames with the chemicals. The canisters could contain different chemicals, so they will have different masses. In order to drop the canisters accurately, you need to know if the motion of a canister depends on its mass. You decide to model the situation by measuring the free-fall acceleration of balls with similar sizes but different masses.

## EQUIPMENT

For this problem, you will have a collection of balls each with approximately the same diameter. You will also have a stopwatch, a meter stick, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\top M}$ (VideoRECORDER and VideoTOOL applications).

## Prediction

Make a sketch of how you expect the average acceleration vs. mass graph to look for falling objects such as the balls in the problem.

Do you think that the freefall acceleration increases, decreases, or stays the same as the mass of the object increases? M ake your best guess and explain your reasoning.

## Warm Up

Read: FishbaneChapter 2, section 2.5.

Answering these questions will help you understand the implications of your prediction and interpret your experimental results.

1. Sketch a graph of acceleration as a function of time for a constant acceleration. Below it, make graphs for velocity and position as functions of time. Write down the equations that best represent each graph. If there are constants in each equation, what kinematics quantities do they represent? How would you determine these constants from your graphs?
2. Make two more sketches of the acceleration vs. time graph: one for a heavy falling ball and another for a falling ball with one quarter of the heavy one's mass. Explain your reasoning. Write the equation that best represents each of acceleration. If there are constants in your equations, what kinematics quantities do they represent? How would you determine the constants from your graphs? How do they differ from each other, and from your constant acceleration graph?
3. Use the relationships between acceleration and velocity and velocity and position of the ball to construct an instantaneous velocity vs. time graph and a position vs. time graph for each case from the previous question. The connection between thederivative of a function and the slope of its graph will be useful. Write down the equations that best represent each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of these constants be determined from the constants in the equations representing the acceleration and velocity?
4. Compare your graphs to those for constant acceleration. What are the differences, if any, that you might observe in your data? The similarities?
5. Write down an outline of how you will determine the acceleration of the object from video data.
6. Use the simulation "Lab2Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the approximate the conditions of your experiment. Look at the graphs produced through simulated freefall. (The initial position of the ball should be well off the table, and the initial speed should be zero. N ote that the initial position and velocity parameters in Lab2Sim are specified as vectors of the form $\left\langle\mathrm{x}_{0}, \mathrm{y}_{0}, \mathrm{z}_{0}\right\rangle$ and $\left\langle\mathrm{v}_{\mathrm{x} 0}, \mathrm{v}_{\mathrm{y} 0}, \mathrm{v}_{\mathrm{z} 0}\right\rangle$. The x -axis is along the Right/ Left direction, the y -axis is Up/ Down, and the z-axis is Front/ Back.) If you believe air resistance may affect your results, explore the effects with the simulation. Check the graphs of position and velocity with various values for air resistance. Test the effects of a large air resistance on the ball's velocity and acceleration. If you believe that uncertainty in position measurements may affect your results, use the simulation to compare the results with and without error. N ote the difference in effect on the position vs. time graph and the velocity vs. time graph.

## EXPLORATION

Review your lab journal from the problems in Lab 1. Position the camera and adjust it for optimal performance. $M$ ake sure everyone in your group gets the chance to operate the camera and the computer.

Practice dropping one of the balls until you can get the ball's motion to fill the screen. Determine how much time it takes for the ball to fall and estimate the number of video points you will get in that time. Are there enough points to make the measurement? Adjust the camera position to give you enough data points.

Although the ball is the best item to use to calibrate the video, the image quality due to its motion might make this difficult. Instead, you might hold an object of known length in the plane of motion of the ball, near the center of the ball's trajectory, for calibration purposes. Where you place your reference object does make a difference in your results. Check your video image when you put the reference object close to the camera and then further away. What do you notice about the size of the reference object in the video image? The best place to put the reference object to determine the distance scale is at the position of the falling ball.

Step through the video and determine which part of the ball is easiest to consistently determine. When the ball moves rapidly you may see a blurred image due to the camera's finite shutter speed. If you cannot make the shutter speed faster, devise a plan to measure the position of the same part of the "blur" in each video frame. You also have the option of changing the camera settings.

Write down your measurement plan.

## Measurement

Measure the mass of a ball and make a video of its fall according to the plan you devised in the exploration section.

Digitize the position of the ball in enough frames of the video so that you have the sufficient data to accomplish your analysis. Make sure you set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the ball travels and total time to determine the maximum and minimum value for each axis before taking data.

Complete your data analysis as you go along (before making the next video), so you can determine how many different videos you need to make. Don't waste time in collecting data you don't need or, even worse, incorrect data. Collect enough data to convince yourself and others of your conclusion.

Repeat this procedure for different balls.

## Analysis

Choose a function to represent the position vs. time graph. How can you estimate the values of the constants of the function from the graph? You can waste a lot of time if you just try to guess the constants. What kinematic quantities do these constants represent?

Choose a function to represent the velocity vs. time graph. How can you calculate the values of the constants of this function from the function representing the position vs. time graph? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematic quantities do these constants represent?

If you cannot get one function to describe your velocity graph in a consistent way, you can try using one function for the first half of the motion and another for the last half. To do this you must go through the video analysis process twice and record your results each time. (How can you avoid repeating some work with the "SaveSession" and "Open Session" commands?)

From the velocity vs. time graph(s) determine the acceleration of the ball. Use the function representing the velocity vs. time graph to calculate the acceleration of the ball as a function of time. Is the average acceleration different for the beginning of the video (when the object is moving slowly) and the end of the video (when the object is moving fast)?

Determine the average acceleration of the object in free fall for each value of its mass and graph this result. Do you have enough data to convince others of your conclusions about your predictions?

## Conclusion

Did the data support your predicted relationship between acceleration and mass? (Make sure you carefully review Appendix C to determine if your data really supports this relationship.) If not, what assumptions did you makethat were incorrect? Explain your reasoning.

What are the limitations on the accuracy of your measurements and analysis?
Do your results hold regardless of the masses of balls? Would the acceleration of a falling Styrofoam ball be the same as the acceleration of a falling baseball? Explain your rationale. Makesure you have some data to back up your claim. Will the acceleration of a falling canister depend on its mass? State your results in the most general terms supported by your analysis.

## SIMULATION

If your results did not completely match your expectations, you should use the simulation "Lab2Sim" again (See A ppendix F for a brief explanation of how to use the simulations) to explore what might have happened.

## PROBLEM \#2:

ACCELERATION OFA BALL WITH AN INITIAL VELOCITY

You have designed an apparatus to measure air quality in your city. To quickly force air through the apparatus, you will launch it straight downward from the top of a tall building. A very large acceleration may destroy sensitive components in the device; the launch system's design ensures that the apparatus is protected during its launch. You wonder what the acceleration of the apparatus will be once it exits the launcher. Does the object's acceleration after it has left the launcher depend on its velocity when it leaves the launcher? You decide to model the situation by throwing balls straight down.

## EQUIPMENT

You will have a ball, a stopwatch, a meter stick, a video camera and a computer with a video analysis application written in LabVIEWTM (VideoRECORDER and VideoTOOL applications). The launcher is your hand.

## Prediction

Sketch a graph of a ball's acceleration as a function of time after it is launched in the manner described above. State how your graph will change if the object's initial velocity increases or decreases.

Do you think that the acceleration increases, decreases, or stays the same as the initial velocity of the object changes? $M$ ake your best guess and explain your reasoning.
$\square$
Read: FishbaneChapter 2, section 2.5.
The following questions will help you examine three possible scenarios. They should help you to understand your prediction and analyze your data.

1. How would you expect an acceleration vs. time graph to look for a ball moving downward with a constant acceleration? With a uniformly increasing acceleration? With a uniformly decreasing acceleration? Sketch the graph for each scenario and explain your reasoning. To make the comparison easier, draw these graphs next to each other. Write down the equation that best represents each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graph?
2. Write down the relationships between the acceleration and the velocity and the velocity and the position of the ball. Use these relationships to construct the graphs for velocity vs. time and position vs. time just below each acceleration graph from question 1. Use the same scale for each time axis. Write down the equation that best represents each graph. If there are constants in your equations, what kinematics quantities do they represent? How would you determine these constants from your graphs? Can any of the constants be determined from the equations representing the acceleration and velocity graphs?
3. Does your prediction agree with one of the scenarios you just explored? Explain why or why not.
4. Write down an outline of how you will determine the acceleration of the object from the video data.
5. Use the simulation "Lab2Sim" to approximate the conditions of your experiment. (See A ppendix $F$ for a brief explanation of how to use the simulations.) Do multiple runs of the simulations with various initial velocities and compare graphs. (The initial position of the ball should be well off the table, and the initial speed should be downward. N ote that the initial position and velocity parameters in Lab2Sim are specified as vectors of the form $<\mathrm{x}_{0}, \mathrm{y}_{0}, \mathrm{Z}_{0}>$ and $<\mathrm{v}_{\mathrm{x} 0}, \mathrm{v}_{\mathrm{y} 0}, \mathrm{v}_{\mathrm{z} 0}>$. The x -axis is along the Right/ Left direction, the y -axis is Up/ Down, and the z axis is Front/ Back.) If you believe air resistance may have affected your results, explore the effects of each with the simulation. If you believe that uncertainty in position measurements may have affected your results, use the simulation to compare the results with and without error. Compare the effect of error in the position vs. time graph with the velocity vs. time graph.

## EXPLORATION

Review your lab journal from Lab 1. Position the camera and adjust it for optimal performance. M ake sure everyone in your group gets the chance to operate the camera and the computer.

Practice throwing the ball straight downward until you can get the ball's motion to fill most of the video screen after it leaves your hand. Determine how much time it takes for the ball to fall and estimate the number of video points you will get in that time. Is it sufficient to make the measurement? Adjust the camera position to get enough data points.

Although the ball is the best item to use to calibrate the video, the image quality due to its motion might make this difficult. Instead, you might hold an object of known length in the plane of motion of the ball, near the center of the ball's trajectory, for calibration purposes. Where you place your reference object does make a difference in your results. Check your video image when you put the reference object close to the camera and then further away. What do you notice about the size of the reference object in the video image? The best place to put the reference object to determine the distance scale is at the position of the falling ball.

Step through the video and determine which part of the ball is easiest to consistently determine. When the ball moves rapidly you may see a blurred image due to the camera's finite shutter speed. If you cannot make the shutter speed faster, devise a plan to measure the position of the same part of the "blur" in each video frame.

Write down your measurement plan.

## Measurement

Makea video of the ball being tossed downwards. Repeat this procedurefor different initial velocities.
Digitize the position of the ball in enough frames of the video so that you have sufficient data to accomplish your analysis. Make sure you set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the ball travels and total time to determine the maximum and minimum valuefor each axis beforetaking data.

Graph your data as you go al ong (before making the next video), so you can determine how many different videos you need to make and how you should change the ball's initial velocity for each video. Don't waste time collecting data you don't need or, even worse, incorrect data. Collect enough data to convince yourself and others of your conclusion.

Repeat this procedurefor different launch velocities.

## Analysis

Choose a function to represent the position vs. time graph. How can you estimate the values of the constants of the function from the graph? You can waste a lot of time if you just try to guess the constants. What kinematic quantities do these constants represent?

Choose a function to represent the velocity vs. time graph. How can you calculate the values of the constants of this function from the function representing the position vs. time graph? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematic quantities do these constants represent? Determinethe launch velocity of the ball from this graph. Is this value reasonable?

If you cannot get one function to describe your velocity graph in a consistent way, you can try using one function for the first half of the motion and another for the last half. To do this you must go through the video analysis process twice and record your results each time. (How can you avoid repeating some work with the "SaveSession" and "Open Session" commands?)

From the velocity vs. time graph(s) determine the acceleration of the ball. Use the function representing the velocity vs. time graph to calculate the acceleration of the ball as a function of time. Is the average acceleration different for the beginning of the video (just after launch) and theend of the video?

Determine the acceleration of the ball just after launch and at the end of the video. How do they compare with the gravitational acceleration? Do you have enough data to convince others of your conclusions about your predictions?

Repeat the anal ysis for another launch velocity and compare the results.

## CONCLUSION

Did the data support your predicted relationship between acceleration and initial velocity? (Make sure you carefully review Appendix $C$ to determine if your data really supports this relationship.) If not, what assumptions did you make that were incorrect? Explain your reasoning.

What are the limitations on the accuracy of your measurements and analysis?
Will the survival of your apparatus depend on its launch velocity? State your results in the most general terms supported by your analysis.

## SIM ULATION

If your results did not completely match your expectations, use the simulation "Lab2Sim" again (See Appendix F for a brief explanation of how to use the simulations) to explore what might have happened

## PROBLEM \#3: <br> PROJECTILE MOTION AND VELOCITY

A toy company has hired you to produce an instructional videotape for would-bejugglers. To plan the videotape, you decide to separately determine how the horizontal and vertical components of a ball's velocity change as it flies through the air. To catch the ball, a juggler must be able to predict its position, so you decide to calculate functions to represent the horizontal and vertical positions of a ball after it is tossed. To check your analysis, you decide to analyze a video of a ball thrown in a manner appropriate to juggling.

## EQUIPMENT

For this problem, you will have a ball, a stopwatch, a meter stick, a video camera and a computer with a video analysis application written in LabVIEW ${ }^{\text {TM }}$ (VideoRECORDER and VideoTOOL).

## Prediction

## Note: for this problem, you should complete the W arm U p Q uestions to help formulate a prediction.

1. Write down equations to describe the horizontal and vertical velocity components of the ball as a function of time. Sketch a graph to represent each equation.

D o you think the horizontal component of the object's velocity changes during its flight? If so, how does it change? Or do you think it is constant (does not change)? M ake your best guess and explain your reasoning. W hat about the vertical component of its velocity?
2. Write down the equations that describe the horizontal and vertical position of the ball as a function of time. Sketch a graph to represent each equation.

## Warm Up

Read: FishbaneChapter 3. Sections 3.1-3.4.
The following questions will help you calculate the details of your prediction and analyze your data.

1. Make a large (about onehalf page) sketch of the trajectory of the ball on a coordinate system. Label thehorizontal and vertical axes of your coordinate system.
2. On your sketch, draw acceleration vectors for the ball (show directions and relative magnitudes) at five different positions: two when the ball is going up, two when it is going down, and one at its maximum height. Explain your reasoning. Decompose each acceleration vector into its vertical and horizontal components.
3. On your sketch, draw velocity vectors for the ball at the same positions as your acceleration vectors (use a different color). Decompose each velocity vector into vertical and horizontal components. Check that the change of the velocity vector is consistent with the acceleration vector. Explain your reasoning.
4. On your sketch, how does the horizontal acceleration change with time? How does it compare to the gravitational acceleration? Write an equation giving the ball's horizontal acceleration as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
5. On your sketch, how does the ball's horizontal velocity change with time? Is this consistent with your statements about the ball's acceleration from the previous question? Write an equation for the ball's horizontal velocity as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
6. Based on the equation of the ball's horizontal velocity, write an equation for the ball's horizontal position as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
7. On your sketch, how does the ball's vertical acceleration change with time? How does it compare to the gravitational acceleration? Write an equation giving the ball's vertical acceleration as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
8. On your sketch, how does the ball's vertical velocity change with time? Is this consistent with your statements about the ball's acceleration questioning the previous question? Write an equation for the ball's vertical velocity as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
9. Based on the equation describing the ball's vertical velocity, write an equation for the ball's vertical position as a function of time. Graph this equation. If there are constants in your equation, what kinematic quantities do they represent? How would you determine these constants from your graph?
10. Use the simulation "Lab2Sim" to simulate the projectilemotion in this problem. N ote that in this case the initial vel ocity should have non-zero horizontal and vertical components.

## EXPLORATION

Review your lab journal from the problems in Lab 1.

Position the camera and adjust it for optimal performance. $M$ ake sure everyone in your group gets the chance to operate the camera and the computer.

Practice throwing the ball until you can get the ball's motion after it leaves your hand to reliably fill the video screen. Determine how much time it takes for the ball to travel and estimate the number of video
points you will get in that time. Do you have enough points to make the measurement? Adjust the camera position to get enough data points.

Although the ball is the best item to use to calibrate the video, the image quality due to its motion might make this difficult. Instead, you might need to place an object of known length on the plane of motion of the ball, near the center of the ball's trajectory, for calibration purposes. Where you place your reference object does make a difference in your results. Check your video image when you put the reference object close to the camera and then further away. What do you notice about the size of the reference object? Determine the best place to put the reference object for calibration.

Step through the video and determine which part of the ball is easiest to consistently determine. When the ball moves rapidly you may see a blurred image due to the camera's finite shutter speed. If you cannot make the shutter speed faster, devise a plan to measure the position of the same part of the "blur" in each video frame.

Write down your measurement plan.

## Measurement

Makea video of the ball being tossed. Make sure you have enough useful frames for your analysis.
Digitize the position of the ball in enough frames of the video so that you have the sufficient data to accomplish your analysis. Make sure you set the scalefor the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the ball travels and total time to determine the maximum and minimum value for each axis before taking data.


Choose a function to represent the horizontal position vs. time graph and another for the vertical position vs. time graph. How can you estimate the values of the constants of the functions from the graph? You can waste a lot of time if you just try to guess the constants. What kinematic quantities do these constants represent?

Choose a function to represent the velocity vs. time graph for each component of the velocity. How can you calculate the values of the constants of these functions from the functions representing the position vs. time graphs? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematic quantities do these constants represent? Determine the launch velocity of the ball from this graph. Is this value reasonable? Determine the velocity of the ball at its highest point. Is this value reasonable?

From the velocity vs. time graphs determine the acceleration of the ball independently for each component of the motion. Use the functions representing the vel ocity vs. time graph for each component to cal culate each component of the ball's acceleration as a function of time. Is the acceleration constant from just after launch to just before the ball is caught? What is its direction? Determine the magnitude of the ball's acceleration at its highest point. Is this value reasonable?

## CONCLUSION

Did your measurements agree with your initial predictions? Why or why not? Did your measurements agree with those taken by other groups? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

How do the horizontal components of a juggled ball's velocity and position depend on time? How do the vertical components of a juggled ball's velocity and position depend on time? State your results in the most general terms supported by your analysis. At what position does the ball have the minimum velocity? Maximum velocity?

If your results did not completely match your expectations, you shoud go back and use the simulation "Lab2Sim" again.

## PROBLEM \#4:

## BOUNCING

You work for NASA designing a low-cost landing system for a Mars mission. The payload will be surrounded by padding and dropped onto the surface. When it reaches the surface, it will bounce. The height and the distance of the bounces will get smaller with each bounce so that it finally comes to rest on the surface. Your boss asks you to determine how the ratio of the horizontal distance covered by two successive bounces depends on the ratio of the heights of the two bounces and the ratio of the horizontal components of the initial velocity of the two bounces. After making the calculation you decide to check it in your laboratory on Earth.

## EQUIPMENT

You will have a ball, a stopwatch, a meter stick, and a computer with a video camera and an analysis application written in LabVIEWTM (VideoRECORDER and VideoTOOL applications.)

## Prediction

Note: for this problem, you should complete the Warm up questions to help formulate a prediction.
Calculate the ratio asked for by your boss. (Assume that you know the ratio of the heights of the two bounces and the ratio of the horizontal components of the initial velocity for the two bounces.)

Be sure to state your assumptions so your boss can decide if they are reasonable for the M ars mission.

## Warm Up

Read: Fishbane Chapter 3. Sections 3.1-3.4.
Thefollowing questions will help you make the prediction.

1. Draw a sketch of the situation, including velocity and acceleration vectors at all relevant times. Decide on a coordinate system. Define the positive and negative directions. During what time interval does the ball have motion that is easiest to calculate? Is the acceleration of the ball during that time interval constant or is it changing? Why? Are the time durations of two successive bounces equal? Why or why not? Label the horizontal distances and the maximum heights for each of the first two bounces. What reasonable assumptions will you probably need to make to solve this problem? How will you check these assumptions with your data?
2. Write down the basic kinematics equations that apply to the time intervals you selected, under the assumptions you have made. Clearly distinguish the equations describing horizontal motion from those describing vertical motion.
3. Write an equation for the horizontal distance the ball travels in the air during the first bounce, in terms of the initial horizontal velocity of the ball, its horizontal acceleration, and the time it stays in the air before reaching the ground again.
4. The equation you just wrote contains the time of flight, which must be rewritten in terms of other quantities. Determine it from the vertical motion of the ball. First, select an equation that gives the ball's vertical position during a bounce as a function of its initial vertical velocity, its vertical acceleration, and the time elapsed since it last touched the ground.
5. The equation in the previous step involves two unknowns, which can both be related to the time of flight. How is the ball's vertical position when it touches the ground at the end of its first bounce related to its vertical position when it touched the ground at the beginning of its first bounce? Use this relationship and the equation from step 4 to write one equation involving the time of flight. How is the time of flight related to the time it takes for the ball to reach its maximum height for the bounce? Use this relationship and the equation from step 4 to write another equation involving the time of flight. Solve these two equations to get an equation expressing the time of flight as a function of the height of the bounce and the vertical acceleration.
6. Combine the previous steps to get an equation for the horizontal distance of a bounce in terms of the ball's horizontal velocity, the height of the bounce, and the ball's vertical acceleration.
7. Repeat the above process for the next bounce; take the ratio of horizontal distances to get your prediction equation.
8. Use the simulation "Lab2Sim" to simulate the lab as best as possible. You will need to trial different initial conditions and possibly use more frames than generally used.

## EXPLORATION

Review your lab journal from any previous problem requiring analyzing a video of a falling ball.
Position the camera and adjust it for optimal performance. M ake sure everyone in your group gets the chance to operate the camera and the computer.

Practice bouncing the ball without spin until you can get at least two full bounces to fill the video screen. Three is better so you can check your results. It will take practice and skill to get a good set of bounces. Everyone in the group should try to determi newho is best at throwing the ball.

Determine how much time it takes for the ball to have the number of bounces you will video and estimate the number of video points you will get in that time. Is that enough points to make the measurement? Adjust the camera position to get enough data points.

Although the ball is the best item to use to calibrate the video, the image quality due to its motion might make this difficult. Instead, you might need to place an object of known length in the plane of motion of the ball, near the center of the ball's trajectory, for calibration purposes. Where you place your reference object does make a difference to your results. Determine the best place to put the reference object for calibration.

Step through the video and determine which part of the ball is easiest to consistently determine. When the ball moves rapidly you may see a blurred image due to the camera's finite shutter speed. If you cannot make the shutter speed faster, devise a plan to measure the position of the same part of the "blur" in each video frame.

Write down your measurement plan.

## MeAsurement

Make a video of the ball being tossed. Make sure you have enough frames to complete a useful analysis.
Digitize the position of the ball in enough frames of the video so that you have the sufficient data to accomplish your analysis. Makesure you set the scalefor the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the ball travels and total time to determine the maximum and minimum value for each axis before taking data.


Analyze the video to get the horizontal distance of two successive bounces, the height of the two bounces, and the horizontal components of the ball's velocity for each bounce. You may wish to calibrate the video independently for each bounce so you can begin your time as close as possible to when the ball leaves the ground. (Alternatively, you may wish to avoid repeating some work with the "Save Session" and "Open Session" commands.) The point where the bounce occurs will usually not correspond to a video frame taken by the camera so some estimation will be necessary to determine this position. (Can you use the "SaveDataTable" command to help with this estimation?)

Choose a function to represent the horizontal position vs. time graph and another for the vertical position graph for the first bounce. How can you estimate the values of the constants of the functions? You can waste a lot of time if you just try to guess the constants. What kinematic quantities do these constants represent? How can you tell where the bounce occurred from each graph? Determine the height and horizontal distance for the first bounce.

Choose a function to represent the velocity vs. time graph for each component of the velocity for the first bounce. How can you calculate the values of the constants of these functions from the functions representing the position vs. time graphs? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematic quantities do these constants represent? How can you tell where the bounce occurred from each graph? Determine the initial horizontal velocity of the ball for the first bounce. What is the horizontal and vertical acceleration of the ball between bounces? Does this agree with your expectations?

Repeat this analysis for the second bounce, and the third bounce if possible.
What kinematics quantities are approximately the same for each bounce? How does that simplify your prediction equation?

## Conclusion

How do your graphs compare to your predictions and warm up questions? What are the limitations on the accuracy of your measurements and analysis?

Will the ratio you calculated be the same on M ars as on Earth? Why?
What additional kinematic quantity, whose value you know, can be determined with the data you have taken to give you some indication of the precision of your measurement? How close is this quantity to its known value?

## SIM ULATION

If your results did not completely match your expectations, you should again use the simulation
"Lab2Sim" See A ppendix F for a brief explanation of how to use the simulations, and see Problem 2 in this laboratory for suggestions of how you could use the simulation here.

## PROBLEM \#5: <br> ACCELERATION AND CIRCULAR MOTION

You have been appointed to a Citizen Committee investigating the safety of a proposed new ride called "The Spinner" at the M all of A merica's Camp Snoopy. The ride consists of seats mounted on each end of a steel beam. For most of the ride, the beam rotates about its center in a horizontal circle at a constant speed. Several Committee members insist that a person moving in a circle at constant speed is not accelerating, so there is no need to be concerned about the ride's safety. You disagree and sketch a diagram showing that each component of the velocity of a person on the ride changes as a function of time even though the speed is constant. Then you calculate the magnitude of a person's acceleration. The committee is still skeptical, so you build a model to show that your calculations are correct.

## EQUIPMENT

You will be using an apparatus that spins a horizontal beam on Aframe base A top view of the device is shown to the right. You will have a stopwatch, a meter stick and the video analysis equipment.


## Prediction

Cal culate the time dependence of the velocity components of an object moving like the ride's seats. Use this to cal culate the object's acceleration.

## Warm Up

Read: FishbaneChapter 3, section 3.5.
Thefollowing questions will help with your prediction and data analysis.

1. Draw the trajectory of an object moving in a horizontal circle with a constant speed. Choose a convenient origin and coordinate axes. Draw the vector that represents the position of the object at some time when it is not along an axis.
2. Write an equation for one component of the position vector as a function of the radius of the circle and the angle the vector makes with one axis of your coordinate system. Calculate how that angle depends on time and the constant angular speed of the object moving in a
circle (Hint: integrate both sides of equation 3-46 with respect to time). You now have an equation that gives a component of the position as a function of time. Repeat for the component perpendicular to the first component. Make a graph of each equation. If there are constants in the equations, what do they represent? How would you determine the constants from your graph?
3. From your equations for the components of the position of the object and the definition of velocity, use calculus to write an equation for each component of the object's velocity. Graph each equation. If there are constants in your equations, what do they represent? How would you determine these constants? Compare these graphs to those for the components of the object's position.
4. From your equations for the components of the object's velocity, calculate its speed. Does the speed change with time or is it constant?
5. From your equations for the components of the object's velocity and the definition of acceleration, use calculus to write down the equation for each component of the object's acceleration. Graph each equation. If there are constants in your equations, what do they represent? How would you determine these constants from your graphs? Compare these graphs to those for the components of the object's position.
6. From your equations for the components of the acceleration of the object, calculate the magnitude of the object's acceleration. Is it a function of time or is it constant?

## EXPLORATION

Practice spinning the beam at different speeds. How many rotations does the beam make before it slows down appreciably? Use the stopwatch to determine which spin gives the closest approximation to constant speed. At that speed, how many video frames will you get for one rotation? Will this be enough to determine the characteristics of the motion?

Check to see if the spinning beam is level.
Move the apparatus to the floor and adjust the camera tripod so that the camera is directly above the middle of the spinning beam. Practice taking some videos. How will you make sure that you always click on the same position on the beam?

Decide how to calibrate your video.

## Measurement

Acquire the position of a fixed point on the beam in enough frames of the video so that you have sufficient data to accomplish your analysis -- at least two complete rotations. Set the scale for the axes of your graph so that you can see the data points as you take them. Use your measurements of total distance the object travels and total time to determine the maximum and minimum value for each axis before taking data.

## Analysis

Analyze your video by digitizing a single point on the beam for at least two complete revolutions.
Choose a function to represent the graph of horizontal position vs. time and another for the graph of vertical position vs. time. How can you estimate the values of the constants in the functions? You can waste a lot of time if you just try to guess the constants. What kinematic quantities do these constants represent? Which are the same for both components? How can you tell from the graph when a completerotation occurred?

Choose a function to represent the velocity vs. time graph for each component of the velocity. How can you calculate the values of the constants of these functions from the functions representing the position vs. time graphs? Check how well this works. You can also estimate the values of the constants from the graph. Just trying to guess the constants can waste a lot of your time. What kinematic quantities do these constants represent? Which are the same for both components? How can you tell when a completerotation occurred from each graph?

Use the equations for the velocity components to cal culate the speed of the object. Is the speed constant? How does it compare with your measurements using a stopwatch and meter stick?

Use the equations for the velocity components to cal culate the equations that represent the components of the acceleration of the object. Use these components to calculate the magnitude of the total acceleration of the object as a function of time. Is the magnitude of the acceleration a constant? What is the relationship between the acceleration and the speed?

## Conclusion

How do your graphs compare to your predictions and warm up questions? What are thelimitations on theaccuracy of your measurements and analysis?

Is it true that the velocity of the object changes with time while the speed remains constant?
Is the instantaneous speed of the object that you calculate from your measurements the same as its average speed that you measure with a stopwatch and meter stick?

Have you shown that an object moving in a circle with a constant speed is always accelerating? Explain.

Compare the magnitude of the acceleration of the object that you calculate from your measurements to the "centripetal acceleration" that you can calculate from the speed and the radius of the object.

## PROBLEM \#6: <br> A VECTOR APPROACH TO CIRCULAR MOTION

You have a job supervising the construction of a highway. Safety requires that you know what the direction of a car's acceleration is when it moves at constant speed along curves. To check your prediction you decide to model, in the lab, curves that are arcs of circles.


You will beusing a apparatus that spins a horizontal beam on a Aframe base A top view of the device is shown to the right. You will have a stopwatch, a meter stick and the video analysis equipment.


## Prediction

What is the direction of the acceleration vector for an object moving at a constant speed along a circle's arc? Explain your reasoning.

## Warm Up

## Read: FishbaneChapter 3, section 3.5.

The following questions will help you to make your prediction and analyze your data. These questions assume that you have completed the predictions and warm up questions for Problem 5. If you have not, you should do so before continuing.

1. Make a large (half-page) perpendicular coordinate system. Choose and label your axes. Draw the trajectory of the object moving along a circular road on this coordinate system. Show the positions of your object at equal time intervals around the circle. Choose several points along the trajectory (at least one per quadrant of the circle) and draw the position vector to each of these points. Write down the equations that describe the components of the object's position at each point.
2. From your position equations, calculate the components of the object's velocity at each point. Choose a scale that allows you to draw these components at each point. Add these components (as vectors) to draw the velocity vector at each point. What is the relationship between the velocity vector direction and the direction of the radial vector from the center of the circle?
3. From your velocity equations, calculate the components of the object's acceleration at each point. Choose a scale that allows you to draw these components at each point. Add these components (as vectors) to draw the acceleration vector at each point. What is the relationship between the acceleration vector direction and the radius of the circle?

## EXPLORATION

If you have already done Problem 5, you can use that video and move on to the analysis. If not, do the exploration for that Problem.

## Measurement

If you have already done Problem 5, you can use those measurements and move on to the analysis. If not, do the measurement for that Problem.

## Analysis

Analyze your video to get equations that describe the motion of a point going in a circle at constant speed. You can use the equations for position and velocity components you found for Problem 5.

Use the procedure outlined in the Warm Up Questions to analyze your data to get the direction of the acceleration of the object in each quadrant of the circle.

## Conclusion

How does the direction of the acceleration compare to your prediction? What are the limitations of your measurements and analysis?

What is the direction of the acceleration for a car moving with a constant speed along a curve that forms an arc of a circle? State your result in the most general terms supported by your analysis.

## PROBLEM \#7: ACCELERATION AND ORBITS

You work with a research group investigating the possibility of extraterrestrial life. Your team is looking at the properties of newly discovered planets orbiting other stars. You have been assigned the task of determining the gravitational force between planets and stars. As a first step, you decide to calculate a planet's acceleration as a function of its orbital radius and period. You assume that it moves in a circle at a constant speed around the star. From previous measurements, you know the radius and period of the orbit.


You will be using a apparatus that spins a horizontal beam on a Aframe base A top view of the device is shown to the right. You will have a stopwatch, a meter stick and the video analysis equipment.


Calculate the acceleration of an object moving as the planet that you are investigating. Make two graphs with one showing acceleration as a function of radius (for a fixed period) and another showing acceleration as a function of period (for a fixed radius.)

## Warm Up

Read: Fishbane Chapter 3, section 3.5.
The following questions should help with the prediction. In addition, do the Warm up questions for Problem 5 if you have not al ready done them.

1. Draw the trajectory of an object moving in a circle when its speed is not changing. Draw vectors describing the kinematic quantities of the object. Label the radius of the circle and the relevant kinematic quantities. Choose and label your coordinate axes.
2. Write down the kinematic equations that describe this type of motion. Your equations should include the definition of speed when the speed is constant and the relationship between acceleration and speed for uniform circular motion. You are now ready to plan your mathematical solution.
3. Select an equation identified in step 2 , which gives the acceleration in terms of quantities you "know" and additional unknowns. In this problem, you know the radius and the period of the object's motion.
4. If you have additional unknowns, determine one of them by selecting a new equation, identified in step 2, relating that unknown to other quantities. Repeat this step until you haveno additional unknowns.

## Exploration

If you have already done Problem 5, you can use that video for some of your data. If not, do the exploration given in that Problem.

Decide how you can measure objects at several different positions on the beam while holding the period of rotation constant. How many videos do you need to takefor this measurement? Decide how you can measure objects at the same position on the beam for different periods of rotation. H ow many videos do you need to take for this measurement?

## MeAsurement

Use your plan from the Exploration section to make your measurements.
If you have already done Problem 5, you can use that for one of your measurements. If not, do the measurement as given in that Problem. In addition, make several measurements at different radii and different periods in arange that will give your predictions the most stringent test.


Use your technique from Problem 5 to analyze your video for the magnitude of the acceleration that describes the motion of a point going in a circle at constant speed. You can also determine the radius of the object and its period from this data. Make a graph of acceleration as a function of radius for objects with the same period. Make a graph of acceleration as a function of period for objects with the same radius.

## Conclusion

Are your measurements consistent with your predictions? Why or why not? What are the limitations of your measurements and analysis?

1. A baseball is hit horizontally with an initial velocity $v_{0}$ at time $t=0$ and follows the parabolic arc shown at right.
a. Which graph below best represents the horizontal position (x) vs. timegraph? Explain
 your reasoning.
b. Which graph below best represents the horizontal velocity $\left(v_{x}\right)$ vs. time graph? Explain your reasoning.
c. Which graph below best represents the horizontal acceleration ( $\mathrm{a}_{\mathrm{x}}$ ) vs. time graph? Explain your reasoning.
d. Which graph below best represents the vertical position (y) vs. time graph? Explain your reasoning.
e. Which graph below best represents the vertical velocity $\left(v_{y}\right)$ vs. time graph? Explain your reasoning.
f. Which graph below best represents the vertical acceleration (ay) vs. time graph? Explain your reasoning.

(a)

(d)


(b)


(e) $t$

(f)

(h)

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

2. Suppose you throw a ball vertically up into the air with an initial velocity $\mathrm{v}_{\mathrm{o}}$.
a. What is the acceleration of the ball at its maximum height? Explain your reasoning.
b. How would the acceleration vs. time graph look from the moment the ball leaves your hand to the moment before it returns to your hand?
3. Two beads are fixed to a rod rotating at constant speed about a pivot at its left end, as shown in the drawing at right.
a. Which bead has the greater speed? Explain your reasoning.

b. Which bead has the greater acceleration? Explain your reasoning.
4. Two racing boats go around a semicircular turn in a racecourse. The boats have the same speed, but boat A is on the inside while boat B is on the outside, as shown in the drawing.
a. Which boat gets around the turn in the smaller time? Explain your reasoning.
b. Which boat undergoes the greater change in velocity while in the turn? Explain your reasoning.

c. Based on the definition of acceleration, which boat has the greater acceleration while in the turn? Explain your reasoning.
d. Based on the equation for centripetal acceleration, which boat has the greater acceleration while in the turn? Compare your answer to part c. Explain your reasoning.
$\qquad$

## PHYSICS 1301LABORATORY REPORT <br> Laboratory II

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readable; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATA AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL (incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total points <br> achieved) |  |
| BONUS POINTS FOR TEAMWORK <br> (as specified by course policy) |  |

* An " R " in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORY III FORCES

The problems in this laboratory will help you further investigate objects' motions. Specifically, you will investigate the effects of the forces associated with different interactions between objects. In the first problem, you will investigate the effect of forces on a sliding object. To solve the second problem you will apply the force concept and the vector nature of forces to a situation in which nothing moves. The last three problems lead you to investigate some effects of frictional forces.

## Objectives:

After successfully completing this laboratory, you should be ableto:

- Make and test quantitative predictions about the relationship of forces on objects and the motion of those objects for real systems.
- Useforces as vector quantities.
- Characterizethe behavior of the friction force.
- Improveyour problem solving skills.


## Preparation:

Read Paul M. Fishbane: Chapter 4 and Chapter 5. Review the motion of a cart moving down a ramp.
Before coming to lab you should be able to:

- Define and use sine, cosine and tangent for a right triangle.
- Describe the difference between mass and weight.
- Determine the net force on an object from its acceleration.
- Draw and useforce diagrams.
- Resolve force into components vectors. Determine a force's magnitude and direction from its components.
- Explain what it means to say a system is in "equilibrium."
- Write the forcelaw for a frictional force.


## PROBLEM \#1: <br> FORCE AND MOTION

You are a volunteer in the city's children's summer program. In one activity the children build and race model cars along a level surface. To give each car a fair start, another volunteer builds a special launcher with a string attached to the car at one end. The string passes over a pulley and from its other end hangs a block. The car starts from rest when the block is allowed to fall. After the block hits the ground, the string no longer exerts a force on the car and it continues along the track. You decide to calculate how the launch velocity of the car depends on the mass of the car, the mass of the block, and the distance the block falls. You hope to use the calculation to impress other volunteers by predicting the winner of each race.

## EQUIPMENT

Released from rest, a cart is pulled along a level track by a hanging object as shown below:


You can vary the mass of Object A and the Cart. They are connected by a light string. Object A falls from a height shorter than the track's length. You will have a meter stick, a stopwatch, a mass hanger, a mass set, cart masses, a pulley, a pulley clamp, a piece of string and the video analysis equipment.

## Prediction

Calculate the cart's velocity after object A has hit thefloor. Express it as an equation, in terms of quantities mentioned in the problem, and draw graphs to show how the velocity changes with each variable.

## Warm UP

Read: Fishbane Chapter 4. Read carefully Sections 4-5 and 4-6 and Examples 4-9 and 4-12.

To figure out your prediction, it is useful to have an organized problem-solving strategy such as the one outlined in the following questions. You might also find the Problem Solving techniques in the Competent Problem Solver useful.

1. Make three sketches of the problem situation, one for each of three instants: when the cart starts from rest, just beforeobject A hits the floor, and just after object A hits the floor. Draw vectors to show the directions and relative magnitudes of the two objects' velocities and accelerations at each instant. Draw vectors to show all of the forces on object A and the cart at each instant. Assign appropriate symbols to all of the quantities describing the motion and the forces. If two quantities have the same magnitude, use the same symbol but write down your justification for doing so. (For example, the cart and object A have the same magnitude of velocity when the cart is pulled by the string. Explain why.) Decide on your coordinatesystem and draw it.
2. The "known" quantities in this problem are the mass of object A, the mass of the cart, and the height above the floor where object $A$ is released. Assign a symbol to each known quantity. Identify all the unknown quantities. What is the relationship between what you really want to know (the velocity of the cart after object A hits the floor) and what you can calculate (the velocity of the cart just before object A hits the floor)?
3. Identify and write the physics principles you will use to solve the problem. (Hint: forces determine the objects' accelerations, so N ewton's 2nd Law may be useful. You need to relate the magnitudes of forces on different objects to one another, so Newton's 3rd Law is probably also useful. Will you need any kinematics principles?) Write down any assumptions you have made which are necessary to solve the problem and justified by the physical situation. (For example, why will it be reasonable to ignore frictional forces in this situation?)
4. Draw one free-body diagram for object $A$, and a separate one for the cart after they start accelerating. Check to se if any of these forces are related by Newton's 3rd Law (Third Law Pairs). Draw the acceleration vector for the object next to its free-body diagram. Next, draw two separate coordinate systems; place vectors to represent each force acting on the cart on one coordinate system, and those acting on Object A on the second one (force diagrams). (The origin (tail) of each vector should be the origin of the coordinate system.) For each force diagram, write down Newton's 2nd law along each axis of the coordinate system. Make sure all of your signs are correct in the Newton's 2nd law equations. (For example, if the acceleration of the cart is in the + direction, is the acceleration of object A + or -? Your answer will depend on how you define your coordinate system.)
5. You are interested in thefinal velocity of the cart, but Newton's 2nd Law only gives you its acceleration; write down any kinematics equations which are appropriate to this situation. Is the acceleration of each object constant, or does it vary while object A falls?
6. Write down an equation, from those you have collected in steps 4 and 5 above, which relates what you want to know (the velocity of the cart just before object A hits the ground) to a quantity you either know or can find out (the acceleration of the cart and the time from the start until just before object A hits the floor). Now you have two new unknowns (acceleration and time). Choose one of these unknowns (for example, time) and write down a new equation (again from those collected in steps 4 and 5) which relates it to another quantity you either know or can find out (distance object A falls). If you have generated no additional unknowns, go back to determine the other original unknown (acceleration). Write down a new equation that relates the acceleration of the cart to other quantities you
either know or can find (forces on the cart). Continue this process until you generate no new unknowns. At that time you should have as many equations as unknowns.
7. Solve your mathematics to give the prediction.

Make a graph of the cart's velocity after object A has hit the floor as a function of the mass of object A, keeping constant the cart mass and the height through which object A falls.
Make a graph of the cart's velocity after object A has hit the floor as a function of the mass of the cart, keeping constant the mass of object A and the height through which object A falls.

Make a graph of the cart's velocity after object A has hit the floor as a function of the distance object A falls, keeping constant the cart mass and the mass of object A.
8. Does the shape of each graph make sense to you? Explain your reasoning.
9. Use the simulation "Lab4Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the effects of a very wide range of masses for the hanging object and the cart. If you believe friction may have affected your results, explore its effects with the simulation. Explore the effects of changing the mass of the string and the pulley. Do multiple runs and check the graphs produced. Use the simulation to compare the results with and without error. Look for theeffects in the position vs. time graph or in the velocity vs. time graph.

## EXPLORATION

Adjust the length of the string such that object A hits the floor well before the cart runs out of track. You will be analyzing a video of the cart after object A has hit the floor. Adjust the string length to give you a video that is long enough to allow you to analyze several frames of motion.

Choose a mass for the cart and find a useful range of masses for object A that allows the cart to achieve a reliably measurable velocity before object A hits the floor. Practice catching the cart before it hits the end stop on the track. Make sure that the assumptions for your prediction are good for the situation in which you are making the measurement. Use your prediction to determine if your choice of masses will allow you to measure the effect that you are looking for. If not, choose different masses.

Choose a mass for object A and find a useful range of masses for the cart.
Now choose a mass for object A and one for the cart and find a useful range of falling distances for object A.

Write down your measurement plan. (Hint: What do you need to measure with video analysis? Do you need video of the cart? Do you need video of object A ?)

## Measurement

Carry out the measurement plan you determined in the Exploration section.
Complete the entire analysis of one case before making videos and measurements of the next case. A different person should operate the computer for each case.

Make sure you measure and record the masses of the cart and object A (with uncertainties). Record the height through which object A falls and the time it takes to fall (measured with the stopwatch).


Ensure a different person in your group operates the computer for each case you are analyzing.
Determine the cart's velocity just after object A hits the floor from your video.
From the time and distance object A fell in each trial, calculate the cart's velocity just after object A hits the floor (assuming constant acceleration). Compare this value to the velocity you measured from the video. A re they consistent with each other?

What are the limitations on the accuracy of your measurements and analysis?

## Conclusion

How does the velocity from your prediction equation compare with the two measured velocities (measured with video analysis, and also with stopwatch / meter stick measurements) compare in each case? Did your measurements agree with your initial prediction? If not, why?

Does the launch velocity of the car depend on its mass? The mass of the block? The distance the block falls?

If the same mass block falls through the same distance, but you change the mass of the cart, does the force the string exerts on the cart change? Is the force of the string on object A always equal to the weight of object A? Is it ever equal to the weight of object A? Explain your reasoning.

## PROBLEM \#2: <br> FORCES IN EQUILIBRIUM

You have a summer job with a research group studying the ecology of a rain forest in South America. To avoid walking on the delicate rain forest floor, the team members walk along a rope walkway that the local inhabitants have strung from tree to tree through the forest canopy. Your supervisor is concerned about the maximum amount of equipment each team member should carry to safely walk from tree to tree. If the walkway sags too much, the team member could be in danger, not to mention possible damage to the rain forest floor. You are assigned to set the load standards.

Each end of the rope supporting the walkway goes over a branch and then is attached to a large weight hanging down. You need to determine how the sag of the walkway is related to the mass of a team member plus equipment when they are at the center of the walkway between two trees. To check your calculation, you decide to model the situation using the equipment shown below.

## EQUIPMENT

The system consists of a central object B (mass M), suspended halfway between two pulleys by a string. The whole system is in equilibrium. The picture below is similar to the situation with which you will work. The objects A and C, which have the same mass ( $m$ ), allow you to determine the force exerted on the central object by the string. You need to make some assumptions about what you can neglect. For this investigation, you will need a meter stick, two pulleys and two pulley clamps, three mass hangers and a mass set to vary the mass of object $B$.


## Prediction

Write an equation for the vertical displacement of the central object $B$ in terms of the horizontal distance between the two pulleys ( L ), the mass of object $B(M)$, and the mass $(\mathrm{m})$ of objects $A$ and $C$.


Read: Fishbane Chapter 4. Read carefully Section 4-6 and Example 4-12.

To solve this problem it is useful to have an organized problem-solving strategy such as the one outlined in the following questions. You should use a technique similar to that used in Problem 1 (where a more detailed set of Warm up questions is provided) to solve this problem.

1. Draw a sketch similar to the one in the Equipment section. Draw vectors that represent the forces on objects A, B, C, and point P. Use trigonometry to show how the vertical displacement of object $B$ is related to the horizontal distance between the two pulleys and the angle that the string between the two pulleys sags below the horizontal.
2. The "known" (measurable) quantities in this problem are $L, m$ and $M$; the unknown quantity is the vertical displacement of object $B$.
3. Write down the acceleration for each object. Draw separate force diagrams for objects $A, B$, $C$ and for point P (if you need help, see your text). Use Newton's third law to identify pairs of forces with equal magnitude. What assumptions are you making?
Which angles between your force vectors and your horizontal coordinate axis are the same as the angle between the strings and the horizontal?
4. For each force diagram, write $N$ ewton's second law along each coordinate axis.
5. Solve your equations to predict how the vertical displacement of object $B$ depends on its mass ( $M$ ), the mass ( $m$ ) of objects A and $C$, and the horizontal distance between the two pulleys (L). Use this resulting equation to make a graph of how the vertical displacement changes as a function of the mass of object $B$.
6. From your resulting equation, analyze what is the limit of mass (M) of object B corresponding to the fixed mass ( m ) of object A and C . What will happen if $\mathrm{M}>2 \mathrm{~m}$ ?

## Exploration

Start with just the string suspended between the pulleys (no central object), so that the string looks horizontal. Attach a central object and observe how the string sags. Decide on the origin from which you will measure the vertical position of the object.

Try changing the mass of objects A and C (keep them equal for the measurements but you will want to explore the case where they are not equal).

Do the pulleys behave in a frictionless way for the entire range of weights you will use? How can you determine if the assumption of frictionless pulleys is a good one? Add mass to the central object to decide what increments of mass will give a good range of values for the measurement. Decide how measurements you will need to make.

## Measurement

Measure the vertical position of the central object as you increase its mass. Make a table and record your measurements with uncertainties.


Graph the measured vertical displacement of the central object as a function of its mass. On the same graph, plot the predicted vertical displacement.

Where do the two curves match? Are there places where the two curves start to diverge from one another? What does this tell you about the system?

What are the limitations on the accuracy of your measurements and analysis?

## Conclusion

What will you report to your supervisor? How does the vertical displacement of an object suspended on a string between two pulleys depend on the mass of that object? Did your measurements of the vertical displacement of object B agree with your predictions? If not, why? State your result in the most general terms supported by your analysis.

What information would you need to apply your calculation to the walkway through the rain forest?
Estimate reasonable values for the information you need, and solve the problem for the walkway over the rain forest.

## PROBLEM \#3: FRICTIONAL FORCE

You have joined a team trying to win the next solar powered car race and have been asked to investigate the effect of friction on the strategy of the race. In any race, sometimes the car coasts and sometimes it speeds up. One of your team has suggested that the frictional force is larger when a force causes an object to speed up than when it coasts and slows down "naturally" because of friction. Do you agree? You suggest making a laboratory model to measure the frictional force when it is speeding up and when it is coasting. You can't measure force directly; to make the model useful you must calculate how measurable quantities will be affected by the friction force. Your model consists of a cart pulled along a level track by a light string. The string passes over a pulley and is tied to some weights hanging down. After the weights hit the ground, the cart continues to coast along the track. A pad between the cart and the track provides a variable friction force.

## EQUIPMENT

A cart is pulled along a level track by a hanging object as shown below:


You can change the mass of Object A and the Cart. You will use the friction cart (with pad). You will have a meter stick, a mass hanger, a stopwatch, a mass set, a pulley clamp, cart masses, a string, and video analysis equipment.

## Prediction

Express the frictional force on the cart in terms of quantities that you can measure in the experiment. Make an educated guess about the relationship between the frictional forces in the two situations.


Read: Fishbane Chapter 5. Read carefully Section 5-1 and Examples 5-3 and 5-6.

It is useful to have an organized problem-solving strategy such as the one outlined in the following questions. You should use a technique similar to that used in Problem 1 (where a more detailed set of Warm up questions aregiven) to solve this problem.

1. Make a drawing of the problem situation while the cart's speed is increasing, and another one while the cart's speed is decreasing. Draw vectors for each drawing to represent all quantities that describe the motions of the block and the cart and the forces acting on them. Assign appropriate symbols to each quantity. If two quantities have the same magnitude, use the same symbol. Choose a coordinate system and draw it.
2. List the "known" (controlled by you)_ and "unknown" (to be measured or calculated) quantities in this problem.
3. Write down what principles of Physics you will use to solve the problem. Will you need any of the principles of kinematics? Write down any assumptions you have made that are necessary to solve the problem and are justified by the physical situation.
4. Start with the time interval in which the string exerts a force on the cart (before object A hits the floor). Draw separate freebody and force diagrams for object A and for the cart after they start accelerating. Check to see if any force pairs are related by Newton's 3rd Law. For each force diagram (one for the car and one for object A), write down Newton's 2nd law al ong each axis of the coordinate system. Be sure all signs are correct.
5. Write down an equation, from those you have collected in step 4 above, that relates what you want to know (the frictional force on the cart) to a quantity you either know or can find out (the acceleration of the cart). Is the force the string exerts on the cart equal to, greater than, or less than the gravitational pull on object A? Explain. Solve your equations for the frictional force on the cart in terms of the masses of the cart, the mass of object A, and the acceleration of the cart.
6. Now deal with the time interval in which the string does not exert a force on the cart (after object A hits the floor). Draw a freebody and force diagram for the cart. Write down Newton's 2nd law along each axis of the coordinate system. Be sure your signs are correct. Solve your equation for the frictional force on the cart in terms of the masses of the cart, the mass of object A, and the acceleration of the cart. You can now determine the frictional force on the cart for each case by measuring the accel eration of the cart.
7. Use the simulation "Lab4Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the effects of a very wide range of friction coefficients. If you believe friction may have affected your results, explore its effects with the simulation. Explore the effects of changing the mass of the string and the pulley. Do multiple runs and check the graphs produced. Use the simulation to compare the results with and without error. Look for theeffects in the position vs. time graph or in the velocity vs. time graph.

## EXPLORATION

Adjust the length of the string such that object A hits the floor well before the cart runs out of track. You will be analyzing a video of the cart both before and after object A has hit the floor. Consider how to distinguish these two cases in the same video. Adjust the string length to give you a video that is long enough to allow you to analyze enough of the motion to measure the cart's acceleration.

Choose a mass for the cart and find a mass for object A that allows you to reliably measure the cart's acceleration both before and after object A hits the floor. Because you are comparing the case of the string pulling on the cart with the case of the string not pulling on the cart, make sure the force of the string on the cart is as large as possible. Practice catching the cart before it hits the end stop on the track. Make sure the assumptions for your prediction are good for the situation in which you make the measurement. Use your prediction to determine if your choice of masses will allow you to measure the effect you are looking for. If not, choose different masses.

Write down your measurement plan. (Do you need video of the cart? Do you need video of object A ?)

## Measurement

Carry out the measurement plan you determined in the Exploration section.
Measure and record the mass of the cart and object A (with uncertainties). Record the height through which object A (the mass hanger) falls and the time it takes to fall.

Make enough measurements to convince yourself and others of your conclusion.

## Analysis

Using the height and time of object A's fall for each trial, calculate the cart's acceleration before object A hits the floor. Use the video to determine the cart's acceleration before and after object A. Is the "before" acceleration from the video consistent with the one you calculate based on time and height of fall?

Use the acceleration to determine the friction force before and after object A hits the floor.
What are the limitations on the accuracy of your measurements and analysis?

## Conclusion

Was the frictional force the same whether or not the string exerted a force on it? Does this agree with your initial prediction? If not, why?

## PROBLEM \#4: NORMAL FORCE AND KINETIC FRICTIONAL FORCEI

You work for a consulting firm with contracts to test the mechanical properties of different materials. A customer wants you to determine the coefficient of kinetic friction for wood on aluminum.

You decide to measure the coefficient of kinetic friction by graphing the frictional force as a function of the normal force when a wood block slides down an aluminum track. The coefficient of kinetic friction is the slope of that graph. Because there is measurement uncertainty no matter how you do the measurement, you decide to vary the normal force in two different ways. You divide your group into two teams. The other team will vary the normal force by changing the angle of incline of the track (Problem \#5). Y our team will vary the normal force by changing the mass of the block.

## EQUIPMENT

A wooden block slides down an aluminum track, as shown below.


The tilt of the aluminum track with respect to the horizontal can be adjusted. You can change the mass of the wooden block by attaching additional mass to it. With video analysis equipment you can determine the acceleration of the wooden block sliding down the aluminum track. Two wooden blocks, a meter stick, a stopwatch and a mass set are available for this experiment.

## Predictions

To make sense of your experimental results, you need to determinethe relationship between the coefficient of kinetic friction and thequantities that you can measure in experiment. You can look up the accepted value of the coefficient of friction from the Table of Coefficients of Friction near the end of this laboratory. Explain your reasoning.


Read: FishbaneChapter 5. Read carefully Sections 5-2 and Example 5-8.

To figure out your prediction you must determine how to calculate the normal force and the kinetic frictional force from quantities you can measure in this problem. It is useful to have an organized problem-solving strategy such as the one outlined in the following questions. You should use a technique similar to that used in Problem 1 (wherea more detailed set of Warm up questions are given) to solve this problem.

1. What do you expect for the shape of a graph of kinetic friction force vs. normal force? What do you expect for the slope?
2. Make a drawing of the problem situation similar to the one in the Equipment section. Draw vectors to represent all quantities that describe the motion of the block and the forces on it. What measurements can you make with a meter stick to determine the angle of incline? Choose a coordinate system. What is the reason for using the coordinate system you picked?
3. What measurements can you make to enable you to calculate the kinetic frictional force on the block? What measurements can you make to enable you to calculate the normal force on the block? Do you expect the kinetic frictional force thetrack exerts on the wooden block to increase, decrease, or stay the same as the normal force on the wooden block increases? Explain your reasoning.
4. Draw a freebody diagram of the wooden block as it slides down the aluminum track. Draw the acceleration vector for the block near the free-body diagram. Transfer the force vectors to your coordinate system. What angles between your force vectors and your coordinate axes are the same as the angle between the aluminum track and the table? Determineall of the angles between the force vectors and the coordinate axes.
5. Write down Newton's 2nd Law for the sliding block along each coordinate axis.
6. Using the equations from step 5 , determine an equation for the kinetic frictional force in terms of quantities you can measure. Next determine an equation for the normal force in terms of quantities you can measure. In your experiment, the measurable quantities include the mass of the block, the angle of incline and the acceleration of the cart.
7. Use the simulation "Lab1Sim" (See Appendix F for a brief explanation of how to use the simulations) to simulate the effects of a wide range of friction coefficients, block masses, initial speeds, and track angles.

## Exploration

Find an angle at which the wooden block accelerates smoothly down the aluminum track. Try this when the wooden block has different masses on top of it. Select an angle and series of masses that will make your measurements most reliable.

## Measurement

Keeping the aluminum track at the same angle, take a video of the wooden block's motion. Keep the track fixed when block is sliding down. M ake sure you measure and record that angle. Y ou will need it later.

Repeat this procedure for different block masses to change the normal force. Make sure the block moves smoothly down the incline for each new mass. Make sure every time you use the same surface of the block to contact the track.

Collect enough data to convince yourself and others of your conclusion about how the kinetic frictional force on the wooden block depends on the normal force on the wooden block.

## Analysis

For each new block mass and video, calculate the magnitude of the kinetic frictional force from the acceleration. Also determine the normal force on the block.

Graph the magnitude of the kinetic frictional force against the magnitude of the normal force, for a constant angle of incline. Use the graph to find the coefficient of kinetic friction.

## Conclusion

What is the coefficient of kinetic friction for wood on aluminum? How does this compare to the value on the table? Does the shape of the measured graph match the shape of the predicted graph? Over what range of values does the measured graph best match the predicted graph?

What are the limitations on the accuracy of your measurements and analysis?
If available, compare your value of the coefficient of kinetic friction (with uncertainty) with the value obtained by the different procedure given in the next problem. Arethe values consistent? Which way of varying the normal force to measure the coefficient of friction do you think is better? Why?

## PROBLEM \#5: NORMAL FORCE AND KINETIC FRICTIONAL FORCE II

You work for a consulting firm with contracts to test the mechanical properties of different materials. A customer wants your group to determine the coefficient of kinetic friction for wood on aluminum.

You decide to measure the coefficient of kinetic friction by graphing the frictional force as a function of the normal force when a wood block slides down an aluminum track. The coefficient of kinetic friction is the slope of that graph. Because there is experimental measurement uncertainty no matter how you do the measurement, you decide to vary the normal force in two different ways. You divide your group into two teams. The other team will vary the normal force by changing the mass of the block (Problem \#4). Y our team will vary the normal force by changing the angle of incline of the aluminum track.


A wooden block slides down an alumi num track, as shown below.


The tilt of the aluminum track with respect to the horizontal can be adjusted. You can change the mass of the wooden block by attaching additional mass to it. With video analysis equipment you can determine the acceleration of the wooden block sliding down the aluminum track. Two wooden blocks, a meter stick, a stopwatch and a mass set are available for this experiment.

## Predictions

To make sense of your experimental results, you need to determine the relationship between the coefficient of kinetic friction and the quantities that you can measure in experiment. Y ou can look up the accepted value of the coefficient of friction from theTable of Coefficients of Friction near the end of this laboratory. Explain your reasoning.


Read: Fishbane Chapter 5. Read carefully Sections 5-2 and Example 5-8.

To figure out your prediction you must determine how to calculate the normal force and the kinetic frictional force from the quantities you can measure in this problem. It is useful to have an organized problem-solving strategy such as the one outlined in the following questions. You should use a technique similar to that used in Problem 1 (where a more detailed set of Warm up questions are given) to solve this problem.

1. What do you expect for the shape of a graph of kinetic friction force vs. normal force? What do you expect for the slope?
2. Make a drawing of the problem situation similar to the one in the Equipment section. Draw vectors to represent all quantities that describe the motion of the block and the forces on it. What measurements can you make with a meter stick to determine the angle of incline? Choose a coordinate system. What is the reason for using the coordinate system you picked?
3. What measurements can you make to enable you to calculate the kinetic frictional force on the block? What measurements can you make to enable you to calculate the normal force on the block? Do you expect the normal force the track exerts on the wooden block to increase, decrease, or stay the same as the angle of the track increases? How do you expect the kinetic frictional force the track exerts on the wooden block to change if the normal force changes? Explain your reasoning.
4. Draw a free-body diagram of the wooden block as it slides down the aluminum track. Draw the acceleration vector for the block near the free-body diagram. Transfer the force vectors to your coordinate system. What angles between your force vectors and your coordinate axes are the same as the angle between the aluminum track and the table? Determine all of the angles between the force vectors and the coordinate axes.
5. Write down Newton's 2nd Law for the sliding block along each coordinate axis.
6. Using the equations from step 5, determine an equation for the kinetic frictional force in terms of quantities you can measure. Next determine an equation for the normal force in terms of quantities you can measure. In our experiment, the measurable quantities include the mass of the block, the angle of incline and the acceleration of the cart.
7. Use the simulation "Lab1Sim" (See A ppendix F for a brief explanation of how to use the simulations) to simulate the effects of a wide range of friction coefficients, block masses, initial speeds, and track angles.

## Exploration

Find a mass for which the wooden block accelerates smoothly down the aluminum track. Try this several different angles of the aluminum track.

Try different block masses. Select a mass that gives you the greatest range of track angles for reliable measurements.

## MeAsurement

Keeping the wooden block's mass fixed, take a video of its motion. Keep the track fixed when block is sliding down. M ake sure you measure and record each angle.

Repeat this procedure for different track angles. Make sure the block moves smoothly down the incline for each new angle. Make sure every time you use the same surface of the block to contact the track.

Collect enough data to convince yourself and others of your conclusion about how the kinetic frictional force on the wooden block depends on the normal force on the wooden block.
AnALYSIS

For each angle and video, calculate the magnitude of the kinetic frictional force from the acceleration. Also determine the normal force on the block.

Graph the magnitude of the kinetic frictional force against the magnitude of the normal force for a constant block mass. Use the graph to find the coefficient of kinetic friction.

## Conclusion

What is the coefficient of kinetic friction for wood on aluminum? How does this compare to the value on the table? Does the shape of the measured graph match the shape of the predicted graph? Over what range of values does the measured graph best match the predicted graph?

What are the limitations on the accuracy of your measurements and analysis?
If available, compare your value of the coefficient of kinetic friction (with uncertainty) with the value obtained by the procedure of the preceding problem. A re the values consistent? Which way of varying the normal force to measure the coefficient of friction do you think is better? Why?

TABLE: COEFFICIENTS OF FRICTION*

| Surfaces | $\mathbf{? ~}_{\mathbf{s}}$ | $\mathbf{?}_{\mathbf{k}}$ |
| :---: | :---: | :---: |
| Steel on steel | 0.74 | 0.57 |
| Aluminum on steel | 0.61 | 0.47 |
| Copper on steel | 0.53 | 0.36 |
| Steel on lead | 0.9 | 0.9 |
| Copper on cast iron | 1.1 | 0.3 |
| Copper on glass | 0.7 | 0.5 |
| Wood on wood | $0.25-0.5$ | 0.2 |
| Glass on glass | 0.94 | 0.4 |
| Metal on metal (lubricated) | 0.15 | 0.07 |
| Teflon on Teflon | 0.04 | 0.04 |
| Rubber on concrete | 1.0 | 0.8 |
| Ice on ice | 0.1 | 0.03 |
| Wood on Aluminum |  | $0.25-0.3$ |

* All values are approximate.


## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

1. A cart and Block 1 are connected by a massless string that passes over a frictionless pulley, as shown in the diagram below.


When Block 1 is rel eased, the string pulls the cart toward the right along a horizontal table. For each question below, explain the reason for your choice.
a. The speed of the cart is:
(a) constant.
(b) continuously increasing.
(c) continuously decreasing.
(d) increasing for a while, and constant thereafter.
(e) constant for a while, and decreasing thereafter.
b. The force of the string on Block 1 is
(a) zero.
(b) greater than zero but less than the weight of Block 1.
(c) equal to the weight of Block 1.
(d) greater than the weight of Block 1.
(e) It is impossible to tell without knowing the mass of Block 1.
c. When the cart traveling on the table reaches position $x$, the string breaks. The cart then
(a) moves on at a constant speed.
(b) speedsup.
(c) slows down.
(d) speeds up, then slows down.
(e) stops at $x$.
d. Block 1 is now replaced by a larger block (Block 2) that exerts twice the pull as was exerted previously. The cart is again reset at starting position $x_{0}$ and released. The string again breaks at position $x$. Now, what is the speed of the cart at position $x$ compared to its speed at that point when pulled by the smaller Block 1?
(a) Half the speed it reached before.
(b) Smaller than the speed it reached before, but not half of it.
(c) Equal to the speed it reached before.
(d) Double the speed it reached before.
(e) Greater than the speed it reached before, but not twice as great.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

2. A crate is given an initial push up the ramp of a large truck. It starts sliding up the ramp with an initial velocity $v_{0}$, as shown in the diagram below. The coefficient of kinetic friction between the box and the floor is? k .


Will the magnitude of the acceleration of the sliding crate be greater on the way up or on the way back down the ramp? Or will the accelerations be the same? Explain using appropriate force diagrams.
3. The same constant force $(P)$ is applied to three identical boxes that are sliding across the floor. The forces are in different directions, as shown in the diagram below.


On which of the three boxes is the frictional force the largest? The smallest? Or is the frictional force on each box the same? Explain using appropriate force diagrams and $N$ ewton's second law.
4. A lamp is hanging from two light cords. The cords make unequal angles with the ceiling, as shown in the diagram at right.
a. Draw the force diagram of the lamp. Clearly describe each force drawn.

b. Is the horizontal component of the pull of the left cord on the lamp greater than, less than, or equal to the horizontal component of the pull of theright cord on the lamp? Explain your reasoning.
c. Is the vertical component of the pull of the left cord on the lamp greater than, less than, or equal to the vertical component of the pull of theright cord on the lamp? Explain your reasoning.
d. Is the vertical component of the pull of the left cord on the lamp greater than, less than, or equal to half the weight of the lamp? Explain your reasoning.
$\qquad$

## PHYSICS 1301LABORATORY REPORT <br> Laboratory III

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readable; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATA AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly ; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL(incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total points <br> achieved) |  |
| BONUS POINTS FOR TEAMWNORK <br> (as specified by course policy) |  |

* An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORYIV CONSERVATION OF ENERGY

In this lab you will begin to use the principle of conservation of energy to determine the motion resulting from interactions that are difficult to analyze using force concepts alone. You will explore how conservation of energy is applied to real interactions. Keep in mind that energy is always conserved, but it is sometimes difficult to calculate the value of all energy terms relevant for an interaction. Some energy may be transferred into or out of the system of interest, and some may be transformed to internal energy of the system. One outcome can be that some fraction of a system's energy of motion before an interaction is not visible energy of motion after the interaction. Since the energy is no longer observable in the macroscopic motion of objects, we sometimes say that the energy is "dissipated" in the interaction.

The first four problems in this laboratory explorethe application of conservation of energy using carts. The fifth problem deals with the very real complication of friction.

## ObJECTIVES:

Successfully completing this laboratory should enable you to:

- Use conservation of energy to predict the outcome of interactions between objects.
- Choose a useful system when using conservation of energy.
- Identify different types of energy when applying energy conservation to real systems.
- Decide when conservation of energy is not useful to predict the outcome of interactions between objects.


## Preparation:

Read Paul M. Fishbane: Chapter 6, Chapter 7. You should also be able to:

- Analyze the motion of an object using video analysis.
- Calculate the kinetic energy of a moving object.
- Calculate the work transferred to or from a system by an external force.
- Calculate the total energy of a system of objects.
- Cal culate the gravitational potential energy of an object with respect to the earth.


## PROBLEM \#1: KINETIC ENERGY AND WORK I

You are working at a company that designs pinball machines and have been asked to devise a test to determine the efficiency of some new magnetic bumpers. You know that when a normal pinball rebounds off traditional bumpers, some of the initial energy of motion is "dissipated" in the deformation of the ball and bumper, thus slowing the ball down. The lead engineer on the project assigns you to determine if the new magnetic bumpers are more efficient. The engineer tells you that the efficiency of a collision is the ratio of the final kinetic energy to the initial kinetic energy of the system.

To limit the motion to one dimension, you decide to model the situation using a cart with a magnet colliding with a magnetic bumper. You will use a level track, and use a video data acquisition system to measure the cart's velocity before and after the collision. You begin to gather your camera and data acquisition system when your colleague suggests a method with simpler equipment. Your colleague claims it would be possible to release the cart from rest on an inclined track and make measurements with just a meter stick. You are not sure you believe it, so you decide to measure the energy efficiency both ways, and determine the extent to which you get consistent results. For this problem, you will use the level track. For problem \#2, you will work with the inclined track.

## EquIPMENT

You will use the video analysis equipment to analyze the motion of a cart colliding with an end stop (the magnetic bumper) on the track. You will also have a meter stick, a stopwatch and a balance to measure the mass of the cart.

## Predictions

Calculate the energy efficiency of the bumper discussed in the problem in terms of the least number of quantities that you can easily measure in the situation of a level track. Calculate the energy dissipated during the impact with the bumper in terms of those measurablequantities.


Read: Fishbane Chapter 6, section 6.1.

1. It is useful to have an organized problem-solving strategy. The following questions will help with your prediction and the analysis of your data.
2. Make a drawing of the cart on the level track before and after the impact with the bumper. Define your system. Label the velocity and kinetic energy of all objects in your system before and after the impact.
3. Write an expression for the efficiency of the bumper in terms of the final and initial kinetic energy of the cart.
4. Write an expression for the energy dissipated during the impact with the bumper in terms of the kinetic energy before the impact and the kinetic energy after the impact.

## EXPLORATION

Review your exploration notes for measuring a velocity using video analysis. Practice pushing the cart with different velocities, slowly enough that the cart will never contact the bumper (end stop) during the impact when you make a measurement. Find a range of velocities for your measurement. Set up the camera and tripod to give you a useful video of the collision immediately before and after the cart collides with the bumper.

Although the effect of friction is small in our lab, you may want to estimate it. Make a schedule to test the effect of friction by the data from video.

## MeAsurement

Take the measurements necessary to determine the kinetic energy before and after the impact with the bumper. What is the most efficient way to measure the velocities with the video equipment? Take data for several different initial velocities.


Calculate the efficiency of the bumper for the level track. Does your result depend on the velocity of the cart before it hits the bumper?

## Conclusion

What is the efficiency of the magnetic bumpers? How much energy is dissipated in an impact? What is effect of friction in your experiment? State your results in the most general terms supported by your analysis.

If available, compare your value of the efficiency (with uncertainty) with the value obtained by the different procedure given in the next problem. Are the values consistent? Which way to measure the efficiency of the magnetic bumper do you think is better? Why?

## PROBLEM \#2: <br> KINETIC ENERGY AND WORK II

You are working at a company that designs pinball machines and have been asked to devise a test to determine the efficiency of some new magnetic bumpers. You know that when a normal pinball rebounds off traditional bumpers, some of the initial energy of motion is "dissipated" in the deformation of the ball and bumper, thus slowing the ball down. The lead engineer on the project assigns you to determine if the new magnetic bumpers are more efficient. The engineer tells you that the efficiency of a collision is the ratio of the final kinetic energy to the initial kinetic energy of the system.

To limit the motion to one dimension, you decide to model the situation using a cart with a magnet colliding with a magnetic bumper. You will use a level track, and use a video data acquisition system to measure the cart's velocity before and after the collision. You begin to gather your camera and data acquisition system when your colleague suggests a method with simpler equipment. Your colleague claims it would be possible to release the cart from rest on an inclined track and make measurements with just a meter stick. You are not sure you believe it, so you decide to measure the energy efficiency both ways, and determine the extent to which you get consistent results. For this problem, you will use the inclined track. For problem \#1, you will work with the level track.

## EquIPMENT

You will have a meter stick, a stopwatch, cart masses and a wooden block to create the incline. You may also use the video analysis equipment to estimate the effect of friction.

## Predictions

Calculate the energy efficiency of the bumper (with friction and without) in terms of the least number of quantities that you can easily measure in the situation of an inclined track.

## Warm Up

Read: FishbaneChapter 6, sections 6.1-6.2.
The following questions will help you to make your prediction and analyze your data.

1. Make a drawing of the cart on the inclined track at its initial position (before you release the cart) and just before the cart hits the bumper. Define the system. Label the kinetic energy of all objects in your system at these two points, the distance the cart traveled, the angle of incline, and the initial height of the cart above the bumper.
2. Now make another drawing of the cart on the inclined track just after the collision with the bumper and at its maximum rebound height. Label kinetic energy of the cart at these two
points, the distance the cart traveled, the angle of the ramp, and the rebound height of the cart above the bumper.
3. Write an expression for the efficiency of the bumper in terms of the kinetic energy of the cart just before the impact and the kinetic energy of the cart just after the impact.
4. Draw a force diagram of the cart as it moves down the track. Which force component does work on the cart (i.e., causes a transfer of energy into the cart system)? Write an expression for the work done on the cart. H ow is the angle of the ramp related to the distance the cart traveled and the initial height of the cart above the bumper? How does the kinetic energy of the cart just before impact compare with the work done on the cart?
5. Draw a force diagram of the cart as it moves up the track. Which force component does work on the cart (i.e., causes a transfer of energy out of the cart system)? Write an expression for the work done on the cart. How does the kinetic energy of the cart just after impact compare with the work done on the cart?
6. Write an expression for the efficiency of the bumper in terms of the cart's initial height above the bumper and the cart's maximum rebound height above the bumper.
7. Write an expression for the energy dissipated during the impact with the bumper in terms of the kinetic energy of the cart just before the impact and the kinetic energy of the cart after the impact. Rewrite this expression in terms of the cart's initial height above the bumper and the cart's maximum rebound height above the bumper.
8. Repeat the procedure, considering the effect of friction.

## Exploration

Find a useful range of heights and inclined angles that will not cause damage to the carts or bumpers. Make sure that the cart will never contact bumper (end stop) during the impact. Decide how you are going to consistently measure the height of the cart.

You may want to estimate the effect of friction. Make a schedule to test the effect of friction by the video analysis equipment. How can you find the average frictional force when the cart moves on the inclined track? How much energy is dissipated by friction?

## MeAsurement

Take the measurements necessary to determine the kinetic energy of the cart just before and after the impact with the bumper. Take data for several different initial heights.

## Analysis

Calculate the efficiency of the bumper for the inclined track. Does your result depend on thevelocity of the cart before it hits the bumper?

## Conclusion

What is the efficiency of the magnetic bumpers? How much energy is dissipated in an impact? State your results in the most general terms supported by your analysis. Is effect of friction significant?

If available, compare your value of the efficiency (with uncertainty) with the value obtained by the different procedure given in the preceding problem. A re the values consistent? Which way to measure the efficiency of the magnetic bumper do you think is better? Why?

## PROBLEM \#3: <br> ENERGYIN COLLISIONS WHEN OBJECTS STICK TOGETHER

You work with the Minnesota Traffic Safety Board. You are helping to write a report about the damage done to vehicles in different kinds of traffic accidents. Your boss wants you to concentrate on the damage done when a moving vehicle hits a stationary vehicle and they stick together.

You know that in a traffic collision, some of the initial energy of motion is "dissipated" in the deforming (damaging) of the vehicles. Your boss believes that the amount of damage done in such a collision depends only on the total mass of the two vehicles and the initial kinetic energy of the moving vehicle, but other members of the team disagree. Is your boss correct?

You decide to test your prediction by measuring the energy efficiency of three different cart collisions: one in which the moving cart is more massive, one in which the stationary cart is more massive, and one in which the moving and stationary carts are equally massive.

## EQUIPMENT

You will use the track and carts with which you are familiar. For this problem, cart A is given an initial velocity towards a stationary cart B. There are pads at the end of each cart. The pads allow the carts to stick together after the collision. Video analysis equipment allows you to determine the cart velocities before and after the collision. You also have a meter stick, a stopwatch, two end stops and cart masses.


Consider the three cases described in the problem, with the same total mass of the carts for each case ( $m_{A}+m_{B}=$ constant). Rank the collisions from most efficient to least efficient. (Make an educated guess and explain your reasoning.)

Calculate the energy dissipated in a collision in which the carts stick together, as a function of the mass of each cart, the initial kinetic energy of the system, and the energy efficiency of the collision. Assuming the kinetic energy of the incoming vehicle is the same in each case, use your calculation and your educated guess to determine which collision will cause the most damage.

## Warm UP

Read: FishbaneChapter 6, sections 6.1-6.2.
The following questions will help you with the calculation part of the prediction and with the analysis of your data.

1. Draw two pictures, one showing the situation before the collision and the other one after the collision. Is it reasonable to neglect friction? Draw velocity vectors on your sketch. Define your system. If the carts stick together, what must be true about their final velocities? Write down the energy of thesystem before and after the collision.
2. Write down the energy conservation equation for this collision (Remember to take into account the energy dissipated).
3. Write an equation for the efficiency of the collision in terms of the final and initial kinetic energy of the carts, and then in terms of the cart masses and their initial and final speeds.
4. Solve your equations for the energy dissipated.
5. Use the simulation "Lab3Sim" (See Appendix F for a brief explanation of how to use the simulations) to explore the conditions of this problem. For this problem you will want to set the elasticity to zero.

## Exploration

Practice rolling the cart so the carts will stick together after colliding. Carefully observe the carts to determine whether either cart leaves the grooves in the track. Minimize this effect so that your results are reliable.

Try giving the moving cart various initial velocities over the range that will give reliable results. Note qualitatively the outcomes. Choose initial velocities that will give you useful videos.

Try varying the masses of the carts so that the mass of the initially moving cart covers a range from greater than the mass of the stationary cart to less than the mass the stationary cart while keeping the total mass of the carts the same. Is the same range of initial velocities useful with different masses? If the moving cart should have approximately the same kinetic energy for each collision, how should its speed depend on its mass? What masses will you use in your final measurement?

## Measurement

Record the masses of the two carts. Make a video of their collision. Examine your video and decide if you have enough frames to determine the velocities you need. Do you notice any peculiarities that might suggest the data is unreliable?

Analyze your data as you go along (before making the next video), so you can determine how many different videos you need to make, and what the carts' masses should be for each video. Collect enough data to convince yourself and others of your conclusion about how the energy efficiency of this type of collision depends on the relative masses of the carts.

Save all of your data and analysis. You will use it again for Laboratory V.

## Analysis

Determine the velocity of the carts before and after the collision using video analysis. For each video, calculate the kinetic energy of the carts before and after the collision.

Calculate the energy efficiency of each collision. Into what other forms of energy do you think the cart's initial kinetic energy is most likely to transform?

Graph how the energy efficiency varies with mass of the initially moving cart (keeping the total mass of both carts constant). What function describes this graph? Repeat for energy efficiency as a function of initial velocity.
$M$ ake sure everyone in your group gets the chance to operate the computer.

## CONCLUSION

Which case ( $m_{A}=m_{B}, m_{A}>m_{B}$, or $m_{A}<m_{B}$ ) is the energy efficiency the largest? The smal lest? Does this make sense? (Imagine extreme cases, such as a flea running into a truck and a truck running into a flea. In which case must the incoming "vehicle" be moving faster to satisfy your boss's assumption about initial kinetic energy? Which collision might cause more damage to the flea? To the truck?)

Was a significant portion of the energy dissipated? Into what other forms of energy do you think the cart's initial kinetic energy is most likely to transform?

Can you approximate the results of this type of collision by assuming that the energy dissipated is small?

Was your boss right? Is the same amount of damage done to the vehicles when a car hits a stationary truck and they stick together as when the truck hits the stationary car (given the same initial kinetic energies)? State your results that support this conclusion.

Suppose two equal mass cars traveling with equal speeds in opposite directions collide head on and stick together. What fraction of the energy is dissipated? Try it.

## PROBLEM \#4: <br> ENERGYIN COLLISIONS WHEN OBJECTS BOUNCE APART

You work for a cable TV sports network, which is interested in developing a new form of "extreme bowling". One feature of the game will be that the masses of the (rolling) bowling balls and (stationary) bowling pins will vary greatly over the course of a match. Another feature is that they will bounce off each other when a ball runs into a pin. Your boss speculates that the energy efficiency of the collisions is useful information, and that it will change with the speed of the ball and the relative masses of the balls and pins. In order to save the most spectacular collisions until the final frames, your boss asks you to determine the energy efficiencies and energy dissipation over a range of ball masses and pin masses. Is your boss correct?

You decide to test your prediction with three different cart collisions: one in which the moving cart is more massive, one in which the stationary cart is more massive, and one in which the moving and stationary carts are equally massive. As a control, you assume that the total mass of the colliding objects remains constant. For your model you use the most efficient bumper you can think of, a magnetic bumper.

## EQUIPMENT

You will use the same equipment as in Problem 3. Magnets at the end of each cart are used as bumpers to ensure that the carts bounce apart after the collision. The video analysis equipment is available to determine the velocities of the carts. You will also have a meter stick, a stopwatch, two end stops and cart masses.


## Prediction

Consider the three cases described in the problem, with the same total mass of the carts for each case ( $m_{A}+m_{B}=$ constant). Rank the collisions from most efficient to least efficient. (Make an educated guess and explain your reasoning.)

Calculate the energy dissipated in a collision in which the carts bounce apart, as a function of the mass of each cart, the initial kinetic energy of the system, and the energy efficiency of the collision. Assuming the kinetic energy of the incoming cart is the same in each case, use your calculation and your educated guess to determine which collision will dissipate the most energy.

## Warm UP

Read: FishbaneChapter 6, sections 6.1-6.2.
The following questions will help you with the calculation part of the prediction and with the analysis of your data.

1. Draw two pictures that show the situation before the collision and after the collision. In this experiment the friction between the carts and the track is negligible. Draw velocity vectors on your sketch. Define your system. Write down the energy of the system before the collision and al so after the collision.
2. Write down the energy conservation equation for this collision (Do not forget to include the energy dissipated).
3. Write an equation for the efficiency of the collision in terms of the final and initial kinetic energy of the carts, and then in terms of the cart masses and their initial and final speeds.
4. Solve your equations for theenergy dissipated.
5. Use the simulation "Lab3Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the conditions of this problem. For this problem you will want to set the elasticity to something other than zero.

## EXPLORATION

Practice setting the cart into motion so that the carts don't touch when they collide. Also, after the collision carefully observe the carts to determine whether or not either cart leaves the grooves in the track. Minimize this effect so that your results are reliable.

Try giving the moving cart various initial velocities over the range that will give reliable results. Note qualitatively the outcomes. Choose initial velocities that will give you useful videos.

Try varying the masses of the carts so that the mass of the initially moving cart covers a range from greater than the mass of the stationary cart to less than the mass of the stationary cart while keeping the total mass of the carts the same. Is the same range of initial velocities useful with different masses? Be sure the carts still move freely over the track. What masses will you use in your final measurement?

## Measurement

Record the masses of the two carts. Make a video of their collision. Examine your video and decide if you have enough positions to determine the velocities that you need. Do you notice any peculiarities that might suggest the data is unreliable?

Analyze your data as you go along (before making the next video), so you can determine how many different videos you need to make, and what the carts' masses should be for each video. Collect enough data to convince yourself and others of your conclusion about how the energy efficiency of this type of collision depends on the relative masses of the carts.

Save all of your data and analysis. You will useit again for Laboratory V.


Determine the velocity of the carts before and after the collision using video analysis. For each video, cal culate the kinetic energy of the carts before and after the collision.

Cal culate the energy efficiency of each collision. Into what other forms of energy do you think the cart's initial kinetic energy is most likely to transform?

Graph how the energy efficiency varies with mass of the initially moving cart (keeping the total mass of both carts constant). What function describes this graph? Repeat for energy efficiency as a function of initial velocity.

## CONCLUSION

For which case $\left(m_{A}=m_{B}, m_{A}>m_{B}\right.$, or $\left.m_{A}<m_{B}\right)$ is the energy efficiency the largest? The smallest?

Was a significant portion of the energy dissipated? How does it compare to the case where the carts stick together after the collision? Into what other forms of energy do you think the cart's initial kinetic energy is most likely to transform?

Could the collisions you measured be considered essentially elastic collisions? Why or why not? The energy efficiency for a perfectly elastic collision is 1.

Can you approximate the results of this type of collision by assuming that the energy dissipated is small?

Was your boss right? Does the energy efficiency of a "bouncing" collision seem to depend on the rel ative masses of the objects? If so, how? State your results that support this conclusion.

## PROBLEM \#5: ENERGY AND FRICTION

You work for an auto company, which has experienced work stoppages when novice forklift drivers stop suddenly, causing crates of auto parts to slide off the forklift and spill on the floor. Your team is investigating the conditions under which such accidents will occur, in order to improve driver training. What factors are important? Your task is to calculate the distance a crate slides after the forklift has come to a sudden stop, as a function of the forklift's initial speed. You assume that the crate is not tied down, and that the surface supporting the crate is horizontal.

To test your prediction, you will model the situation with a cart on the track.

## EQUIPMENT

You will have a cart, cart masses, a track, an end stop, a wood/ cloth block, a mass set, a meter stick, a stopwatch and the video analysis equipment to determine the velocity of the cart before the collision. You will need to put the cart masses on the top of the cart so that the wood/ cloth block can slide on the cart. You can suddenly stop the cart by colliding it with the end stop on the track. Friction between the cart and the track is negligible.


## Predictions

Calculate the distance the block slides in the situation described in the problem as a function of the cart's speed before the collision. Illustrate your prediction graphically.

## Warm up

Read: FishbaneChapter 6, sections 6.4-6.4.
Thefollowing questions will help with the prediction, and analysis of your data.

1. Draw three pictures: one showing the situation just before the collision of the cart with the end-stop, one immediately after the collision when the cart is stopped but the block has not yet begun to slow down, and the third when the wood block has cometo rest. Draw velocity vectors on your sketches, and label any important distances. What is the relationship between the cart's velocity and the wood block's velocity in each picture? Define your system. Write down the energy of the system for each picture.
2. Write down the energy conservation equation for this situation, between the second and third pictures. Is any energy transferred into or out of the system?
3. Draw a force diagram for the wood/ cloth block as it slides across the cart. Identify the forces that do work on the block (i.e., result in the transfer of energy in or out of the system). Write an equation relating the energy transferred by these forces to the distance the block slides.
4. Complete your prediction, and graph sliding distance vs. initial forklift speed.

## Exploration

Practice setting the cart with masses into motion so the cart sticks to the end stop. What adjustments are necessary to make this happen consistently? Place the wood/ cloth block on the cart. Try giving the cart various initial velocities. Choose a range of initial velocities that give you good video data. Make sure that the wood/ cloth block does not begin to slide on the cart before the collision. Try several masses for the cart and the block. N ote qualitatively the outcomes when the cart sticks to the end stop.

## Measurement

Make the measurements that you need to check the prediction. Because you are dealing with friction, it is especially important that you repeat each measurement several times under the same conditions to see if it is reproducible.


Make a graph of the distance the block travels as a function of the cart's initial speed. Does this result depends on the mass of the block or the mass of the cart? If the graph is not linear, graph the distance vs. some power of the speed to produce a linear graph (see A ppendix C). (Use your prediction to guess which power of speed to use.) What is the meaning of the slope of that line?

## Conclusion

Do your results agree with your predictions? What are the limitations on the accuracy of your measurements and analysis? As a check, determine the coefficient of kinetic friction between the block and the cart from your results. Is it reasonable?

Does the distance that the crate slides depend on the mass of the forklift? On the mass of the crate? If the sliding distance varies linearly with some power of the forklift's initial speed, what is that power? What would you tell forklift drivers about the effect of doubling their speed? In a sentence or two, relate this result to conservation of energy.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING:

1. A 1 kg ball dropped from a height of 2 meters rebounds only 1.5 meters after hitting the floor. The amount of energy dissipated during the collision with the floor is:
(a) 5 joules.
(b) 10 joules.
(c) 15 joules.
(d) 20 joules.
(e) More than 20 joules.
2. Two boxes start from rest and slide down a frictionless ramp that makes an angle of $30^{\circ}$ with the horizontal. Block A starts at height $h$, while Block $B$ starts at a height of 2 h .

a. Suppose the two boxes have the same mass. At the bottom of the ramp,
(a) BoxA is moving twice as fast as box $B$.
(b) Box $B$ is moving twice as fast as box $A$.
(c) Box $A$ is moving faster than box $B$, but not twice as fast.
(d) Box $B$ is moving faster than box $A$, but not twice as fast.
(e) Box $A$ has the same speed as box $B$.
b. Suppose box $B$ has a larger mass than box $A$. At the bottom of the ramp,
(a) Box $A$ is moving twice as fast as box $B$.
(b) Box $B$ is moving twice as fast as box $A$.
(c) Box $A$ is moving faster than box $B$, but not twice as fast.
(d) Box $B$ is moving faster than box $A$, but not twice as fast.
(e) Box $A$ has the same speed as box $B$.
3. A hockey puck is moving at a constant velocity to the right, as shown in the diagram. Which of the following forces will do positive work on the puck (i.e., cause an input of energy)?

(a)

(b)

(c)

(d)

(e)

## $\square$ CHECK YOUR UNDERSTANDING

4. Five balls made of different substances are dropped from the same height onto a board. Four of the balls bounce up to the maximum height shown on the diagram below. Ball E sticks to the board.


B

a. For which ball was the most energy dissipated in the collision?
(a) Ball A
(b) Ball B
(c) Ball C
(d) Ball D
(e) Ball E
b. Which ball has the largest energy efficiency?
(a) Ball A
(b) Ball B
(c) Ball C
(d) Ball D
(e) Ball E
5. A skier is pulled a distance $x$ up a hill at a constant velocity by a towrope. The coefficient of friction between the skis and the snow is? $k$.

a. Draw a force diagram of the skier. Which of the forces acting on the skier do positive work (i.e., cause an input of energy). Which of the forces do negative work (i.e., cause an output of energy)? Explain your reasoning.
b. Based on the definition of work, write an expression for the positive work done on the skier (i.e., the energy input). Write an expression for the negative work done on the skier (i.e., the energy output).
c. Which is larger, the positive work done on the skier or the negative work done on the skier? Or are they the same size? Explain your reasoning?
$\qquad$

## PHYSICS 1301 LABORATORY REPORT Laboratory IV

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in joumnal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readabbe; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATA AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly ; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL(incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total <br> points achieved) |  |
| BONUS POINTS FOR TEAMWORK <br> (as specified by course policy) |  |

* An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORYV CONSERVATION OFMOMENTUM

In this lab you will use conservation of momentum to predict the motion of objects resulting from collisions. It is often difficult or impossible to obtain enough information for a complete analysis of collisions in terms of forces. Conservation principles can be used to relate the motion of objects before a collision to motion after the collision without knowledge of the complicated details of the collision process itself, but conservation of energy alone is usually not enough to predict the outcome. To fully analyze a collision, one must often use both conservation of energy and conservation of momentum.

## Objectives:

Successfully completing this laboratory should enable you to:

- Use conservation of momentum to predict the outcome of interactions between objects.
- Choose a useful system when using conservation of momentum.
- Identify momentum transfer (impulse) when applying momentum conservation to real systems.
- Use the principles of conservation of energy and of momentum together to describe the behavior of systems.


## Preparation:

Read Paul M. Fishbane: Chapter 8. You should also be able to:

- Analyze the motion of an object using video analysis.
- Calculate the work transferred to or from a system by an external force.
- Calculate the total energy of a system of objects.
- Calculate the total momentum of a system of objects.


## PROBLEM \#1: <br> PERFECTLY INELASTIC COLLISIONS

You work for NASA with a group designing a docking mechanism that would allow two space shuttles to connect with each other. The mechanism is designed for one shuttle to move carefully into position and dock with a stationary shuttle. Since the shuttles may be carrying different payloads and different amounts of fuel, their masses may not be identical: the shuttles could be equally massive, the moving shuttle could be more massive, or the stationary shuttle could have a larger mass. Your supervisor wants you to calculate the magnitude and direction of the velocity of the pair of docked shuttles, as a function of the initial velocity of the moving shuttle and the mass of each shuttle. You may assume that the total mass of the two shuttles is constant. Y ou decide to model the problem in the lab using carts to check your predictions.

## EqUIPMENT

You will use the track and carts with which you are familiar. For this problem, cart A is given an initial velocity towards a stationary cart B. Pads at the end of each cart allow the carts to stick together after the collision. Video analysis equipment is available. Y ou will also need a meter stick, a stopwatch, two end stops and cart masses.


Restate the problem to identify your target and get the relationships useful for the three cases considered in the problem.


Read: FishbaneChapter 8, sections 8.1-8.3.

The following questions are designed to help you with your prediction and the analysis of your data.

1. Make two drawings that show the situation (a) before and (b) after the collision. Show and label velocity vectors for each object in your drawings. If the carts stick together, what must betrue about their final velocities? Defineyour system.
2. Write down the momentum conservation equation for the system; identify all of the terms in the equation. Are there any of these terms that you cannot measure with the equipment at hand? Is the momentum of the system conserved during the collision? Why or why not?
3. Write down the energy conservation equation for the system; identify all the terms in the equation Are there any of these terms that you cannot measure with the equipment at hand? Is the energy of the system conserved? Why or why not? Is the kinetic energy of the system conserved? Why or why not?
4. Which conservation principle should you use to predict the final velocity of the stucktogether carts, or do you need both equations? Why?
5. Use the simulation "Lab3Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the conditions of this problem. For this problem you will want to set the elasticity to zero.

## Exploration

If you have done Problem \#3 in Lab IV, you should be able to skip this part.
Practice rolling the cart so the carts will stick together after colliding. Carefully observe the carts to determine whether either cart leaves the grooves in the track. Minimize this effect so that your results are reliable.

Try giving the moving cart various initial velocities over the range that will give reliable results. N ote qualitatively the outcomes. Choose initial velocities that will give you useful videos.

Try varying the masses of the carts so that the mass of the initially moving cart covers a range from greater than the mass of the stationary cart to less than the mass the stationary cart while keeping the total mass of the carts the same. Is the same range of initial velocities useful with different masses? What masses will you use in your final measurement?

## Measurement

If you have done Problem \#3 in Lab IV, you should be able to skip this part and just use the data you have already taken. Otherwise make the measurements outlined below.

Record the masses of the two carts. Make a video of their collision. Examine your video and decide if you have enough frames to determine the velocities you need. Do you notice any peculiarities that might suggest the data is unreliable?

Analyze your data as you go along (before making the next video), so you can determine how many different videos you need to make, and what the carts' masses should be for each video. Collect enough data to convince yourself and others of your conclusion about how the final velocity of both carts in this type of collision depends on velocity of the initially moving cart and the masses of the carts.

## Analysis

Determine the velocities of the carts (with uncertainty) before and after each collision from your video. Cal culate the momentum of the carts before and after the collision.

Now use your Prediction equation to calculate each final velocity (with uncertainty) of the stucktogether carts.

## CONCLUSION

How do your measured and predicted values of the final velocity compare? Compare both magnitude and direction. What arethe limitations on the accuracy of your measurements and analysis?

When a moving shuttle collides with a stationary shuttle and they dock (stick together), how does the final velocity depend on the initial velocity of the moving shuttle and the masses of the shuttles? State your results in the most general terms supported by the data.

What conditions must be met for a system's total momentum to be conserved? Describe how those conditions were or were not met for the system you defined in this experiment. What conditions must be met for a system's total energy to be conserved? Describe how those conditions were or werenot met for the system you defined in this experiment.

## PROBLEM \#2: ELASTIC COLLISIONS

You are still working for NASA with the group designing a docking mechanism that would allow two space shuttles to connect with each other. Themechanism is designed for one shuttle to move carefully into position and dock with a stationary shuttle. Since the shuttles may be carrying different payloads and have consumed different amounts of fuel, their masses may be different when they dock: the shuttles could be equally massive, the moving shuttle could be more massive, or the stationary shuttle could have a larger mass.

Your supervisor wants you to consider t case which could result from the pilot missing the docking mechanism or the mechanismfailing to function. In this casethe shuttles gently collide and bounce off each other. Your supervisor asks you to calculate the final velocity of both shuttles as a function of (a) the initial velocity of the initially moving shuttle, (b) the masses of both shuttles, and (c) the fraction of the moving shuttle's initial kinetic energy that is not dissipated during the collision (the "energy efficiency"). You may assume that the total mass of the two shuttles is constant. You decide to check your calculations in the laboratory using the most efficient bumper you have, a magnetic bumper.

## EQUIPMENT

You will use the same equipment as in Problem \#lm except that magnets will be used to bounce the carts apart after the collision. Masses can be added to the top of either cart. The video analysis equipment is available. You will also need a meter stick, a stopwatch, two end stops and cart masses.


Restate the problem such that you understand and identify its goal then get the equations necessary to test your lab model.

## Warm UP

Read: FishbaneChapter 8, sections 8.1-8.2 and 8.4.
Thefollowing questions are designed to help you with your prediction and the analysis of your data.

1. Draw two pictures that show thesituation before the collision and after the collision. Draw velocity vectors on your sketch. If the carts bounce apart, do they have the same final velocity? Define your system.
2. Write down the momentum of the system before and after the collision. Is the system's momentum conserved during the collision? Why or why not?
3. If momentum is conserved, write the momentum conservation equation for this situation; identify all of the terms in the equation.
4. Write down theenergy of the system (a) before and (b) after the collision.
5. Write down the energy conservation equation for this situation and identify all the terms in the equation.
6. Write the expression for the energy dissipated in the collision in terms of the energy efficiency and the initial kinetic energy of the system (see Laboratory IV, Problem \#4). Can you assume that no energy will be converted into internal energy?
7. Solve the equations you wrote in previous steps to find the final velocity of each cart in terms of the cart masses, the energy efficiency of the collision, and the initial speed of the moving cart. W arning: the algebra may quickly become unpleasant! Stay organized.
8. Use the simulation "Lab3Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the conditions of this problem. For this problem you will want to set the elasticity to something other than zero.

## EXPLORATION

If you have done Problem \#4 in Lab IV, you should be able to skip this part.
Practice setting the cart into motion so that the carts don't touch when they collide.. Carefully observe the carts to determine whether or not either cart leaves the grooves in the track. Minimize this effect so that your results are reliable.

Try giving the moving cart various initial velocities over the range that will give reliable results. Note qualitatively the outcomes. Keep in mind that you want to choose an initial velocity that gives you a good video.

Try varying the masses of the carts so that the mass of the initially moving cart covers a range from greater than the mass of the stationary cart to less than the mass the stationary cart while keeping the total mass of the carts the same. Be sure the carts still move freely over the track. What masses will you use in your final measurement?

## Measurement

If you have done Problem \#4 in Lab. IV, you should be able to skip this part and just use the data you have already taken. Otherwise make the measurements outlined below.

Record the masses of the two carts. Make a video of their collision. Examine your video and decide if you have enough frames to determine the vel ocities you need. Do you notice any peculiarities that might suggest the data is unreliable?

Analyze your data as you go along (before making the next video), so you can determine how many different videos you need to make, and what the carts' masses should be for each video. Collect enough data to convince yourself and others of your conclusion about how the final velocities of both carts in this type of collision depend on the velocity of the initially moving cart, the masses of the carts, and the energy efficiency of the collision.

## Analysis

Determine the velocities of the carts (with uncertainty) before and after each collision from your video. Cal culate the momentum and kinetic energy of the carts before and after the collision.

If you have the results from Lab IV, Problem 4, use the appropriate energy efficiency you determined for the collision from that problem. If not, calculate the energy efficiency of each collision from the initial and final kinetic energy of the system. Graph how the energy efficiency varies with mass of the initially moving cart (keeping the total mass of both carts constant). What is the function that describes this graph? Repeat this for energy efficiency as a function of initial velocity. Can you make the approximation that no energy goes into internal energy of the system (energy efficiency $=1$ )?

Now use your Prediction equation to calculate the final velocity (with uncertainty) of each cart, in terms of the cart masses, the initial velocity of the moving cart, and the energy efficiency of each collision.

## CONCLUSION

Did your measurement agree with your prediction? Why or why not? Was the collision perfectly elastic in the three different cases? What are the limitations on the accuracy of your measurements and analysis?

What conditions must be met for a system's total momentum to be conserved? Describe how those conditions were or were not met for the system you defined in this experiment. What conditions must be met for a system's total energy to be conserved? Describe how those conditions were or were not met for the system you defined in this experiment.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

1 If a runner speeds up from $2 \mathrm{~m} / \mathrm{s}$ to $8 \mathrm{~m} / \mathrm{s}$, the runner's momentum increases by a factor of
(a) 64.
(b) 16 .
(c) 8 .
(d) 4 .
(e) 2 .
2. A piece of clay slams into and sticks to an identical piece of clay that is initially at rest. Ignoring friction, what percentage of the initial kinetic energy goes into changing the internal energy of the clay balls?
(a) $0 \%$
(b) $25 \%$
(c) $50 \%$
(d) $75 \%$
(e) There is not enough information to tell.
3. A tennis ball and a lump of clay of equal mass are thrown with equal speeds directly against a brick wall. The lump of clay sticks to the wall and the tennis ball bounces back with onehalf its original speed. Which of the following statements is (are) true about the collisions?
(a) During the collision, the clay ball exerts a larger average force on the wall than the tennis ball.
(b) The tennis ball experiences the largest change in momentum.
(c) The clay ball experiences the largest change in momentum.
(d) Thetennis ball transfers the most energy to the wall.
(e) The clay ball transfers the most energy to the wall.
4. A golf ball is thrown at a bowling ball so that it hits head on and bounces back. Ignorefrictional effects.

a. Just after the collision, which ball has the largest momentum, or are their momenta the same? Explain using vector diagrams of the momentum before and after the collisions.
b. Just after the collision, which ball has the largest kinetic energy, or are their kinetic energies the same? Explain your reasoning.
5. A 10 kg sled moves at $10 \mathrm{~m} / \mathrm{s}$. A 20 kg sled moving at $2.5 \mathrm{~m} / \mathrm{s}$ has:
(a) 1/4 as much momentum.
(b) 1/2 as much momentum.
(c) twice as much momentum.
(d) four times the momentum.
(e) None of the above.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

6. Two cars of equal mass travel in opposite directions with equal speeds on an icy patch of road. They lose control on the essentially frictionless surface, have a head-on collision, and bounce apart.

a. Just after the collision, the velocities of the cars are:
(a) zero.
(b) equal to their original velocities.
(c) equal in magnitude and opposite in direction to their original velocities.
(d) less in magnitude and in the same direction as their original velocities.
(e) less in magnitude and opposite in direction to their original velocities.
b. In the type of collision described above, consider the system to consist of both cars. Which of the following can be said about the collision?
(a) The kinetic energy of the system does not change.
(b) The momentum of the system does not change.
(c) Both momentum and kinetic energy of the system do not change.
(d) Neither momentum nor kinetic energy of the system change.
(e) The extent to which momentum and kinetic energy of the system do not change depends on the coefficient of restitution.
7. Ignoring friction and other external forces, which of the following statements is (are) true just after an arrow is shot from a bow?
(a) The forward momentum of the arrow equals that backward momentum of the bow.
(b) The total momentum of the bow and arrow is zero.
(c) The forward speed of the arrow equals the backward speed of the bow.
(d) Thetotal velocity of the bow and arrow is zero.
(e) The kinetic energy of the bow is the same as the kinetic energy of the arrow.

## $\square$ CHECK YOUR UNDERSTANDING

$\qquad$

## PHYSICS 1301 LABORATORY REPORT

Laboratory V

Name and ID \#: $\qquad$
D ate performed: $\qquad$ D ay/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :---: |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |

## PROBLEM REPORT:

## ORGANIZATION

(clear and readable; logical progression from problem statement through conclusions; pictures provided where necessary; correct grammar and spelling; section headings provided; physics stated correctly)

DATA AND DATA TABLES
(clear and readable; units and assigned uncertainties clearly stated)
RESULTS
(results clearly indicated; correct, logical, and well-organized calculations with uncertainties indicated; scales, labels and uncertainties on graphs; physics stated correctly)

CONCLUSIONS
(comparison to prediction \& theory discussed with physics stated correctly ; possible sources of uncertainties identified; attention called to experimental problems)

TOTAL (incorrect or missing statement of physics will result in a maximum of $60 \%$ of the total points achieved; incorrect grammar or spelling will result in a maximum of $70 \%$ of the total points achieved)

BONUS POINTS FOR TEAMWORK
(as specified by course policy)

* An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORY VI ROTATIONAL DYNAMICS

So far this semester, you have been asked to think of objects as point particles rather than extended bodies. This assumption is useful and sometimes good enough. However, the approximation of extended bodies as point particles gives an incomplete picture of the real world.

Now we begin a more realistic description of the motion and interactions of objects. Real objects usually rotate as well as move al ong trajectories. You already have a lot of experience with rotating objects from your everyday life. Every time you open or close a door, something rotates. Rotating wheels are everywhere. Balls spin when they are thrown. The earth rotates about its axis. Rotations are important whether you are discussing galaxies or subatomic particles.

An object's rotational motion can be described with the kinematic quantities you have already used: position, velocity, acceleration, and time. In these problems, you will explore the connection of these familiar linear kinematic quantities to a more convenient set of quantities for describing rotational kinematics: angle, angular velocity, angular acceleration, and time. Often, the analysis of an interaction requires the use of both linear and rotational kinematics.

## Objectives:

Successfully completing this laboratory should enable you to:

- Uselinear kinematics to predict the outcome of a rotational system.
- Choose a useful system when using rotational kinematics.
- Identify links between linear and rotational motion.
- Decide when rotational kinematics is more useful and when it is a not.
- Use both linear and rotational kinematics as a means of describing the behavior of systems.


## Preparation:

Read Paul M. Fishbane: Chapter 9, Section 9-1; Chapter 5, Section 5-4. You should also be able to:

- Analyze the motion of an object using linear kinematics and video analysis.
- Identify the connection between the linear description of motion and rotational description of motion
- Calculate the angle of rotation in radians.
- Calculate the angular speed of a rotating object.
- Calculate the angular acceleration of a rotating object.


## PROBLEM \#1:

## ANGULAR SPEED AND LINEAR SPEED

You are working with an engineering group testing equipment that might be used on a satellite. To equalize the heat load from the sun, the satellite will spin about its center. Y our task is to determine the forces exerted on delicate measuring equipment when the satellite spins at a constant angular speed. You know that since any object traveling in a circular path must have exerted on it a non-zero net force, that object must be accelerating. As a first step in finding the net force, you decide to cal culate the linear speed of any object in the satellite as a function of its distance from the center of the satellite and the satellite's angular speed. From the linear speed of the object in circular motion, you calculate its acceleration. You will test your calculations in a laboratory on earth, before launching the satellite.

## EQUIPMENT

You will use an apparatus that spins a horizontal beam on an Aframe base A top view of the device is shown to the right. You will also have a meter stick, a stopwatch, and the video analysis equipment.


What are you trying to calculate? Restate the problem to clearly identify your objective. Illustrate


Read: Fishbane Chapter 5, section 5.4 and Chapter 9, section 9.1.
The following questions will help you to reach your prediction and the analysis of your data.

1. Draw the trajectory of a point on a beam rotating. Choose a coordinate system. Choose a point on that trajectory that is not on a coordinate axis. Draw vectors representing the position, velocity, and acceleration of that point.
2. Write equations for each component of the position vector, as a function of the distance of the point from the axis of rotation and the angle the vector makes with an axis of your coordinate system. Next, calculate how that angle depends on time and the constant angular speed of the beam. Sketch three graphs, (one for each of these equations) as a
function of time. Explain why one of the graphs increases monotonically with time, but the other two oscillate.
3. Using your equations for components of the position of the point, calculate an equation for each component of the velocity of the point. Graph these two equations as a function of time. Compare these graphs to those for the components of the position of the object (when one component of the position is at a maximum, for example, is the same component of the velocity at a maximum value?) Draw these components at the point you have chosen in your drawing; verify that their vector sum gives the correct direction for the velocity of the point.
4. Use your equations for the point's velocity components to calculate its speed. Does the speed change with time? Should it?
5. Use the equations for the point's velocity components to calculate an equation for each component of the point's acceleration. Graph these two equations as functions of time, and compare to the velocity and position graphs. Verify that the vector sum of the components gives the correct direction for the acceleration of the point you have chosen in your drawing. Use the acceleration components to calculate the magnitude of the acceleration.
6. For comparison, write down the expression for the acceleration of the point as a function of its speed and its distance from the axis of rotation.


Practice spinning the beam at different angular speeds. How many rotations does the beam make before it slows down appreciably? Select a range of angular speeds to use in your measurements.

Move the apparatus to the floor and adjust the camera tripod so that the camera is directly above the middle of the spinning beam. Make sure the beam is level. Practice taking some videos. Find the best distance and angle for your video. How will you make sure that you always measure the same position on the beam?

Plan how you will measure the perpendicular components of the velocity to calculate the speed of the point. How will you also use your video to measure the angular speed of the beam?

## Measurement

Take a video of the spinning beam. Be sure you have more than two complete revolution of the beam. For best results, use the beam itself when calibrating your video.

Determine the time it takes for the beam to make two complete revolutions and the distance between the point of interest and the axis of rotation. Set the scale of your axes appropriately so you can see the data as it is digitized.

Decide how many different points you will measure to test your prediction. How will you ensure that the angular speed is the samefor all of these measurements?

How many times will you repeat these measurements using different angular speeds?


A nalyze your video by following a single point on the beam for at least two complete revolutions. Use the velocity components to determine the direction of the velocity vector. Is it in the expected direction?

A nalyze enough different points in the same video to make a graph of speed of a point as a function of distance from the axis of rotation. What quantity does the slope of this graph represent?

Calculate the acceleration of each point and graph the acceleration as a function of the distance from the axis of rotation. What quantity does the slope of this graph represent?

## Conclusions

How do your results compare to your predictions and the answers to the warm up questions? Did the measured acceleration match the acceleration predicted by your equation from Warm up question 5 ? Question 6? Explain.

Was the measured linear speed of each point on the beam a constant? Demonstrate this in terms of your fit equations for velocity.

## PROBLEM \#2: <br> ROTATION AND LINEAR MOTION AT <br> CONSTANT SPEED

While hel ping a friend take apart a lawn mower engine, you notice the pull cord wraps around a heavy, solid disk, "a flywheel," and that disk is attached to a shaft. You know that the flywheel must have at least a minimum angular speed to start the engine. Intrigued by this setup, you wonder how the angular speed of the flywheel is related to the speed of the handle at the end of the pull cord, and you make a prediction. To test your prediction, you make a laboratory model so that you can measure the speed of the cord, the speed of the point on theflywheel where the cord is attached, and the angular speed of the flywheel.


You will have a disk mounted horizontally on a sturdy stand, with a ring coaxially fastened on the disk. Together, the disk and the ring represent the flywheel. The disk and the ring rotatefreely about a vertical shaft through their center.

You will attach one end of a string to the outside surface of the ring, so that it can wrap around the ring. The other end of the string will be connected to a cart that can move along a level track. You also have a stopwatch, a meter stick, an end stop, some wooden blocks and the video analysis equipment.


Restate the problem. What are you trying to calculate? Which experimental parameters will be determi ned by the laboratory equipment, and which ones will you control?

## Warm UP

Read: Fishbane Chapter 5, section 5.4 and Chapter 9, section 9.1.
Thefollowing questions will help you to reach your prediction.

1. Draw a top view of the system. Draw the velocity and acceleration vectors of a point on the outside edge of the ring. Draw a vector representing the angular velocity of the ring. Draw the velocity and acceleration vectors of a point along the string. Draw the velocity and acceleration vectors of the cart. Write an equation for the relationship between the linear velocity of the point where the string is attached to the ring and the velocity of the cart (if the string is taut).
2. Choose a coordinate system useful for describing the motion of the point where the string is attached to the ring. Select a point on the outside edge of the ring. Write equations for the perpendicular components of the position vector as a function of the distance from the axis of rotation and the angle the vector makes with one axis of your coordinate system. Calculate how that angle depends on time and the constant angular speed of the ring. Sketch three graphs, (one for each of these equations) as a function of time.
3. Using your equations for the components of the position of the point, determineequations for the components of the velocity of the point. Graph these equations as a function of time. Compare these graphs to those representing the components of the position of the object.
4. Use your equations for the components of the vel ocity of the point to cal culate its speed. Is the speed a function of time or is it constant?
5. Now write an equation for the cart's speed as a function of time, assuming the string is taut.

## EXPLORATION

Try to make the cart move along the track with a constant velocity. (To account for friction, you may need to slant the track slightly. You might even use somequick video analysis to get this right.) Do this before you attach the string.

Try two different ways of having the string and the cart move with the same constant velocity so that the string remains taut. Try various speeds and pick the way that works most consistently for you. If the string goes slack during the measurement you must redo it.
(1) Gently push the cart and let it go so that the string unwinds from the ring at a constant speed.
(2) Gently spin the disk and let it go so that the string winds up on the ring at a constant speed.

Where will you place the camera to give the best recording looking down on the system? You will need to get data points for both the motion of the ring and the cart. Try sometest runs.

Decide what measurements you need to make to determine the speed of the outer edge of the ring and the speed of the string from the same video.

Outline your measurement plan.

## Measurement

Make a video of the motion of the cart and the ring for several revolutions of the ring. Measure the radius of the ring. What are the uncertainties in your measurements? (See A ppendices $A$ and $B$ if you need to review how to determine significant figures and uncertainties.)

A nalyze your video to determine the velocity of the cart and, because the string was taut throughout the measurement, the velocity of the string. Use your measurement of the distance the cart goes and the time of the motion to choose the scale of the computer graphs so that the data is visible when you take it. If the velocity was not constant, adjust your equipment and repeat the measurement.

A nalyze the same video to determine the velocity components of the edge of the ring. Use your measurement of the diameter of the ring and the time of the motion to choose the scale of the computer graphs so that the data is visible when you take it.

In addition to finding the angular speed of the ring from the speed of the edge and the radius of the ring, also determine the angular speed directly (using its definition) from either position component of the edge of the ring versus timegraph.

## Analysis

Use an analysis technique that makes the most efficient use of your data and your time.
Compare the measured speed of the edge of the ring with the measured speed of the cart and thus the string. Calculate the angular speed of the ring from the measured speed of the edge of the ring and the distance of the edge of the ring from the axis of rotation. Compare that to the angular speed measured directly.

## Conclusions

Did your measurements agree with your initial prediction? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

Explain why it is difficult to keep the string taut in this measurement, by considering the forces exerted on each end of the string? Determine the force of the string on the cart and the force of the cart on the string. Determine the force of the string on the ring and the force of the ring on the string. What is the string tension?

## PROBLEM \#3:

ANGULAR AND LINEAR ACCELERATION

You are working in a bioengineering laboratory when the building power fails. An ongoing experiment will be damaged if there is any temperature change. There is a gasoline powered generator on the roof for just such emergencies. You run upstairs and start the generator by pulling on a cord attached to a flywheel. It is such hard work that you begin to design a gravitational powered generator starter. The generator you design has its flywheel as a horizontal disk that is free to rotate about its center. One end of a rope is wound up on a horizontal ring attached to the center of the flywheel. The free end of the rope goes horizontally to the edge of the building roof, passes over a vertical pulley, and then hangs straight down. A heavy block is attached to the hanging end of the rope. When the power fails, the block is released, the rope unrolls from the ring giving theflywheel a large enough angular acceleration to start the generator. To see if this design is feasible you must determine the relationship between the angular acceleration of the flywheel, the downward acceleration of the block, and the radius of the ring. Before putting more effort in the design, you test your idea by building a laboratory model of the device.


## DISK



You will have a disk mounted horizontally on a sturdy stand. The disk represents the flywheel and is free to rotate about a vertical shaft through its center. You will attach the string to a spool under the center of the disk, in place of the ring in your flywheel design. A string has one end wrapped around the horizontal spool. The other end of the string passes over a vertical pulley lined up with the tangent to the spool. An object (a mass hanger) is hung from the free end of the string so that it can fall past the table. Y ou also have a stopwatch, a meter stick, a pulley clamp, a mass set, a mass hanger and the video analysis equipment.

## Prediction

Reformulate the problem in your own words to understand its target. What do you need to calculate?

## Warm UP

Read: Fishbane Chapter 5, section 5.4 and Chapter 9, section 9.1.
Thefollowing questions are designed to help you solve the problem in an organized way.

1. Draw a top view of the system. Draw the velocity and acceleration vectors of a point on the outside edge of the spool. Draw a vector representing the angular acceleration of the spool. Draw the velocity and acceleration vectors of a point along the string.
2. Draw a side view of the system. Draw the velocity and acceleration vectors of the hanging object. What is the relationship between the linear acceleration of the string and the acceleration of the hanging object if the string is taut? Do you expect the acceleration of the hanging object to be constant? Explain.
3. Choose a coordinate system useful to describe the motion of the spool. Select a point on the outside edge of the spool. Write equations giving the perpendicular components of the point's position vector as a function of the distance from the axis of rotation and the angle the vector makes with one axis of your coordinate system. A ssume the angular acceleration is constant and that the disk starts from rest. Determine how the angle between the position vector and the coordinate axis depends on time and the angular acceleration of the spool. Sketch three graphs, (onefor each of these equations) as a function of time.
4. Using your equations for components of the position of the point, calculate the equations for the components of the velocity of the point. Is the speed of this point a function of time or is it constant? Graph these equations as a function of time.
5. Use your equations for the components of the velocity of the point on the edge of the spool to calculate the components of the acceleration of that point. From the components of the acceleration, calculate the square of the total acceleration of that point. It looks like a mess but it can be simplified to two terms if you can use: $\sin ^{2}(z)+\cos ^{2}(z)=1$.
6. From step 5, the magnitude acceleration of the point on the edge of the spool has one term that depends on time and another term that does not. Identify the term that depends on time by using the relationship between the angular speed and the angular acceleration for a constant angular acceleration. If you still don't recognize this term, use the relationship among angular speed, linear speed and distance from the axis of rotation. Now identify the relationship between this time-dependent term and the centripetal acceleration.
7. We also can solve the acceleration vector of the point on the edge of the spool into two perpendicular components by another way. One component is the centripetal acceleration and the other component is the tangential acceleration. In step 6, we already identify the
centripetal acceleration term from the total acceleration. So now you can recognize the tangential acceleration term. How is the tangential acceleration of the edge of the spool related to the angular acceleration of the spool and the radius of the spool? What is the relationship between the angular acceleration of the spool and the angular acceleration of thedisk?
8. How is the tangential acceleration of the edge of the spool related to the acceleration of the string? How is the acceleration of the string related to the acceleration of the hanging object? Explain the relationship between the angular acceleration of the dsk and the acceleration of the hanging object.
9. Use the simulation "Lab7Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore connections among graphs of angle, angular velocity, and angular acceleration for the flywhel; position, velocity, and acceleration for the hanging object; and position components of a point on the ring and the velocity components,. A djust the sizes and masses of the objects to get clear graphs for at least two rotations of the disk. You may need to adjust the axis limits for the graphs, and redraw them several times.

## Exploration

Practice gently spinning the spool/ disk system by hand. How long does it take the disk to stop rotating about its central axis? What is the average angular acceleration caused by this friction? Make sure the angular acceleration you use in your measurements is much larger than the one caused by friction so that it has a negligible effect on your results.

Find the best way to attach the string to the spool. How much string should you wrap around the spool? How should the pulley be adjusted to allow the string to unwind smoothly from the spool and pass over the pulley? Practice releasing the hanging object and the spool/ disk system.

Determine the best mass to use for the hanging object. Try a large range. What mass will give you the smoothest motion? What is the highest angular acceleration? How many useful frames for a single video?

Where will you place the camera to give the best top view recording on the whole system? Try sometest runs. Since you can't get a video of the falling object and the top of the spinning spool/ disk at the same time, attach a piece of tape to the string. The tape will show up in the video and will have the same linear motion as the falling object.

Decide what measurements you need to make to determine the angular acceleration of the disk and the acceleration of the string from the same video.

Outline your measurement plan.

## MeAsurement

Make a video of the motion of the tape on the string and the disk for several revolutions. Measure the radius of the spool. What are the uncertainties in your measurements?

Digitize your video to determine the acceleration of the string and, because the string was taut throughout the measurement, the acceleration of the hanging object. Use your measurement of the distance and time that the hanging object falls to choose the scale of the computer graphs so that the data is visible when you take it. Check to see if the acceleration is constant.

Use a stopwatch and meter stick to directly determine the acceleration of the hanging object.
Digitize the same video to determine the velocity components of the edge of the disk. Use your measurement of the diameter of the disk and the time of the motion to choose the scale of the computer graphs so that the data is visible when you take it.


From an analysis of the video data for the tape on the string, determine the acceleration of the piece of tape on the string. Compare this acceleration to the hanging object's acceleration determined directly. Be sure to use an analysis technique that makes the most efficient use of your data and your time.

From your video data for the disk, determine if the angular speed of the disk is constant or changes with time.

Use the equations that describe the measured components of the velocity of a point at the edge of the disk to cal culate the tangential acceleration of that point and use this tangential acceleration of the edge of the disk to calculate the angular acceleration of the disk (it is also the angular acceleration of spool). You can refer to the Warm up questions.

## Conclusion

Did your measurements agree with your initial prediction? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

Explain why it is not difficult to keep the string taut in this measurement by considering the forces exerted on each end of the string? Determine the pull of the string on the hanging object and the pull of the hanging object on the string, in terms of the acceleration of the hanging object. Determinetheforce of the string on the spool and the force of the spool on the string. What is the string tension? Is it equal to, greater than, or less than the weight of the hanging object?

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

1. The direction of angular velocity for the wheel spinning as shown is:
(a) Clockwise.
(b) Counterclockwise.
(c) Into the page.
(d) Out of the page.
(e) Down.

2. The wheel in question 1 is slowing down. The direction of its angular acceleration is:
(a) Clockwise.
(b) Counterclockwise.
(c) Into the page
(d) Out of the page.
(e) Down.
3. An object in circular motion has a constant angular velocity ? and is moving as shown. The object is at position $x=+A, y=0$ at time $t=0$. The $y$ component of the object's acceleration is given by:
(a) $A ?^{2} \cos (? \mathrm{t})$.
(b) $-A ?^{2} \sin (? \mathrm{t})$.
(c) $A ?^{2}$.
(d) $A ? \cos (? t)$.
(e) $-A ? \sin (? t)$.

4. If an object is in circular motion, its
(a) Velocity is proportional to its displacement.
(b) A cceleration is proportional to its displacement.
(c) Both a and b.
(d) Neither a nor b.

The graph represents the $x$-component of the position of an object in circular motion.


## $\square$ CHECK YOUR UNDERSTANDING

5. Which graph below is the $x$ component of thevelocity-versus-time graph for the object?

(e) None of the above.
6. Which graph below is they component of the velocity-versus-timegraph for the object in question 5 ?

(e) None of the above.

## $\square$ CHECK YOUR UNDERSTANDING

$\qquad$

# PHYSICS 1301 LABORATORY REPORT <br> Laboratory VI 

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readable; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATA AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well--rganized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL (incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total <br> points achieved) |  |
| BONUS POINTS FOR TEAMWORK <br> (as specified by course policy) |  |

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## LABORATORY VII ROTATIONAL DYNAMICS

Describing rotations requires applying the physics concepts you have already been studying - position, velocity, acceleration, force, mass, kinetic energy, and momentum to objects that can rotate. However, as we have seen, a modified set of kinematic quantities is sometimes easier to apply to objects with a definite shape angle, angular velocity, and angular acceleration. To more closely investigate the interactions of these objects, it is also useful to define a modified set of dynamic quantities - torque, moment of inertia (or rotational inertia), rotational kinetic energy, and angular momentum.

In this laboratory, you will analyze and predict the motion of extended objects and describe the behavior of structures that are stationary. For static structures, you will apply the concept of torque and the concept of force. To predict motions of objects when torques are applied to them, you will calculate moments of inertia. To compare the motions of objects before and after interactions with each other, you will apply the principle of conservation of energy, including terms for rotational kinetic energy, and you will use a new conservation theory: the conservation of angular momentum.

## Objectives:

After successfully completing this laboratory, you should be ableto:

- Use the concept of torque for a system that is in static equilibrium.
- Relate the concepts of torque, angular acceleration and moment of inertia for rigid bodies.
- Use the conservation principles of energy, momentum, and angular momentum for rigid body motion.


## Preparation:

Read Paul M. Fishbane: Chapter 9, sections 9-2 to 9-6; Chapter 10.

Before coming to lab you should be able to:

- Determine the net force on an object from its acceleration.
- Know when to use mass and when to use moment of inertia to determine the motion of objects.
- Determine the net torque on an object from its angular acceleration.
- Draw and use force and torque diagrams.
- Explain what is meant by a system in "equilibrium."
- Know how to determine the period of rotation of an object.


## PROBLEM \#1:

## M OMENT OF INERTIA OF A COM PLEX SYSTEM

While examining the engine of your friend'ssnow blower you notice that the starter cord wraps around a cylindrical ring. This ring is fastened to the top of a heavy, solid disk, "a flywheel," and that disk is attached to a shaft. You are intrigued by this configuration and decide to determine its moment of inertia. Your friend thinks you can add the moment of inertial by parts to get the moment of inertia of the system. To test this idea you decide to build a laboratory model described below to determine the moment of inertia of a similar system from the acceleration of the hanging weight.

## EQUIPMENT

For this problem you will have a disk, which is mounted on a sturdy stand by a metal shaft. Below the disk there is a metal spool on the shaft to wind string around. A ring sits on the disk so both ring and disk share the same rotational axis. A length of string is wrapped around the spool and then passes over a pulley lined up with the tangent to the spool. A weight is hung from the other end of the string so that the weight can fall past the edge of the table.


As the hanging weight falls, the string pulls on the spool, causing the ring/ disk/ shaft/ spool system to rotate. You will also have a meter stick, a stopwatch, a pulley clamp, a mass hanger, a mass set and the video analysis equipment in this experiment.


Restate your friend's idea as an equation.
What quantities will you measure in the lab? What relationships do you need to calculate in order to test your friend's ideas in the lab?

## Warm UP

Read: Fishbane Chapter 9. Read carefully Sections 9-3 and 9-4 and Example 9-11.
Thefollowing questions will help you figure out the prediction, and find a way to test your friend's idea in the lab. It is hel pful to use a problem-solving strategy such as the one outlined below:

1. Draw a side view of the equipment. Draw the velocity and acceleration vectors of the weight. Add the tangential velocity and tangential acceleration vectors of the outer edge of the spool. Also, show the angular acceleration of the spool. What are the relationships among the acceleration of the string, the acceleration of the weight, and the tangential acceleration of the outer edge of the spool if the string is taut?
2. To relate the moment of inertia of the system to the acceleration of the weight, you need to consider a dynamics approach (Newton's second law) especially considering the torques exerted on the system. The relationships between rotational and linear kinematics will also beinvolved.
3. Draw a free-body diagram for the ring/ disk/ shaft/ spool system. Show the locations of the forces acting on that system. Label all the forces. Does this system accelerate? Is there an angular acceleration? Check to see if you have all the forces on your diagram. Which of these forces can exert a torque on the system? Identify the distance from the axis of rotation to the point where each force is exerted on the system. Write down an equation that gives the torque in terms of the distance and the force that causes it. Write down Newton's second law in its rotational form for this system. Remember that the moment of inertia includes everything in the system that will rotate.
4. Draw a free-body diagram for the hanging weight. Label all the forces acting on it. Does this weight accelerate? Is there an angular acceleration? Check to see if you have included all the forces on your diagram. Write down Newton's second law for the hanging weight. Is the force of the string on the hanging weight equal to the weight of the hanging weight?
5. Can you use Newton's third law to relate pairs of forces shown in different force diagrams?
6. Is there a relationship between the angular acceleration of the ring/ disk/ shaft/ spool system and the acceleration of the hanging weight? To decide, examine the accelerations that you labeled in your drawing of the equipment.
7. Solve your equations for the moment of inertia of the ring/ disk/ shaft/ spool system as a function of the mass of the hanging weight, the acceleration of the hanging weight, and the radius of the spool. Start with the equation containing the quantity you want to know, the moment of inertia of the ring/ disk/ shaft/ spool system. Identify the unknowns in that equation and select equations for each of them from those you have collected. If those equations generate additional unknowns, search your collection for equations that contain them. Continue this process until all unknowns are accounted for. Now solve those equations for your target unknown.
8. For comparison with your experimental results, calculate the moment of inertia of the ring/ disk/ shaft/ spool system using your friend's idea.
9. Use the simulation "Lab7Sim" (See Appendix F for a brief explanation of how to use the simulations) to explore the effects of varying the moment of inertia of the system and the mass of
the hanging object. N ote that in the simulation, the string acts as if it were attached to the outer edge of the disk. Use the simulation to test your "lab measurement" prediction equation. In making your "lab measurement" prediction, you made several assumptions. Use the parameters in the simulation to (a) think about what some of those assumptions were (for instance, did you notice that you made an assumption about the mass of the pulley?) and (b) test the effects of violating those assumptions.

## EXPLORATION

Practice gently spinning the ring/ disk/ shaft/ spool system by hand. H ow long does it take the disk to stop rotating about its central axis? What is the average angular acceleration caused by this friction? Make sure the angular acceleration you use in your measurements is much larger than the one caused by friction so that it has a negligible effect on your results.

Find the best way to attach the string to the spool. How much string should you wrap around the spool? How should the pulley be adjusted to allow the string to unwind smoothly from the spool and pass over the pulley? Practice releasing the hanging weight and the ring/ disk/ shaft/ spool system.

Determine the best mass to use for the hanging weight. Try a large range. What mass will give you the smoothest motion?

Decide what measurements you need to make to determine the moment of inertia of the system from your Prediction equation. If any major assumptions are involved in connecting your measurements to the acceleration of the weight, decide on the additional measurements that you need to make to justify them.

Outlineyour measurement plan.
Make some rough measurements to make sureyour plan will work.

## Measurement

Follow your measurement plan. What are the uncertainties in your measurements? (See A ppendices A and B if you need to review how to determine significant figures and uncertainties.)

Don't forget to make the additional measurements required to determine the moment of inertia of the ring/ disk/ shaft/ spool system from the sum of the moments of inertia of its components. What is the uncertainty in each of the measurements? What effects do the hole, the ball bearings, the groove, and the holes in the edges of the disk have on its moment of inertia? Explain your reasoning.

## Analysis

Determine the acceleration of the hanging weight. How does this acceleration compare to what its acceleration would be if you just dropped the weight without attaching it to the string? Explain whether or not this makes sense.

Using your Prediction equation and your measured acceleration, the radius of the spool and the mass of the hanging weight, calculate the moment of inertia (with uncertainty) of the disk/ shaft/ spool system.

Adding the moments of inertia of the components of the ring/ disk/ shaft/ spool system, calculate the value (with uncertainty) of the moment of inertia of the system. What fraction of the moment of inertia of the system is due to the shaft? Thedisk? Thering? Explain whether or not this makes sense.

Compare the values of moment of inertia of the system from these two methods.

## Conclusion

Did your measurements agree with your initial prediction? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

## PROBLEM \#2:

MOMENTS OFINERTIA ABOUT DIFFERENT AXES

While spinning a coin on a table, you wonder if the coin's moment of inertia spinning on its edge is the same as if it were spinning about an axis through its center and perpendicular to its surface. You do a quick calculation to decide. To test your prediction, you build a laboratory model with a disk that can spin around two different axes, and find the moment of inertia in each configuration by measuring the acceleration of a hanging weight attached to the spinning system by a string.

## EQUIPMENT

You will use the same equipment as in Problem \#1. A disk is mounted above a spool on a sturdy stand by a metal shaft. The disk can be attached to the shaft so it rotates about its central axis or about its diameter, as shown below.


Axis Through Genter
Axis Through Diameter
A length of string is wrapped around the spool and then passes over a pulley lined up with the tangent to the spool. A weight is hung from the other end of the string so that the weight can fall past the edge of the table. As the hanging weight falls, the string pulls on the spool, causing the disk/ shaft/ spool system to rotate. You will also have a meter stick, a stopwatch, a mass hanger, a mass set, a pulley clamp and the video analysis equipment in this experiment.


Restate the problem. What are you asked to predict? What relationships do you need to calculate to use thelab model?

## Warm UP

Read: FishbaneChapter 9. Read carefully Sections 9-3 and 9-4 and Examples 9-5, 9-6 and 9-11.
To figure out your prediction, you need to determine how to calculate the rotational inertia of the disk from the quantities you can measure in the laboratory. It is helpful to use a problem solving strategy such as the one outlined below:

More details for answering these Warm up questions are given in Problem \#1.

1. Draw a side view of the equipment with all relevant kinematic quantities. Write down any relationships that exist between them. Label all the relevant forces.
2. Determine the basic principles of physics that you will use. Write down your assumptions and check to see if they are reasonable.
3. If you decide to use dynamics, draw a freebody diagram of all the relevant objects. Note the acceleration of the object as a check to see if you have drawn all the forces. Write down Newton's second law for each free-body diagram either in its linear form or its rotational form or both as necessary.
4. Use N ewton's third law to relate the forces between two free-body diagrams. If forces are equal give them the same labels.
5. Identify the target quantity you wish to determine. Use the equations collected in steps 1 and 3 to plan a solution for thetarget.
6. For comparison with your experimental results, calculate the moment of inertia of the disk in each orientation.
7. Use the simulation "Lab7Sim" (See A ppendix F for a brief explanation of how to use the simulations) to explore the effects of varying the moment of inertia of the system and the mass of the hanging object. Note that in the simulation, the string acts as if it were attached to the outer edge of the disk. Use the simulation to test your "lab measurement" prediction equation. In making your "lab measurement" prediction, you made several assumptions. Use the parameters in the simulation to (a) think about what some of those assumptions were (for instance, did you notice that you made an assumption about the mass of the pulley?) and (b) test the effects of violating those assumptions.

## Exploration

Practice gently spinning the disk/ shaft/ spool system by hand. How long does it take the disk to stop rotating about its central axis? How long does it take the disk to stop rotating about its diameter? How will friction affect your measurements?

Find the best way to attach the string to the spool. How much string should you wrap around the spool? How much mass will you attach to the other end of the string? How should the pulley be
adjusted to allow the string to unwind smoothly from the spool and pass over the pulley? Practice releasing the hanging weight and the disk/ shaft/ spool system.

Determine the best mass to use for the hanging weight. Try a large range. What mass will give you the smoothest motion?

Decide what measurements you need to make to determine the moment of inertia of the system from your Prediction equation. If any major assumptions are involved in connecting your measurements to the acceleration of the weight, decide on the additional measurements that you need to make to justify them. If you already have this data in your lab journal you don't need to redo it, just copy it.

Outline your measurement plan. Make some rough measurements to makesure your plan will work.

## Measurement

Follow your measurement plan. What are the uncertainties in your measurements? (See A ppendices A and $B$ if you need to review how to determine significant figures and uncertainties.)

Don't forget to make the additional measurements required to determine the moment of inertia of the disk/ shaft/ spool system by adding all of the moments of inertia of its components. What is the uncertainty of each of the measurements? What effects do the hole, the ball bearings, the groove, and the holes in the edges of the disk have on its moment of inertia? Explain your reasoning.

## Analysis

Determine the acceleration of the hanging weight. How does this acceleration compare to its acceleration if you just dropped the weight without attaching it to the string? Explain whether or not this makes sense.

Using your Prediction equation and your measured accel eration, the radius of the spool and the mass of the hanging weight, calculate the moment of inertia (with uncertainty) of the disk/ shaft/ spool system, for both orientations of the disk.

Adding the moments of inertia of the components of the disk/ shaft/ spool system, calculate the value (with uncertainty) of the moment of inertia of the system, for both orientations of the disk. Compare the results from these two methods for both orientations of the disk.

## Conclusion

How do the measured and predicted values of the disk's moment of inertia compare when the disk rotates about its central axis? When the disk rotates around its diameter?

Is the moment of inertia of a coin rotating around its central axis larger than, smaller than, or the same as its moment of inertia when it is rotating around its diameter? State your results in the most general terms supported by the data.

Did your measurements agree with your initial predictions? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

## PROBLEM \#3:

## MOMENT OF INERTIA WITH AN OFF-AXIS RING

You have been hired as a member of a team designing an energy efficient car. The brakes of a traditional car transform the kinetic energy of the car into internal energy of the brake material, resulting in an increased temperature of the brakes. That energy is lost in the sense that it cannot be recovered to power the car. Your task has been to evaluate a new braking system, which transforms the kinetic energy of the car into rotational energy of a flywheel system. The energy of the flywheel can then be used to drive the car. As designed, the flywheel consists of a heavy horizontal disk with an axis of rotation through its center. A metal ring is mounted on the disk but is not centered on the disk. You wonder what effect the off-center ring will have on the motion of theflywheel.

To answer this question, you decide to make a laboratory model to measure the moment of inertia of a ring/ disk/ shaft/ spool system when the ring is off-axis and compare it to the moment of inertia for a system with a ring in the center.


The equipment is the same as Problem \#1 and \#2.


Restate the problem. What are you asked to predict? What relationships do you need to calculate to use the lab model?

## Warm UP

Read: FishbaneChapter 9. Read carefully Sections 9-3 and 9-4 and Examples 9-7, 9-8 and 9-11.
To figure out your prediction, you need to determine how to calculate the rotational inertia of the disk from the quantities you can measure in this problem. It is helpful to use a problem solving strategy such as the one outlined below:

More details for answering these Warm up questions are given in Problem \#1.

1. Draw a side view of the equipment with all the relevant kinematics quantities. Write down any relationships that exist between them. Label all the relevant forces.
2. Determine the basic principles of physics that you will use. Write down your assumptions and check to see if they are reasonable.
3. If you decide to use dynamics, draw a freebody diagram of all the relevant objects. Note the acceleration of the object as a check to see if you have drawn all the forces. Write down Newton's second law for each free-body diagram either in its linear form or its rotational form or both as necessary.
4. Use N ewton's third law to relate the forces between two freebody diagrams. If forces are equal give them the same labels.
5. Identify the target quantity you wish to determine. Use the equations collected in steps 1 and 3 to plan a solution for the target. If there are more unknowns than equations, reexamine the previous steps to see if there is additional information about the situation. If not, see if one of the unknowns will cancel out.
6. For comparison with your experimental results, calculate the moment of inertia of the disk/ ring system in each configuration. The parallel-axis theorem should behelpful.

## Exploration

THE OFF-AXIS RING IS NOT STABLE BY ITSELF! Be sure to secure the ring to the disk, and be sure that the system is on a stable base.

Practice gently spinning the ring/ disk/ shaft/ spool system by hand. How will friction affect your measurements?

Find the best way to attach the string to the spool. How much string should you wrap around the spool? How much mass will you attach to the other end of the string? How should the pulley be adjusted to allow the string to unwind smoothly from the spool and pass over the pulley? Practice releasing the mass and the ring/ disk/ shaft/ spool system.

Determine the best mass to use for the hanging weight. Try a large range. What mass will give you the smoothest motion?

Decide what measurements you need to make to determine the moment of inertia of the system from your Prediction equation. If any major assumptions are involved in connecting your measurements to the acceleration of the weight, decide on the additional measurements that you need to make to justify them.

Outlineyour measurement plan. Make some rough measurements to make sure your plan will work.

## Measurement

Follow your measurement plan. What are the uncertainties in your measurements? (See Appendices A and B if you need to review how to determine significant figures and uncertainties.)

Don't forget to make the additional measurements required to determine the moment of inertia of the ring/ disk/ shaft/ spool system from the moments of inertia of its components and the parallel axis theorem. What is the uncertainty in each of the measurements? What effects do the hole, the ball bearings, the groove, and the holes in the edges of the disk have on its moment of inertia? Explain your reasoning.

## Analysis

Determine the acceleration of the hanging weight. How does this acceleration compare to its acceleration if you just dropped the weight without attaching it to the string? Explain whether or not this makes sense.

Using your Prediction equation and your measured acceleration, the mass of the hanging weight and the radius of the spool, calculate the moment of inertia (with uncertainty) of the disk/ shaft/ spool system.

Adding the moments of inertia of the components of the disk/ shaft/ spool system and applying the parallel axis theorem, calculate the value (with uncertainty) of the moment of inertia of the system.

## Conclusion

Compare the two values for the moment of inertia of the system when the ring is off-axis. Did your measurement agree with your predicted value? Why or why not?

Compare the moments of inertia of the system when the ring is centered on the disk, and when the ring is off-axis.

What effect does the off-center ring have on the moment of inertia of the ring/ disk/ shaft/ spool system? Does the rotational inertia increase, decrease, or stay the same when the ring is moved off-axis?

State your result in the most general terms supported by your analysis. Did your measurements agree with your initial prediction? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

## PROBLEM \#4: <br> FORCES, TORQUES, AND ENERGY

While examining the manual starter on a snow blower, you wonder why the manufacturer chose to wrap the starter cord around a smaller ring that is fastened to a spool under the flywheel instead of around the flywheel itself. When starting asnow blower, you know you need the starter system to spin as fast as possible when you pull the starter cord. Your friend suggests that the flywheel might spin faster, even if you do the same amount of work when you pull on the handle, if the cord is wrapped around a smaller diameter. You notice that the handle is not very light. To see whether this idea is correct, you decide to calculate the final angular speed of the flywheel after pulling on the handle for a fixed distance with afixed force, as a function of thespool's radius. To test your calculation, you set up a laboratory model of the flywheel starter assembly. Unfortunately, it is difficult to keep the force on the handle consistent across trials, so in the lab you attach a hanging mass to one end of the cord.


You will use the same equipment as in Problem \#1. A length of string can be fastened and wrapped around the ring, the disk or the spool.


As the hanging weight falls, the string causes the ring/ disk/ shaft/ spool system to rotate.
You will also have a stopwatch, a meter stick, a mass hanger, a mass set, a pulley clamp and the video analysis equipment.

## Prediction

Restate the problem. What quantities do you need to cal culate to test your idea?

## Warm UP

Read: FishbaneChapter 9. Read carefully Sections 9-2 and 9-4.
To figureout your prediction, it is useful to use a problem-solving strategy such as the one outlined below:

1. Make two side view drawings of the situation (similar to the diagram in the Equipment section), one just as the hanging mass is released, and one just as the hanging mass reaches the ground (but before it hits). Label all relevant kinematic quantities and write down the relationships that exist between them. What is the relationship between the velocity of the hanging weight and the angular velocity of the ring/ disk/ shaft/ spool system? Label all the relevant forces.
2. Determine the basic principles of physics that you will use and how you will use them. Determine your system. Are any objects from outside your system interacting with your system? Write down your assumptions and check to see if they are reasonable. How will you ensure that your equipment always pulls the cord through the same length when it is wrapped around different diameters?
3. Use dynamics to determine what you must do to the hanging weight to get the force for each diameter around which the cord is wrapped. Draw a free-body diagram of all relevant objects. N ote the acceleration of the object in the free-body diagram as a check to see if you have drawn all the forces. Write down Newton's second law for each free-body diagram either in its linear form or its rotational form or both as necessary. Use Newton's third law to relate the forces between two free-body diagrams. If forces are equal, give them the same symbol. Solve your equations for the force that the string exerts.
4. Use the conservation of energy to determine the final angular speed of the rotating objects. Define your system and write the conservation of energy equation for this situation:

What is the energy of the system as the hanging weight is released? What is its energy just beforethe hanging weight hits the floor? Is any significant energy transferred to or from the system? If so, can you determine it or redefine your system so that there is no transfer? Is any significant energy changed into internal energy of the system? If so, can you determine it or redefine your system so that there is no internal energy change?
5. Identify the target quantity you wish to determine. Use the equations collected in steps 1,3 , and 4 to plan a solution for the target. If there are more unknowns than equations, reexamine the previous steps to see if there is additional information about the situation that can be expressed in an addition equation. If not, see if one of the unknowns will cancel out.


Practice gently spinning the ring/ disk/ shaft/ spool system by hand. How will friction affect your measurements?

Find the best way to attach the string to the spool, disk, or ring. How much string should you wrap around each? H ow should the pulley be adjusted to allow the string to unwind smoothly and pass over the pulley in each case? Y ou may need to reposition the pulley when changing the position where the cord wraps. Practice releasing the weight and thering/ disk/ shaft/ spool system for each case.

Determine the best mass to use for the hanging weight. Remember this mass will be applied in every case. Try a large range. What mass range will give you the smoothest motion?

Is the time it takes the hanging weight to fall different for the different situations? How will you determine the time taken for it to fall? Determine a good setup for each case (string wrapped around the ring, the disk, or the spool).

Decide what measurements you need to make to check your prediction. If any major assumptions are used in your cal culations, decide on the additional measurements that you need to make to justify them. If you already have this data in your lab journal you don't need to redo it, just copy it.

Outline your measurement plan. Make some rough measurements to be sure your plan will work.

## Measurement

Follow your measurement plan. What are the uncertainties in your measurements?

## Analysis

Determine the final angular velocity of the ring/ disk/ shaft/ spool system for each case after the weight hits the ground. How is this angular velocity related to the final velocity of the hanging weight? If your calculation incorporates any assumptions, make sure you justify these assumptions based on data that you have analyzed.

## Conclusion

In each case, how do your measured and predicted values for the final angular velocity of the system compare?

Of the three places you attached the string, which produced the highest final angular velocity? Did your measurements agree with your initial prediction? Why or why not? What are the limitations on the accuracy of your measurements?

Given your results, how much does it matter where the starter cord is attached? Why do you think the manufacturer chose to wrap the cord around thering? Explain your answers.

Can you make a qualitative argument, in terms of energy conservation, to support your conclusions?

## PROBLEM \#5: <br> CONSERVATION OFANGULAR MOMENTUM

While driving around the city, your car is constantly shifting gears. You wonder how the gear shifting process works. Y our friend tells you that there are gears in the transmission of your car that are rotating about the same axis. When the car shifts, one of these gear assemblies is brought into connection with another one that drives the car's wheels. Thinking about a car starting up, you decide to cal culate how the angular speed of a spinning object changes when it is brought into contact with another object at rest. To keep your calculation simple, you decide to use a disk for the initially spinning object and a ring for the object initially at rest. Both objects will be able to rotate freely about the same axis, which is centered on both objects. To test your calculation you decide to build a laboratory model of the situation.


You will use the same basic equipment in the previ ous problems.


## Prediction

Restate the problem. What quantities do you need to calculate to test your idea?

## Warm up

Read: FishbaneChapter 9. Read carefully Sections 9-4 and 9-5 and Examples 9-11 and 9-13.

To figure out your prediction, it is useful to use a problem solving strategy such as the one outlined below:

1. Make two side view drawings of the situation (similar to the diagram in the Equipment section), one just as the ring is released, and one after the ring lands on the disk. Label all relevant kinematic quantities and write down the relationships that exist between them. Label all relevant forces.
2. Determine the basic principles of physics that you will use and how you will use them. Determine your system. Are any objects from outside your system interacting with your system? Write down your assumptions and check to see if they are reasonable.
3. Use conservation of angular momentum to determine the final angular speed of the rotating objects. Why not use conservation of energy or conservation of momentum? Define your system and write the conservation of angular momentum equation for this situation:

Is any significant angular momentum transferred to or from the system? If so, can you determine it or redefineyour system so that there is no transfer?
4. Identify the target quantity you wish to determine. Use the equations collected in steps 1 and 3 to plan a solution for the target. If there are more unknowns than equations, reexamine the previous steps to see if there is additional information about the situation that can be expressed in an addition equation. If not, see if one of the unknowns will cancel out.

## Exploration

Practice dropping the ring into the groove on the disk as gently as possible to ensure the best data. What happens if the ring is dropped off-center? What happens if the disk does not fall smoothly into the groove? Explain your answers.

Decide what measurements you need to make to check your prediction. If any major assumptions are used in your calculations, decide on the additional measurements that you need to make to justify them.

Outline your measurement plan.
Make some rough measurements to be sure your plan will work.

## MeAsurements

Follow your measurement plan. What are the uncertainties in your measurements?


Determine the initial and final angular velocity of the disk from the data you collected. Using your prediction equation and your measured initial angular velocity, calculate the final angular velocity of
the disk. If your calculation incorporates any assumptions, make sure you justify these assumptions based on data that you have analyzed.


Did your measurement of the final angular velocity agree with your calculated value by prediction? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

Could you have easily measured enough information to useconservation of energy to predict the final angular velocity of this system? Why or why not? Use your data to check your answer.

## PROBLEM \#6:

DESIGNING A MOBILE

Your friend has asked you to help make a mobilefor her daughter's room. You design a mobile using 5 pieces of string and two rods. The first rod hangs from the ceiling. One object hangs from one end of the rod and another rod hangs from the other end. That second rod has two objects hanging from each end. The project would be easier if your friend's daughter knew what she wanted to hang from the mobile, but she cannot make up her mind. One day it is dinosaurs, another day it is the Power Rangers, and another day it is famous women scientists. Frustrated, you decide to build a laboratory model to test the type of mobile you will build in order to make sure no matter what she decides to hang, the mobile can be easily assembled.


To test your mobile design, you will have two wooden dowel rods, some string, and three objects ( $\mathrm{A}, \mathrm{B}$, and C ) of different masses. Your final mobile should use all these parts.


One metal rod and one table clamp will be used to hang the mobile. You will also have three mass hangers and one mass set.

## Prediction

Restate the problem. What quantities do you need to calculate to test your design? What are the variables in the system?


Read: Fishbane Chapter 10. Read carefully Sections 10-2 and 10-3 and Examples 10-5 and 10-6.
To figure out your prediction, it is useful to use a problem solving strategy such as the one outlined below:

1. Draw a mobile similar to the one in the Equipment section. Select your coordinate system. Identify and label the masses and lengths relevant to this problem. Draw and label all the relevant forces.
2. Draw a free-body diagram for each rod showing the location of the forces acting on the rods. Label these forces. Identify any forces related by Newton's third law. Choose the axis of rotation for each rod. Identify any torques on each rod.
3. For each free-body diagram, write the equation expressing $N$ ewton's second law for forces and another equation for torques. (Remember that your system is in equilibrium.) What are the total torque and the sum of forces on an object when it is in equilibrium?
4. Identify the target quantities you wish to determine. Use the equations collected in step 3 to plan a solution for the target. If there are more unknowns than equations, reexamine the previous steps to see if there is additional information about the situation that can be expressed in an additional equation. If not, see if one of the unknowns will cancel out.

## Exploration

Collect the necessary parts of your mobile. Find a convenient place to hang it.
Decide on the easiest way to determine the position of the center of mass of each rod.
Will the length of the strings for the hanging objects affect the balance of the mobile? Why or why not? Try it.

Where does the heaviest object go? The lightest?
Decide what measurements you need to make to check your prediction. If any major assumptions are used in your calculations, decide on the additional measurements that you need to make to justify them.

Outline your measurement plan.

## Measurement

M easure and record the location of the center of mass of each rod. Determine the location on thetop rod from which you will hang it. Determine the location on the second rod from which you will hang it. Also, measure and record the mass of each rod and the mass of the three hanging objects.

Is there another configuration of the three objects that also results in a stable mobile?

## Analysis

Using the values you measured and your prediction equations, calculate the locations (with uncertainties) of the two strings holding up the rods.

To test your prediction, build your mobile and then hang it. If your mobile did not balance, adjust the strings attached to the rods until it does bal ance and determine their new positions.

Is there another configuration of the three objects that also results in a stable mobile? Try it.

## Conclusion

Did your mobile balance as designed? What corrections did you need to make to get it to balance? Were these corrections a result of some systematic error, or was there a mistake in your prediction?

Explain why the lengths of each string were or were not important in the mobile design.

## PROBLEM \#7:

## EQUILIBRIUM

You have been hired to design new port facilities for Duluth. Your assignment is to evaluate a new crane for lifting containers from the hold of a ship. The crane is a boom (a steel bar of uniform thickness) with one end attached to the ground by a hinge that allows it to rotate in the vertical plane. Near the other end of the boom is a motor driven cable that lifts a container straight up at a constant speed. The boom is supported at an angle by another cable. One end of the support cable is attached to the boom and the other end goes over a pulley. That other end is attached to a counterweight that hangs straight down. The pulley is supported by a mechanism that adjusts its height so the support cable is always horizontal. Your task is to determine how the angle of the boom from the horizontal changes, as a function of the weight of the container being lifted. The mass of the boom, the mass of the counterweight, the attachment point of the support cable and the attachment point of the lifting cable have all been specified by the engineers.

You will test your cal culations with a laboratory model of the crane.

## EQUIPMENT

You will have a channel of aluminum, a pulley, a pulley clamp, two mass hangers, a mass set and somestrings.


## Prediction

Restate the problem. What quantities do you need to calculate to test your design? What parameters are set, and which one(s) will you vary?


Read: Fishbane Chapter 10. Read carefully Sections 10-2 and 10-3 and Examples 10-5 and 10-6.

To figure out your prediction, it is useful to use a problem solving strategy such as the one outlined below:

1. Draw a crane similar to the one in the Equipment section. Select your coordinate system. Identify and label the masses and lengths relevant to this problem. Draw and label all the relevant forces.
2. Draw a free-body diagram for the bar showing the location of the forces acting on it. Label these forces. Choose the axis of rotation. Identify any torques on the rod.
3. Write the equation expressing Newton's second law for forces and another equation for torques. Remember that the bar is in equilibrium.
4. Identify thetarget quantities you wish to determine. Use the equations collected in step 3 to plan a solution for the target. If there are more unknowns than equations, reexamine the previous steps to see if there is additional information about the situation that can be expressed in an additional equation. If not, see if one of the unknowns will cancel out.
5. Make a graph of the bar's angle as a function of the weight of object $A$.

## EXPLORATION

Collect the necessary parts of your crane. Find a convenient place to build it.
Decide on the easiest way to determine where the center of mass is located on the bar.
Determine where to attach the lifting cable and the support cable so that the crane is in equilibrium for the weights you want to hang. Try several possibilities. If your crane tends to lean to one side or the other, try putting a vertical rod near the end of the crane to keep your crane from moving in that direction. If you do this, what effect will this vertical rod have on your calculations?

Do you think that the length of the strings for the hanging weights will affect the balance of the crane? Why or why not?

## Outlineyour measurement plan.

## Measurement

Build your crane.
Make all necessary measurements of the configuration. Every time only change the mass of object A and determine the angle of the bar when the system is in equilibrium. Remember to adjust the height of the pulley to keep the support string horizontal that hangs the object B for each case.

Is there another configuration of the three objects that also results in a stable configuration?

## ANALYSIS

Make a graph of the bar's angle as a function of the weight of object A and compare it with your predicted graph.

What happens to that graph if you change the mass of object B or the position of the attachment of the support cable to the bar?

## CONCLUSION

Did your crane balance as designed? What corrections did you need to make to get it to balance? Were these corrections a result of some systematic error, or was there a mistake in your prediction? In your opinion, what is the best way to construct a crane that will allow you to quickly adjust the setup so as to meet the demands of carrying various loads? Justify your answer.

## $\square$ CHECK YOUR UNDERSTANDING

1. A long stick is supported at its center and is acted on by three forces of equal magnitude, as shown at right. The stick is free to
 swing about its support. $\mathbf{F}_{\mathbf{2}}$ is a vertical force and $\mathbf{F}_{\mathbf{3}}$ is horizontal.
a. Rank the magnitudes of the torques exerted by the three forces about an axis perpendicular to the drawing at the left end of thestick. Explain your reasoning.
b. Rank themagnitudes of the torques about the center support. Explain your reasoning.
c. Rank the magnitudes of the torques about an axis perpendicular to the drawing at the right end of the stick. Explain your reasoning.
d. Can the stick be in translational equilibrium? Explain your reasoning.
e Can the stick be in rotational equilibrium? Explain your reasoning.
2. Four light beads of mass $m$ are arranged in different ways on four identical light rods, as shown in the diagrams below.


Rod \#4

Rank the rotational inertia of the four rods. Explain your reasoning.

## $\square$ CHECK YOUR UNDERSTANDING

3. Two pulleys are firmly attached to each other and rotate on a stationary axle through their centers, as shown at right. A weight $\mathbf{W}$ is attached to a string wound around the smaller pulley. You pull on the string wound around the larger pulley with just enough force $\mathbf{F}$ to raise the weight at a constant speed.

a. Is the magnitude of $\mathbf{F}$ greater than, less than, or equal to $\mathbf{W}$ ? Explain.
b. If you raise the weight a distance $h$, is the distance that you pulled the string greater than, less than, or equal to h? Explain.
c. Is the work done by the man greater than, less than or equal to the increase in potential energy of the weight? Explain.
4. A yo-yo is made from two uniform disks of radius $b$ connected by a short cylindrical axle of radius a, as shown at right.


The yo-yo sits on a table. A string is wound
 around the axle, and one end of the string is pulled by a force $\mathbf{F}$. If the force is small enough, theyo-yo rolls without slipping. It rotates clockwise as it accelerates to the right.
a. Write an expression for the total moment of inertia of the yo-yo.
b. What is the direction of the frictional force exerted on the yo-yo by the table surface? Explain.
c. Which force, $\mathbf{F}$ or the frictional force, is greater? Or are the two forces equal? Explain.
d. Which force exerts the larger torque on the yo-yo, or are the torques equal? Explain.
5. Two identical disks have a common axis. Initially, one of the disks is spinning with an angular frequency $w_{0}$. When the two disks are brought into contact, they stick together.
a. Is the final angular frequency greater than, less than, or equal to $w_{0} / 2$ ? Explain.

b. Is the kinetic energy of the system the same before and after the collision? Explain.

## $\square$ CHECK YOUR UNDERSTANDING

$\qquad$

# PHYSICS 1301 LABORATORY REPORT <br> Laboratory VII 

Name and ID \#: $\qquad$
Date performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$
$\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORAT ORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in joumal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readabbe; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATA AND DATA TABLE S <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; scales, labels and uncertainties on graphs; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly ; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL(incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total <br> points achieved) |  |
| BONUS POINTS FOR TEAMWORK <br> (as specified by course policy) |  |

* An "R" in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## LABORATORY VIII MECHANICAL OSCILLATIONS

In most of the laboratory problems this semester, objects have moved with constant accel eration because the net force acting on them has been constant. In this set of laboratory problems the force on an object, and thus its acceleration, will change with the object's position.

You are familiar with many objects that oscillate-- a tuning fork, the balance wheel of a mechanical watch, a pendulum, or the strings of a guitar. At the atomic level, atoms oscillate within molecules, and molecules within solids. All of these objects are subjected to forces that change with position. Springs are a common example of objects that exert this type of force.

In this lab you will study oscillatory motion caused by springs exerting a force on an object. You will use different methods to determine the strength of the force exerted by different spring configurations, and investigate what quantities determine the oscillation frequency of systems.

## Objectives:

After successfully completing this laboratory, you should be able to:

- provide a qualitative explanation of the behavior of oscillating systems using the concepts of restoring force and equilibrium position.
- identify the physical quantities which influence the period (or frequency) of the oscillatory motion and describe this influencequantitatively.
- demonstrate a working knowledge of the mathematical description of an oscillator's motion.
- describe qualitatively the effect of additional forces on an oscillator's motion.


## Preparation:

Read Paul M. Fishbane: Chapter 13.
Before coming to lab you should be able to:

- Describe the similarities and differences in the behavior of the sine and cosine functions.
- Recognized the difference between amplitude, frequency, angular frequency, and period for repetitive motion.
- Determine the force on an object exerted by a spring using the concept of a spring constant.


## PROBLEM \#1: <br> MEASURING SPRING CONSTANTS

You are selecting springs for a large antique clock; to determine the forces they will exert in the clock, you need to know their spring constants. One book recommends a static approach: hang objects of different weights on the spring and measure the displacement from equilibrium. Another book suggests a dynamic approach: hang an object on the end of a spring and measure its oscillation frequency. You decide to compare the results of the two methods, in order to get the best precision possible for your characterization of the clock's springs. But first you have to figure out how to cal culate spring constants from each type of measurement.

## EQUIPMENT

You can hang a spring from a metal rod that is fastened on a table clamp. Then you can attach an object to the hanging end of the spring. You can vary the mass of the object. A meter stick, a triple-beam balance, a stopwatch, a mass hanger, a mass set and the video analysis equipment are available for this experiment.


## Predictions

Restate the problem. What two relationships must you calculate to prepare for your experiment?

## Warm UP

Read: Fishbane Chapter 13. Read carefully Section 13-3 and Example 13-4.

To figure out your predictions, it is useful to apply a problem-solving strategy such as the one outlined below:

M ethod \#1: Suppose you hang objects of several different masses on a spring and measure the vertical displacement of each object.

1. Make two sketches of the situation, one before you attach a mass to a spring, and one after a mass is suspended from the spring and is at rest. Draw a coordinate system and label the position where the spring is unstretched, the stretched position, the mass of the object, and the spring constant. Assume the springs are massless.
2. Draw a force diagram for the object hanging at rest from the end of the spring. Label the forces. Newton's second law gives the equation of motion for the hanging object. Solve this equation for the spring constant.
3. Use your equation to sketch the displacement (from the unstretched position) versus weight graph for the object hanging at rest from the spring. How is the slope of this graph related to the spring constant?

M ethod \#2: Suppose you hang an object from the spring, start it oscillating, and measure the period of oscillation.

1. Make a sketch of the oscillating system at a time when the object is below its equilibrium position. Draw this sketch to the side of the two sketches drawn for method \#1. Identify and label this new position on the same coordinate axis.
2. Draw a force diagram of the object at this new position. Label the forces.
3. Apply Newton's second law to write down the equation of motion for the object at each of the above positions.

When the object is below its equilibrium position, how is the stretch of the spring from its unstretched position related to the position of the system's (spring \& object) equilibrium position and its displacement from that equilibrium position to the position in your second sketch. Define these variables, and write an equation to show this relationship.
4. Solve your equations for acceleration of the object as a function of the mass of the suspended object, the spring constant, and the displacement of the spring/ object system from its equilibrium position. Keep in mind that acceleration is second derivative of position with respect to time.
5. Try a periodic solution $(\sin (\omega \cdot t)$ or $\cos (\omega \cdot t)$ ) to your equation of motion (Newton's second law). Find the frequency $\omega$ that satisfies equation of motion for all times. How is the frequency of the system related to its period of oscillation?

## EXPLORATION

Method \#1: Select a series of masses that give a usable range of displacements. The smallest mass must be much greater than the mass of the spring to fulfill the massless spring assumption. The largest mass should not pull the spring past its elastic limit (about 60 cm ). Beyond that point you will damage the spring. Decide on a procedure that allows you to measure the displacement of the spring-object system in a consistent manner. Decide how many measurements you will need to make a reliable determination of the spring constant.

Method \#2: Secure one end of the spring safely to the metal rod and select a mass that gives a regular oscillation without excessive wobbling to the hanging end of the spring. Again, the largest mass should not pull the spring past its elastic limit and the smallest mass should be much greater than the mass of the spring. Practice starting the mass in vertical motion smoothly and consistently.

Practice making a video to record the motion of the spring-object system. Decide how to measure the period of oscillation of the spring-object system by video and stopwatch. How can you minimizethe uncertainty introduced by your reaction time in starting and stopping the stopwatch? How many times should you measure the period to get a reliable value? How will you determine the uncertainty in the period?

## Measurement

Method \#1: Record the masses of different hanging objects and the corresponding displacements.
Method \#2: For each hanging object, record the mass of the object. Use a stopwatch to roughly determine the period of the oscillation and then make a video of the motion of the hanging object. Repeat the same procedure for objects with different masses.

Analyze your data as you go along so you can decide how many measurements you need to make to determine the spring constant accurately and reliably.

## Analysis

Method \#1: Make a graph of displacement versus weight for the object-spring system. From the slope of this graph, cal culate the value of the spring constant, including the uncertainty.

Method \#2: Determinethe period of each oscillation from your videos. (Usethe period by stopwatch as a predicted parameter in your fit equations.) Make a graph of period (or frequency) versus mass for the object-spring system. If this graph is not a straight line, make another graph of the period vs. some power of the mass that should produce a straight line. (Use your prediction equation to decide what that power should be.) From the slope of the straight-line graph, calculate the value of the spring constant, including the uncertainty.

## Conclusion

How do the two values of the spring constant compare? Which method is faster? Which method gives you the best precision? Justify your answers in terms of your data and measurements.

Did your prediction equation for Method \#2 help you correctly identify a power of the mass that would produce a straight-linegraph when you were working through the analysis? Explain why or why not.

How did you minimize the uncertainty involved in the timing for Method \#2? Did video analysis give you a better estimate of the period than the stopwatch?

## PROBLEM \#2:

## THE EFFECTIVE SPRING CONSTANT

Your company has bought the prototype for a new flow regulator from a local inventor. Your job is to prepare the prototype for mass production. While studying the prototype, you notice the inventor used some rather innovative spring configurations to supply the tension needed for the regulator valve. In one location the inventor had fastened two different springs side-by-side, as in Figure A below. In another location the inventor attached two different springs end-to-end, as in Figure B below.

To decrease the cost and increase the reliability of the flow regulator for mass production, you need to replace each spring configuration with a single spring. These replacement springs must exert the same forces when stretched the same amount as the original spring configurations.

The spring constant for a single spring that replaces a configuration of springs is called the configuration's effective spring constant.

## Equipment

You have two different springs with the same unstretched length, but different spring constants $\mathrm{k}_{1}$ and k2. These springs can be hung vertically side-by-side (FigureA) or end-to-end (FigureB). You will also have a meter stick, a stopwatch, a metal rod, a wooden rod, a table clamp, a mass hanger, a mass set and the video anal ysis equipment.


Figure A


Figure B

## Predictions

Restate the problem. What ratios do you need to calculate for each spring configuration in the problem?


Read: Fishbane Chapter 13. Read carefully Section 13-3 and Example 13-4.

To figure out your predictions, it is useful to apply a problem-solving strategy such as the one outlined below. A pply the strategy first to the sideby-side configuration, and then repeat for the end-to-end configuration:

1. Make a sketch of the spring configuration similar to one of the drawings in the Equipment section. Draw a coordinate system and label the positions of each unstretched spring, the final stretched position of each spring, the two spring constants, and the mass of the object suspended. Assume that the springs are massless.

For the sideby-side configuration, assume that the light bar attached to the springs remains horizontal (it does not twist).

Now make a second sketch of a single (massless) spring with spring constant $\mathrm{k}^{\prime}$ that has the same object suspended from it and the same total stretch as the combined springs. Label this second sketch with the appropriate quantities.
2. Draw force diagrams of the object suspended from the combined springs and the same object suspended from the single replacement spring. Label the forces. Use Newton's Third Law to identify forces on different diagrams that have the same magnitudes.
For the end-to-end configuration, draw an additional force diagram for the point at the connection of the two springs.
3. For each force diagram, write a Newton's Second Law equation to relate the net force on an object (or the point connecting the springs) to its acceleration.

Write an equation relating the total stretch of the combined springs related to the stretch of each of the springs? How does this compare to the stretch of the single replacement spring? How does the stretch of each spring relate to its spring constant and the force it exerts?
4. Rewrite each Newton's second law equation in terms of the stretch of each spring.

For the end-to-end configuration: At the connection point of the two springs, what is the force of the top spring on the bottom spring? What is the force of the bottom spring on the top spring?
5. Solve your equations for the effective spring constant ( $\mathrm{k}^{\prime}$ ) of the single replacement spring, in terms of the two spring constants.

## Exploration

To test your predictions, you must decide how to measure each spring constant of the two springs and the effective spring constants of the side-by-side and end-to-end configurations.

From your results of Problem \#1, select the best method for measuring spring constants. Justify your choice. DO NOT STRETCH THE SPRINGS PAST THEIR ELASTIC LIMIT (ABOUT 60 CM) OR YOU WILL DAMAGETHEM.

Perform an exploration consistent with your selected method. If necessary, refer back to the appropriate Exploration section of Problem \#1.

Remember, the smallest mass must be much greater than the mass of the spring to fulfill the massless spring assumption. The largest mass should not pull the spring past its elastic limit.

Outline your measurement plan.

## Measurement

Make the measurements that are consistent with your selected method. If necessary, refer back to the appropriate M easurement section of Problem \#1. What are the uncertainties in your measurements?


Determine the effective spring constants (with uncertainties) of the side-by-side spring configuration and the end-to-end spring configuration. If necessary, refer back to Problem \#l for the analysis technique consistent with your selected method.

Determinethe spring constants of the two springs. Calculate the effective spring constants (with uncertainties) of the two configurations using your Prediction equations.

How do the measured and predicted values of the effective spring constants for the two configurations compare?

## CONCLUSION

What are the effective spring constants of a side-by-side spring configuration and an end-to-end spring configuration? Did your measured values agree with your initial predictions? Why or why not? What are the limitations on the accuracy of your measurements and analysis?

Which configuration provides a larger effective spring constant?

## PROBLEM \#3:

## OSCILLATION FREQUENCY WITH TWO SPRINGS

You have a summer job with a research group at the University. Your supervisor asks you to design equipment to measure earthquake aftershocks. The calibration sensor needs to be isolated from the earth movements, yet free to move. You decide to place the sensor on a track cart and attach a spring to both sides of the cart. You should now be able to measure the component of the aftershocks al ong the axis defined by the track. To make any quantitative measurements with the sensor you need to know the frequency of oscillation for the cart as a function of the spring constants and the mass of the cart.

## EquIPMENT

You will have an aluminum track, two adjustable end stops, two oscillation springs, a meter stick, a stopwatch, a cart and the video analysis equipment.


Restate the problem. What quantities do you need to calculate to test your design?

## Warm UP

Read: FishbaneChapter 13 . Read carefully Sections $13-3$ and $13-4$ and Examples 13-6.
To figure out your prediction, it is useful to use a problem-solving strategy such as the one outlined below:

1. Make two sketches of the oscillating cart, one at its equilibrium position, and one at some other position and time while it is oscillating. On your sketches, show the direction of the velocity and acceleration of the cart. Identify and label the known (measurable) and unknown quantities.
2. Draw a force diagram of the oscillating cart away from its equilibrium position. Label the forces.
3. A pply Newton's laws as the equation of motion for the cart. Consider both cases when the cart is in the equilibrium and displaced from the equilibrium position.

Solve your equation for the acceleration, simplifying the equation until it is similar to equation 13-14 (Fishbane).
4. Try a periodic solution $(\sin (\omega \cdot t)$ or $\cos (\omega \cdot t)$ ) to your equation of motion (Newton's second law). Find the frequency $\omega$ that satisfies equation of motion for all times. How is the frequency of the system related to its period of oscillation? Calculate frequency of the system as a function of the mass of the cart and the two spring constants.
5. Use the simulation "LabSim5" (See A ppendix F for a brief explanation of how to use the simulations) to approximate the conditions of this problem.


Decide the best method to determine the spring constants based on your results of Problem \#1. D O NOT STRETCH THE SPRINGS PAST THEIR ELASTIC LIMIT (ABOUT 60 CM) OR YOU WILL DAMAGETHEM.

Find the best place for the adjustable end stop on the track. D o not stretch the springs past 60 cm , but stretch them enough so they oscillate the cart smoothly.

Practice releasing the cart smoothly. Y ou may notice the amplitude of oscillation decreases. What's the reason for it? Does this affect the period of oscillation?

## MeAsurement

Determine the spring constants. Record these values. What is the uncertainty in these measurements?
Record the mass of the cart. Use a stopwatch to roughly determine the period of oscillation and then make a video of the motion of the oscillating cart. Y ou should record at least 3 cycles.

## Analysis

A nalyzeyour video to find the period of oscillation. Calculate the frequency (with uncertainty) of the oscillations from your measured period.

Calculate the frequency (with uncertainty) using your Prediction equation.

## CONCLUSION

What is the frequency of the oscillating cart? Did your measured frequency agree with your predicted frequency? Why or why not? What are the limitations on the accuracy of your measurements and anal ysis? What is the effect of friction?

If you completed Problem \#2: What is the effective spring constant of this configuration? How does it compare with the effective spring constants of the side-by-side and end-to-end configurations?

## PROBLEM \#4: OSCILLATION FREQUENCY OFAN EXTENDED SYSTEM

You are the technical advisor for the next Bruce Willis action movie, DieEven H arder, which is to be filmed in Minnesota. The script calls for a spectacular stunt. BruceWillis dangles over a cliff from a long rope whose other end is tied to the Bad Guy. The Bad Guy is on the ice-covered ledge of the cliff. The Bad Guy's elastic parachute line is tangled in a tree located several feet from the edge of the cliff. Bruce and the Bad Guy are in simple harmonic motion, and at the top of his motion, Bruce unsuccessfully tries to grab for the safety of the cliff edge while the Bad Guy reaches for his discarded knife. The script calls for Bad Guy to cut the rope just as Bruce reaches the top of his motion again.

The problem is that it is expensive to have Bruce hanging from the rope while the crew films closeups of the Bad Guy, but the stunt double weighs at least 50 pounds more than Bruce. The director wants to know if the stunt double will have a different motion than Bruce, and if so whether the difference would be noticeable. Will he?

You decide to test your prediction by modeling the situation with the equipment described below.

## EQUIPMENT

You have an aluminum track with an adjustableend stop, a pulley, a pulley clamp, an oscillation spring, a cart, some strings, a mass hanger, a mass set, a meter stick, a stopwatch and the video analysis equipment.

The track represents the ice-covered ledge of the cliff, the adjustable end-stop represents the tree, the spring represents the elastic cord, the cart represents the Bad Guy, the string represents the rope and the hanging object represents Bruce Willis or his stunt double in this problem.


## Prediction

Restate the problem. What quantities must you calculate to answer the director's question?

## Warm UP

Read: Fishbane Chapter 13. Read carefully Section 13-4 and Examples 13-5 and 13-6.
To figure out your prediction, it is useful to use a problem-solving strategy such as the one outlined below:

1. Make sketches of the situation when the cart and hanging object are at their equilibrium positions and at some other time while the system is oscillating. On your sketches, show the direction of the acceleration of the cart and hanging object. Identify and label the known (measurable) and unknown quantities.
2. Draw separate force diagrams of the oscillating cart and hanging object. Label each force. Are there any third-law pairs?
3. Independently apply N ewton's laws to the cart and to the hanging object.
4. Solve your equations for the acceleration, simplifying the equation until it is similar to equation 13-14 (Fishbane).
5. Try a periodic solution $[\sin (\omega \cdot t)$ or $\cos (\omega \cdot t)$ ] to your equation of motion (Newton's second law). Find the frequency $\omega$ that satisfies equation of motion for all times. How is the frequency of the system related to its period of oscillation? Calculate frequency of the system as a function of the mass of the cart, the mass of the hanging object, and the spring constant.
6. Use your equation to sketch the expected shape of a graph of the oscillation frequency versus hanging mass. Will the frequency increase, decrease or stay the same as the hanging mass increases?
7. Now you can complete your prediction. Use your equation to sketch the expected shape of the graph of oscillation frequency versus the hanging object's mass.

## EXPLORATION

If you do not know the spring constant of your spring, you should decide the best way to determine the spring constant based on your results of Problem \#1.

Find the best place for the adjustable end stop on the track. DO NOT STRETCH THE SPRING PAST 60 CM OR YOU WILL DAMAGE IT, but stretch it enough so the cart and hanging mass oscillate smoothly. Determine the best range of hanging masses to use.

Practice rel easing the cart and hanging mass smoothly and consistently. You may notice the amplitude of oscillation decreases. What's the reason for it? Does this affect the period of oscillation?

## Measurement

If necessary, determine the spring constant of your spring. What is the uncertainty in your measurement?

For each hanging object, record the masses of the cart and the hanging object. Use a stopwatch to roughly determine the period of oscillation and then make a video of the oscillating cart for each hanging object. You should record at least 3 cycles for each video.
A nalyze your data as you go along, so you can determine the size and number of different hanging masses you need to use.

Collect enough data to convince yourself and others of your conclusion about how the oscillation frequency depends on the hanging mass.


For each hanging object, digitize the video to get the period of oscillation and then calculate the oscillation frequency (with uncertainty) from your measured period.

Graph the frequency versus the hanging object's mass. On the samegraph, show your predicted relationship.

What are the limitations on the accuracy of your measurements and analysis? Over what range of values does the measured graph match the predicted graph best? Do the two curves start to diverge from one another? If so, where? What does this tell you about the system?

## CONCLUSION

Does the oscillation frequency increase, decrease or stay the same as the hanging object's mass increases? State your result in the most general terms supported by your analysis.

What will you tell the director? Do you think the motion of the actors in the stunt will change if the heavier stunt man is used instead of Bruce Willis? How much heavier than Bruce would the stunt man have to be to produce a noticeable difference in the oscillation frequency of the actors? Explain your reasoning in terms the director would understand so you can collect your paycheck.

## PROBLEM \#5:

## DRIVEN OSCILLATIONS

You are now prepared to calibrate your seismic detector (from Problem \#3). You need to determine how the amplitude of the oscillations of the detector will vary with the frequency of the earthquake aftershocks. So you replace the end stop on the track with a device that moves the end of the spring back and forth, simulating the earth moving beneath the track. The device, called a mechanical oscillator, is designed so you can change its frequency of oscillation.

## EQUIPMENT

You will use your seismic detector apparatus and a mechanical oscillator.
The mechanical oscillator is somewhat like a loudspeaker with one end of a metal rod attached to the center, and the other end of the rod is attached to one of the springs. The oscillator is connected to a function generator which causes the rod to oscillate back and forth with adjustable frequencies which can be read from the display on the function generator.


You will also have a meter stick, a stopwatch, a metal rod, a table clamp, an end stop, two oscillation springs and two banana cables.

## Prediction

Make your best-guess sketch of what you think a graph of the amplitude of the cart versus the frequency of the mechanical driver will look like. Assume the mechanical oscillator has constant amplitude of a few millimeters.

## Warm Up

Read: FishbaneChapter 13. Read carefully Section 13-8. Use the simulation "LabSim5" (See A ppendix F for a brief explanation of how to use the simulations) to approximate the conditions of this problem.

## EXPLORATION

Examine the mechanical oscillator. Mount it at the end of the aluminum track, using the clamp and metal rod so its shaft is aligned with the cart's motion. Connect it to the function generator, using the output marked Lo (for "Iow impedance"). Use middle or maximum amplitude to observe the oscillation of the cart at the lowest frequency possible.

Determine the accuracy of the digital display on the frequency generator by timing one of the lower frequencies. Devise a scheme to accurately determine the amplitude of a cart on the track, and practice the technique. For each new frequency, should you restart the cart at rest?

When the mechanical oscillator is at or near the un-driven frequency (natural frequency) of the cartspring system, try to simultaneously observe the motion of the cart and the shaft of the mechanical oscillator. What is the relationship? What happens when the oscillator's frequency is twice as large as the natural frequency?


If you do not know the natural frequency of your system when it is not driven, determine it using the technique of Problem \#3. Collect enough cart amplitude and oscillator frequency data to test your prediction. Be sure to collect several data points near the natural frequency of the system.


Make a graph the oscillation amplitude of the cart versus oscillator frequency. Is this the graph you had anticipated? Where is it different? Why? What is the limitation on the accuracy of your measurements and analysis?

## CONCLUSION

Can you explain your results? Is energy conserved? What will you tell your boss about your design for a seismic detector?

## $\square$ CHECK YOUR UNDERSTANDING

1. The diagram below shows an oscillating mass/ spring system at times $0, \mathrm{~T} / 4, \mathrm{~T} / 2,3 \mathrm{~T} / 4$, and T , where $T$ is the period of oscillation. For each of these times, write an expression for the displacement ( $x$ ), the velocity ( v ), the acceleration (a), the kinetic energy (KE), and the potential energy (PE) in terms of the amplitude of the oscillations (A), the angular velocity (w), and the spring constant (k).

2. Identical masses are attached to identical springs which hang vertically. The masses are pulled down and released, but mass $B$ is pulled further down than mass $A$, as shown at right.
a. Which mass will take a longer time to reach the equilibrium position? Explain.
b. Which mass will have the greater acceleration at the instant of release, or will they have the same acceleration? Explain.
c. Which mass will be going faster as it passes through equilibrium, or will they have the same speed? Explain.
d. Which mass will have the greater acceleration at the equilibrium point, or will they have the same acceleration? Explain.

## $\boxed{\square}$ CHECK YOUR UNDERSTANDING

3. Two different masses are attached to different springs which hang vertically. Mass A is larger, but the period of simple harmonic motion is the same for both systems. They are pulled the same distance below their equilibrium positions and released from rest.

a. Which spring has the greater spring constant? Explain.
b. Which spring is stretched more at its equilibrium position? Explain.
c. The instant after release, which mass has the greater acceleration? Explain.
d. If potential energy is defined to be zero at the equilibrium position for each mass, which system has the greater total energy of motion? Explain.
e. Which mass will have the greater kinetic energy as it passes through its equilibrium position? Explain
f. Which mass will have the greater speed as it passes through equilibrium? Explain.
4. Five identical springs and three identical masses are arranged as shown at right.
a. Compare the stretches of the springs at equilibrium in the three cases. Explain.
b. Which case, a, b, or c, has the greatest effective spring constant?
The smallest effective spring constant?
Explain.
c. Which case would execute simple harmonic motion with the greatest period? With the least period? Explain.

## $\square$ CHECK YOUR UNDERSTANDING

$\qquad$

## PHYSICS 1301LABORATORY REPORT <br> Laboratory VIII

Name and ID \#: $\qquad$
D ate performed: $\qquad$ Day/ Time section meets: $\qquad$
Lab Partners' Names: $\qquad$

Problem \# and Title: $\qquad$
Lab Instructor's Initials: $\qquad$

| Grading Checklist | Points* |
| :--- | :--- |
| LABORATORY JOURNAL: |  |
| PREDICTIONS <br> (individual predictions and warm-up completed in journal before each lab session) |  |
| LAB PROCEDURE <br> (measurement plan recorded in journal, tables and graphs made in journal as data is collected, <br> observations written in journal) |  |
| PROBLEM RE PORT: |  |
| ORGANIZATION <br> (clear and readable; logical progression from problem statement through conclusions; pictures <br> provided where necessary; correct grammar and spelling; section headings provided; physics stated <br> correctly) |  |
| DATAN AND DATA TABLES <br> (clear and readable; units and assigned uncertainties clearly stated) |  |
| RESULTS <br> (results clearly indicated; correct, logical, and well-organized calculations with uncertainties <br> indicated; ccales, labels and uncertainties on graph; physics stated correctly) |  |
| CONCLUSIONS <br> (comparison to prediction \& theory discussed with physics stated correctly ; possible sources of <br> uncertainties identified; attention called to experimental problems) |  |
| TOTAL(incorrect or missing statement of physics will result in a maximum of 60\% of the total <br> points achieved; incorrect grammar or spelling will result in a maximum of 70\% of the total points <br> achieved) |  |
| BONUS POINTS FOR TEAMWWORK <br> (as specified by course policy) |  |

* An " R " in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.


## Appendix A: Significant Figures

Calculators make it possible to get an answer with a huge number of figures. Unfortunately, many of them are meaningless. For instance, if you needed to split $\$ 1.00$ among three people, you could never give them each exactly $\$ 0.333333 . .$. The same is true for measurements. If you use a meter stick with millimeter markings to measure the length of a key, as in figure A-1, you could not measure more precisely than a quarter or half or a third of a mm . Reporting a number like 5.8142712 cm would not only be meaningless, it would be misleading.

Figure A-1


In your measurement, you can precisely determine the distance down to the nearest millimeter and then improve your precision by estimating the next figure. It is always assumed that the last figure in the number recorded is uncertain. So, you would report the length of the key as 5.81 cm . Since you estimated the 1 , it is the uncertain figure. If you don't like estimating, you might be tempted to just give the number that you know best, namely 5.8 cm , but it is clear that 5.81 cm is a better report of the measurement. An estimate is always necessary to report the most precise measurement. When you quote a measurement, the reader will al ways assume that the last figure is an estimate. Quantifying that estimate is known as extimating uncertainties. Appendix B will illustrate how you might use those estimates to determine the uncertainties in your measurements.

## What are significant figures?

The number of significant figures tells the reader the precision of a measurement. Table A-1 gives some examples.

## Table A-1

| Length <br> (centimeters) | Number of <br> Significant <br> Figures |
| :---: | :---: |
| 12.74 | 4 |
| 11.5 | 3 |
| 1.50 | 3 |
| 1.5 | 2 |
| 12.25345 | 7 |
| 0.8 | 1 |
| 0.05 | 1 |

One of the things that this table illustrates is that not all zeros are significant. For example, the zero in 0.8 is not significant, while the zero in 1.50 is significant. Only the zeros that appear after the first non-zero digit aresignificant.

A good rule is to always express your values in scientific notation. If you say that your friend lives 143 m from you, you are saying that you are sure of that distance to within a few meters (3 significant figures). What if you really only know the distance to a few tens of meters (2 significant figures)? Then you need to express the distance in scientific notation $1.4 \times 10^{2} \mathrm{~m}$.

## Is it al ways better to have more figures?

Consider the measurement of the length of the key shown in FigureA-1. If we have a scale with ten etchings to every millimeter, we could use a microscope to measure the spacing to the nearest tenth of a millimeter and guess at the one
hundredth millimeter. Our measurement could be 5.814 cm with the uncertainty in the last figure, four significant figures instead of three. This is because our improved scale allowed our estimate to be more precise. This added precision is shown by more significant figures. The more significant figures a number has, the more precise it is.

How do I use significant figures in calculations? When using significant figures in calculations, you need to keep track of how the uncertainty propagates. There are mathematical procedures for doing this estimate in the most precise manner. This type of estimate depends on knowing the statistical distribution of your measurements. With a lot less effort, you can do a cruder estimate of the uncertainties in a calculated result. This crude method gives an overestimate of the uncertainty but it is a good place to start. For this course this simplified uncertainty estimate (described in Appendix B and below) will begood enough.

## Addition and subtraction

When adding or subtracting numbers, the number of decimal places must be taken into account.

The result should be given to as many decimal places as the term in the sum that is given to the smallest number of decimal places.
Examples:

| Addition | Subtraction |
| :---: | :--- |
| 6.242 | 5.875 |
| +4.23 | $\frac{-3.34}{2.535}$ |
| +0.013 |  |
| 10.485 |  |
| 10.49 | 2.54 |

The uncertain figures in each number are shown in bold-faced type.

## M ultiplication and division

When multiplying or dividing numbers, the number of significant figures must be taken into account.
The result should be given to as many significant figures as the term in the product that is given to the smallest number of significant figures.

The basis behind this rule is that the least accurately known term in the product will dominate the accuracy of the answer.

As shown in the examples, this does not always work, though it is the quickest and best rule to use. When in doubt, you can keep track of the significant figures in the calculation as is done in the examples.

Examples:

| Multiplication |  |
| :--- | :--- |
| 15.84 | 17.27 |
| $\times 2.5$ | $\underline{\times 4.0}$ |
| 7920 | 69.080 |
| 3168 |  |
| 39.600 |  |
| 40 | 69 |


| Division |  |
| :---: | :---: |
| $\frac{117}{23) 2691}$ | $75) \frac{25}{1875}$ |
| $\underline{23}$ | $\frac{150}{39}$ |
| $\underline{\mathbf{2 3}}$ | 375 |
| $\frac{161}{161}$ |  |
| $1.2 \times 10^{2}$ | $2.5 \times 10^{1}$ |

## PRACTICE EXERCISES

1. Determine the number of significant figures of the quantities in the following table:

| Length <br> (centimeters) | Number of <br> Significant <br> Figures |
| :---: | :---: |
| 17.87 |  |
| 0.4730 |  |
| 17.9 |  |
| 0.473 |  |
| 18 |  |
| 0.47 |  |
| $1.34 \times 10^{2}$ |  |
| $2.567 \times 10^{5}$ |  |
| $2.0 \times 10^{10}$ |  |
| 1.001 |  |
| 1.000 |  |
| 1 |  |
| 1000 |  |
| 1001 |  |

2. Add: 121.3 to $6.7 \times 102$ :
[Answer: $121.3+6.7 \times 10^{2}=7.9 \times 10^{2}$ ]
3. Multiply: 34.2 and $1.5 \times 10^{4}$
[Answer: $34.2 \times 1.5 \times 10^{4}=5.1 \times 10^{5}$ ]

# Appendix B: Accuracy, Precision and Uncertainty 

How tall are you? How old are you? When you answered these everyday questions, you probably did it in round numbers such as "five foot, six inches" or "nineteen years, three months." But how true are these answers? Are you exactly $5^{\prime} 6^{\prime \prime}$ tall? Probably not. You estimated your height at $5^{\prime} 6 "$ and just reported two significant figures. Typically, you round your height to the nearest inch, so that your actual height falls somewhere between $5^{\prime} 5^{1} / 2^{\prime \prime}$ and $5^{\prime} 6^{1 / 2} / 2^{\prime \prime}$ tall, or $5^{\prime} 6^{\prime \prime} \pm 1 / 2^{\prime \prime}$. This $\pm 1 / 2^{\prime \prime}$ is the uncertainty, and it informs the reader of the precision of thevalue $5^{\prime} 6{ }^{\prime \prime}$.

## What is uncertainty?

Whenever you measure something, there is always some uncertainty. There are two categories of uncertainty: systematic and random.
(1) Systematic uncertainties are those that consistently cause the value to be too large or too small. Systematic uncertainties include such things as reaction time, inaccurate meter sticks, optical parallax and miscalibrated balances. In principle, systematic uncertainties can be eliminated if you know they exist.
(2) Random uncertainties are variations in the measurements that occur without a predictable pattern. If you make precise measurements, these uncertainties arise from the estimated part of the measurement. Random uncertainty can be reduced, but never eliminated. We need a technique to report the contribution of this uncertainty to the measured value.

## How do I determine the uncertainty?

This A ppendix will discuss two basic techniques for determining the uncertainty: estimating the uncertainty and measuring the average
deviation. Which one you choose will depend on your need for precision. If you need a precise determination of some value, the best technique is to measure that value several times and use the average deviation as the uncertainty. Examples of finding the average deviation aregiven below.

## H ow do l estimate uncertainties?

If time or experimental constraints make repeated measurements impossible, then you will need to estimate the uncertainty. When you estimate uncertainties you are trying to account for anything that might cause the measured value to be different if you were to take the measurement again. For example, suppose you were trying to measure the length of a key, as in Figure B-1.

Figure B-1


If the true value were not as important as the magnitude of the value, you could say that the key's length was 6 cm , give or take 1 cm . This is a crude estimate, but it may be acceptable. A better estimate of the key's length, as you saw in A ppendix A, would be 5.81 cm . This tells us that the worst our measurement could be off is a fraction of a mm . To be more precise, we can estimate it to be about a third of a mm , so we can say that the length of the key is $5.81 \pm 0.03 \mathrm{~cm}$.

A nother time you may need to estimate uncertainty is when you analyze video data. Figures B2 and B-3 show a ball rolling off the edge of a table. These are two consecutive frames, separated in time by $1 / 30$ of a second.

Figure B-2


Figure B-3


The exact moment the ball left the table lies somewhere between these frames. We can estimate that this moment occurs midway between them ( $t=10 \frac{1}{60} \mathrm{~s}$ ). Since it must occur at some point between them, the worst our estimate could be off by is $\frac{1}{60} s$. We can therefore say the time the ball leaves the table is $t=10 \frac{1}{60} \pm \frac{1}{60} s$.

## How do I find the average deviation?

If estimating the uncertainty is not good enough for your situation, you can experimentally determine the un-certainty by making several measurements and calculating the average deviation of those measurements. To find the average deviation: (1) Find the average of all your measurements; (2) Find the absolute value of the difference of each measurement from the average
(its deviation); (3) Find the average of all the deviations by adding them up and dividing by the number of measurements. Of course you need to take enough measure-ments to get a distribution for which the average has some meaning.

In example 1, a class of six students was asked to find the mass of the same penny using the same balance. In example 2, another class measured a different penny using six different balances. Their results are listed below:

Class 1: Penny A massed by six different students on the same balance.

| Mass (grams) |
| :---: |
| 3.110 |
| 3.125 |
| 3.120 |
| 3.126 |
| 3.122 |
| 3.120 |
| 3.121 average. |
| The deviations are: $0.011 \mathrm{~g}, 0.004 \mathrm{~g}, 0.001 \mathrm{~g}$, |
| $0.005 \mathrm{~g}, 0.001 \mathrm{~g}, 0.001 \mathrm{~g}$ |
| Sum of deviations: 0.023 g |
| Average deviation: |
| (0.023g)/ $6=0.004 \mathrm{~g}$ |
| Mass of penny A: $3.121 \pm 0.004 \mathrm{~g}$ |

Class 2: Penny B massed by six different students on six different balances

| $\frac{\text { Mass (grams) }}{3.140}$ |
| :--- |
| 3.133 |
| 3.144 |
| 3.118 |
| 3.126 |
| $\frac{3.125}{3.131 ~ a v e r a g e ~}$ |
| The deviations are: $0.009 \mathrm{~g}, 0.002 \mathrm{~g}, 0.013 \mathrm{~g}$, |
| 0.013g, $0.005 \mathrm{~g}, 0.006 \mathrm{~g}$ |
| Sum of deviations: 0.048 g |
| Average deviation: |
| (0.048g)/ $6=0.008 \mathrm{~g}$ |
| Mass of penny B: $3.131 \pm 0.008 \mathrm{~g}$ |

However you choose to determine the uncertainty, you should always state your
method clearly in your report. For the remainder of this appendix, we will use the results of these two examples.

## How do I know if two values are the same?

If we compare only the average masses of the two pennies we see that they are different. But now include the uncertainty in the masses. For penny A, the most likely mass is somewhere between 3.117 g and 3.125 g . For penny $B$, the most likely mass is somewhere between 3.123 g and 3.139 g . If you compare the ranges of the masses for the two pennies, as shown in Figure B-4, they just overlap. Given the uncertainty in the masses, we are able to conclude that the masses of the two pennies could be the same. If the range of the masses did not overlap, then we ought to conclude that the masses are probably different.

Figure B-4


M ass of pennies (in grams) with uncertainties

## Which result is more precise?

Suppose you use a meter stick to measure the length of a table and the width of a hair, each with an uncertainty of 1 mm . Clearly you know more about the length of the table than the width of the hair. Your measurement of the table is very precise but your measurement of the width of the hair is rather crude. To express this sense of precision, you need to calculate the percentage uncertainty. To do this, divide the uncertainty in the measurement by the value of the measurement itself, and then multiply by $100 \%$. For example, we can calculate the precision in the measurements made by class 1 and class 2 as follows:

Precision of Class 1's value: $(0.004 \mathrm{~g} \div 3.121 \mathrm{~g}) \times 100 \%=0.1 \%$
Precision of Class 2's value:
$(0.008 \mathrm{~g} \div 3.131 \mathrm{~g}) \times 100 \%=0.3 \%$

Class l's results are more precise. This should not be surprising since class 2 introduced more uncertainty in their results by using six different balances instead of only one.

## Which result is more accurate?

Accuracy is a measure of how your measured value compares with the real value. Imagine that class 2 made the measurement again using only one balance. Unfortunately, they chose a bal ance that was poorly calibrated. They analyzed their results and found the mass of penny $B$ to be 3.556 $\pm 0.004 \mathrm{~g}$. This number is more precise than their previous result since the uncertainty is smaller, but the new measured value of mass is very different from their previous value. We might conclude that this new value for the mass of penny $B$ is different, since the range of the new value does not overlap the range of the previous value. However, that conclusion would be wrong since our uncertainty has not taken into account the inaccuracy of the balance. To determine the accuracy of the measurement, we should check by measuring something that is known. This procedure is called calibration, and it is absolutely necessary for making accurate measurements.

Be cautious! It is possible to make measurements that are extremely precise and, at the same time, grossly inaccurate.

## H ow can I do calculations with values that have uncertainty?

When you do calculations with values that have uncertainties, you will need to estimate (by cal culation) the uncertainty in the result. There are mathematical techniques for doing this, which depend on the statistical properties of your measurements. A very simple way to estimate uncertainties is to find thelargest possible uncertainty the calculation could yield. This will always overestimate the uncertainty of your cal culation, but an overestimate is better than no estimate. The method for performing arithmetic operations on quantitieswith uncertainties is illustrated in the following examples:

## Addition:

$(3.131 \pm 0.008 \mathrm{~g})+(3.121 \pm 0.004 \mathrm{~g})=$ ?
First, find the sum of the values:
$3.131 \mathrm{~g}+3.121 \mathrm{~g}=6.252 \mathrm{~g}$
Next, find the largest possible value:
$3.139 \mathrm{~g}+3.125 \mathrm{~g}=6.264 \mathrm{~g}$
The uncertainty is the difference between the two:
$6.264 \mathrm{~g}-6.252 \mathrm{~g}=0.012 \mathrm{~g}$
A nswer: $6.252 \pm 0.012 \mathrm{~g}$.
Note: This uncertainty can be found by simply adding the individual uncertainties:

$$
0.004 \mathrm{~g}+0.008 \mathrm{~g}=0.012 \mathrm{~g}
$$

## Subtraction:

$(3.131 \pm 0.008 \mathrm{~g})-(3.121 \pm 0.004 \mathrm{~g})=$ ?
First, find the difference of the values:
$3.131 \mathrm{~g}-3.121 \mathrm{~g}=0.010 \mathrm{~g}$
Next, find the largest possible difference:
$3.139 \mathrm{~g}-3.117 \mathrm{~g}=0.022 \mathrm{~g}$
The uncertainty is the difference between thetwo:

$$
0.022 \mathrm{~g}-0.010 \mathrm{~g}=0.012 \mathrm{~g}
$$

## A nswer: $0.010 \pm 0.012 \mathrm{~g}$.

Note: This uncertainty can be found by simply adding the individual uncertainties:

$$
0.004 \mathrm{~g}+0.008 \mathrm{~g}=0.012 \mathrm{~g}
$$

Notice also, that zero is included in this range, so it is possible that there is no difference in the masses of the pennies, as we saw before.

## Multiplication:

$(3.131 \pm 0.013 \mathrm{~g}) \times(6.1 \pm 0.2 \mathrm{~cm})=$ ?
First, find the product of the values:
$3.131 \mathrm{~g} \times 6.1 \mathrm{~cm}=19.1 \mathrm{~g}-\mathrm{cm}$
Next, find the largest possible value:
$3.144 \mathrm{~g} \times 6.3 \mathrm{~cm}=19.8 \mathrm{~g}-\mathrm{cm}$
The uncertainty is the difference between the two:
$19.8 \mathrm{~g}-\mathrm{cm}-19.1 \mathrm{~g}-\mathrm{cm}=0.7 \mathrm{~g}-\mathrm{cm}$

## Answer: $19.1 \pm 0.7 \mathrm{~g}-\mathrm{cm}$.

Note: The percentage uncertainty in the answer is the sum of the individual percentage uncertainties:
$\frac{0.013}{3.131} \times 100 \%+\frac{0.2}{6.1} \times 100 \%=\frac{0.7}{19.1} \times 100 \%$

## Division:

$(3.131 \pm 0.008 \mathrm{~g}) \div(3.121 \pm 0.004 \mathrm{~g})=$ ?
First, divide the values:
$3.131 \mathrm{~g} \div 3.121 \mathrm{~g}=1.0032$
N ext, find the largest possible value:
$3.139 \mathrm{~g} \div 3.117 \mathrm{~g}=1.0071$
The uncertainty is the difference between the two:

$$
1.0071-1.0032=0.0039
$$

## Answer: $1.003 \pm 0.004$

Note: The percentage uncertainty in the answer is the sum of the individual percentage uncertainties:
$\frac{0.008}{3.131} \times 100 \%+\frac{0.004}{3.121} \times 100 \%=\frac{0.0039}{1.0032} \times 100 \%$ Notice also, the largest possible value for the numerator and the smallest possible value for the denominator gives the largest result.

The same ideas can be carried out with more complicated calculations. Remember this will always give you an overestimate of your uncertainty. There are other calculation techniques, which give better estimates for uncertainties. If you wish to use them, pease discuss it with your instructor to see if they are appropriate.

These techniques help you estimate the random uncertainty that al ways occurs in measurements. They will not help account for mistakes or poor measurement procedures. There is no substitute for taking data with the utmost of care. A little forethought about the possible sources of uncertainty can go a long way in ensuring precise and accurate data.

## PRACTICE EXERCISES:

B-1. Consider the following results for different experiments. Determine if they agree with the accepted result listed to the right. Also calculate the precision for each result.
a) $\mathrm{g}=10.4 \pm 1.1 \mathrm{~m} / \mathrm{s}^{2}$

$$
\begin{aligned}
& \mathrm{g}=9.8 \mathrm{~m} / \mathrm{s}^{2} \\
& \mathrm{~T}=1.1 \mathrm{sec} \\
& \mathrm{k}=1300 \pm 50 \mathrm{~N} / \mathrm{m}
\end{aligned}
$$

b) $\mathrm{T}=1.5 \pm 0.1 \mathrm{sec}$
c) $k=1368 \pm 45 \mathrm{~N} / \mathrm{m}$

Answers: a) Yes, 11\%; b) No, 7\%; c) Yes, 3.3\%
B-2. The area of a rectangular metal plate was found by measuring its length and its width. The length was found to be $5.37 \pm 0.05 \mathrm{~cm}$. The width was found to be $3.42 \pm 0.02 \mathrm{~cm}$. What is the area and the average deviation?

Answer: $18.4 \pm 0.3 \mathrm{~cm}^{2}$
B-3. Each member of your lab group weighs the cart and two mass sets twice. The following table shows this data. Calculate the total mass of the cart with each set of masses and for the two sets of masses combined.

| Cart <br> (grams) | M ass set 1 <br> (grams) | M ass set 2 <br> (grams) |
| :---: | :---: | :---: |
| 201.3 | 98.7 | 95.6 |
| 201.5 | 98.8 | 95.3 |
| 202.3 | 96.9 | 96.4 |
| 202.1 | 97.1 | 96.2 |
| 199.8 | 98.4 | 95.8 |
| 200.0 | 98.6 | 95.6 |

Answers:

$$
\begin{array}{ll}
\text { Cart and set 1: } & 299.3 \pm 1.6 \mathrm{~g} . \\
\text { Cart and set 2: } & 297.0 \pm 1.2 \mathrm{~g} . \\
\text { Cart and both sets: } & 395.1+1.9 \mathrm{~g} .
\end{array}
$$

## Appendix C: Graphing

One of the most powerful tools used for data presentation and analysis is the graph. Used properly, graphs are an important guide to understanding the results of an experiment. They are an easy way to make sense out of your data. Therefore, it is important to graph your data as you take it.

LabVIEW $^{\text {™ }}$ will often provide you with a graph, but on occasion you will have to make your own. Good graphing practice, as outlined below, is a way to save time and effort while solving a problem in the laboratory.

## How do I make a graph?

1. Accurate graphs are drawn on graph paper. Even if you are just making a quick sketch for yourself, it will save you time and effort to use graph paper. That is why every page of your lab journal is a piece of graph paper. M ake sure to graph your data as you take it. Never put off drawing a graph until the end.
2. Every graph should have a title to indicate the data it represents. In a large collection of graphs, it is difficult to keep one graph distinct from another without clear, concise titles.
3. The axes of the graph should take up at least half a page. Give yourself plenty of space so that you can see the pattern of the data as it is developing. Both axes should be labeled to show the values being graphed and their appropriate units.
4. The scales on the graphs should be chosen so that the data occupies most of the space of your graph. You do not need to include zero on
your scales unless it is important to the interpretation of the graph.
5. If you have more than one set of data on a set of axes, be sure to label each set to avoid confusion later.

## How do I plot data and uncertainties?

A nother technique that makes data analysis easier is to record all your data in a table.

A useful data table will always include a title and column headings, so that you will not forget what all the numbers mean. The column headings should include the units of the quantities listed, and usually serve as the labels for the axes of your graph. For example, look at Table C-1 and Graph C-1 on the next page. This is a position-versus-time graph drawn for a hypothetical situation.

The uncertainty for each data point is shown on the graph as a line representing a range of possible values with the principal value at the center. The lines are called error bars, and they are useful in determining if your data agrees with your prediction. Any curve (function) that represents your data should pass through your error bars.

Table C-1: Position vs. Time: Exercise 3, Run 1

| Time, sec | Position, cm |
| :---: | :---: |
| 0.1 | $10 \pm 5$ |
| 0.2 | $20 \pm 5$ |
| 0.3 | $30 \pm 5$ |
| 0.4 | $39 \pm 5$ |
| 0.5 | $49 \pm 5$ |
| 0.6 | $59 \pm 5$ |
| 0.7 | $69 \pm 5$ |
| 0.8 | $79 \pm 5$ |
| 0.9 | $89 \pm 5$ |
| 1.0 | $98 \pm 5$ |

## What is a best fit straight line?

If your data points appear to lie on a straight line, then use a clear straight edge and draw a line through all the error bars, making sure the line has as many principal values beneath it as above it. The line does not need to touch any of the principle values. Do not connect the dots. When done correctly, this straight line represents the function that best fits your data.
You can read the slope and intercept from your graph. These quantities usually have important physical interpretations. Some computer programs, such as Excel or Cricket Graph, will determine the best straight line for your data and compute its slope, intercept, and their uncertainties. You should check with your lab instructor, before you use a graphing program to see if it is appropriate. As an example, look at Graph C-1. The dashed lines are possible linear fits, but the solid line is the best fit. Once you have found the best-fit line, you should determine the slope from the graph and record its value.

## How do I find the slope of a line?

The slope of a line is defined as the ratio of the change in a line's ordinate (vertical axis) to the change in the abscissa (horizontal axis), or the "rise" divided by "run." Your text explains slope. For Graph C-1, the slope of the best-fit line will be the change in the position of the object divided by the time interval for that change in position. To find the value of the slope, look carefully at your best-fit line to find points along the line that have coordinates that you can identify. It is usually not a good idea to use your data points for these values, since your line might not pass through them exactly. For example, the best-fit line on Graph $\mathrm{C}-1$ passes through the points ( 0.15 sec , 15 cm ) and ( $1.10 \mathrm{sec}, 110 \mathrm{~cm}$ ). This means the slope of the line is

$$
\begin{aligned}
\text { Slope } & =\frac{110 \mathrm{~cm}-15 \mathrm{~cm}}{1.10 \mathrm{sec}-0.15 \mathrm{sec}}=\frac{95 \mathrm{~cm}}{0.95 \mathrm{sec}} \\
& =100 \frac{\mathrm{~cm}}{\mathrm{sec}}
\end{aligned}
$$

Note that the slope of a position-versus-time graph has the units of velocity.

## How do I find the uncertainty in the slope of a line?

Look at the dashed lines in Graph C-1. These lines are the largest and smallest values of the slopes that can realistically fit the data. The lines run through the extremes in the uncertainties and they represent the largest and smallest possible slopes for lines that fit the data. You can extend these lines and compute their slopes. These are your uncertainties in the determination of the slope. In this case, it would be the uncertainty in the velocity.

How do I get the slope of a curve that is not a straight line?
The tangent to a point on a smooth curve is just the slope of the curve at that point. If the curve is not a straight line, the slope will change from point to point al ong the curve.


To draw a tangent line at any point on a smooth curve, draw a straight line that only touches the curve at the point of interest, without going inside the curve. Try to get an equal amount of
space between the curve and the tangent line on both sides of the point of interest.

The tangent line that you draw needs to be long enough to allow you to easily determine its slope. You will also need to determine the uncertainty in the slope of the tangent line by considering all other possible tangent lines and selecting the ones with the largest and smallest slopes. The slopes of these lines will give the uncertainty in the slope of the tangent line. Notice that this is exactly like finding the uncertainty of the slope of a straight line.

## How do I "linearize" my data?

A straight-line graph is the easiest graph to interpret. By seeing if the slope is positive, negative, or zero you can quickly determine the relationship between two measurements. But not all the relationships in nature produce straight-line graphs. However, if we have a theory that predicts how one measured quantity (e.g., position) depends on another (e.g., time) for the experiment, we can make the graph be a straight line. To do this, you make a graph with the appropriate function of one quantity on one axis (e.g., time squared) and the other quantity (e.g., position) on the other axis. This is called "linearizing" the data.

For example, if a rolling cart undergoes constant acceleration, the position-versus-time graph is curved. In fact, our theory tells us that the curve should be a parabola. To be concrete we will assume that your data starts at a time when the initial velocity of the cart was zero. The theory predicts that the motion is described by $x=1 / 2 a t 2$. To linearize this data, you square the time and plot position versus time squared. This graph should be a straight line with a slope of $0.5 a$. N otice that you can only linearize data if you know, or can guess, the
relationship between the measured quantities involved.

## How do I interpret graphs from LabVIEW"?

Graphs C-2 through C-4 were produced with LabVIEW ${ }^{\prime \prime \prime}$. They give the horizontal position as a function of time. Even though LabVIEW ${ }^{\text {m }}$ draws the graphs for you, it usually does not label the axes and never puts in the uncertainty. You must add these to the graphs yourself.

One way to estimate the uncertainty is to observe how much the data points are scattered from a smooth behavior. By estimating the average scatter, you have a fair estimate of the data's uncertainty. Graph C-2 shows position versus time for a moving cart. The vertical axis is position in cm and the horizontal axis is time in seconds. See if you can label the axes appropriately and estimate the uncertainty for the data.


Finding the slope of any given curve with LabVIEW ${ }^{\text {m }}$ should be easy after you have chosen the mathematical equation of the best-fit curve. Graphs C-3 and C-4 each show one possible line to describe the same data. From looking at these graphs, the estimate of the data's uncertainty is less than the diameter of the circles representing that data.


The line touching the data points in Graph C-3 has a slope of $0.38 \mathrm{~m} / \mathrm{sec}$. This is the minimum possible slope for a line that fits the given data.


The line touching the data points in Graph C-4 shows a slope of $0.44 \mathrm{~m} / \mathrm{sec}$. This is the maximum possible slope for a line that fits the given data.You can estimate the uncertainty by calculating the average difference of these two slopes from that of the best-fit line. Therefore the uncertainty determined by graphs $\mathrm{C}-3$ and $\mathrm{C}-4$ is $\pm 0.03 \mathrm{~m} / \mathrm{sec}$.

## PRACTICE EXERCISES

Explain all graphing mistakes (if any) on the plots bel ow.



APPENDIX C: GRAPHING

## Appendix D: Video A nalysis of M otion

A nalyzing pictures (movies or videos) is a powerful tool for understanding how objects move. Like most forms of data, video is most easily analyzed using a computer and data acquisition software. This appendix will guide a person somewhat familiar with WindowsNT through the use of one such program: the video analysis application written in LabVIEW ${ }^{\top M}$. LabVIEW ${ }^{T M}$ is a generalpurpose data acquisition programming system. It is widely used in academic research and industry. We will also use LabVIEW ${ }^{\top M}$ to acquire data from other instruments throughout the year.


Using video to analyze motion is a two-step process. The first step is recording a video. This process uses the video software to record the images from the camera and compress the file. The second step is to analyze the video to get a kinematic description of the recorded motion.

## (1) MAKING VIDEOS

After logging into the computer, open the video recording program by double clicking the icon on the desktop abeled VideoRECORDER. A window similar to the picture on the previous page should appear.

If the camera is working, you should see a "live" video image of whatever is in front of the camera. (See your instructor if your camera is not functioning and you are sure you turned it on.) By adjusting the lens on the video camera, you can alter both the magnification and the sharpness of the image until the picturequality is as good as possible.

The controls are fairly self-explanatory; pressing the Record Video button begins the process of recording a 5 -second video image. While the video is recording, the blue Progress bar beneath the video frame grows. Once you have finished recording, you can move through the video by dragging the Frame Number slider control. If you are not pleased with your video recording, delete it by pressing the D ispose button.

You may notice that the computer sometimes skips frames. You can identify the dropped frame by playing the video back frame by frame. If the recorded motion does not appear smooth or if the object moves irregularly from frame to frame, then frames are probably missing. If the computer is skipping frames, speak with your instructor.

While you are recording your video, you should try to estimate the kinematic variables you observe, such as the initial position, velocities, and acceleration. The time with the unit of second is shown in the VideoRECORDER window, in the box below the Frame N umber slider. These values prove very useful for your prediction equations. Be sure to record your estimates in your journal.

Once you have recorded a satisfactory video, save it by pressing the SaveV ideo button. You will see a Savewindow, as shown on the next page.

To avoid cluttering the computer, you will only be able to save your video to certain folders on the hard disk. One such folder is the M y Documents folder located on the C drive. You should check with your lab instructor for the most suitable place to save your video. In the File name box, you should enter the location of the folder in which you wish to save your video followed by the name that you wish to give to your video. This name should be descriptive enough to be useful to you later (see the picture for an example).


## (2) AN ALYSIS BASICS

Open the video analysis application by clicking the icon labeled VideoTOOL, which is located on the desktop. You should now take a moment to identify several elements of the program.
The two most important of these are the Program Controls panel shown to the right and the Instructions box shown below.


These two elements of the analysis program work in tandem. The Instructions box will give you directions and tasks to perform. It will also tell you when to select a control in the Program Controls panel. After you select a control, it will "gray out" and the next control will become available. If you make a
 mistake, you cannot go backwards! You would have to quit your analysis and reopen the video to begin afresh.

You print and/ or quit the video analysis from theP rogram Controls panel. You also have the option to save the data to continue later, or to save a data table.

Be careful not to quit without printing and saving your data! You will have to go back and analyze the data again if you fail to select Print Results before selecting Q uit P rogram or Return to Beginning. Also be sure to save the data (Save All) and save the data table (SaveD ata Table).

## CALIBRATION

While the computer is a very handy tool, it is not smart enough to identify objects or the sizes of those objects in the videos that you take and analyze. For this reason, you will need to enter this information into the computer. If you are not careful in the calibration process, your analysis will not make any sense.

After you open the video that you wish to analyze and select Begin Calibration from the Program C ontrols panel you will be advised in the Instructions box "To begin Calibration, advance the video to a frame where the first data point will be taken. The time stamp of this frame will be used as the initial time." To advance the video to where you want time $t=0$ to be, you need to use the video control buttons, shown below. This action is equival ent to starting a stopwatch.


Practice with each button until you are proficient with its use. When you are ready to continue with the calibration, locate the object you wish to use to calibrate the size of the video. The best object to use is the object whose motion you are analyzing, but sometimes this is not easy. If you cannot use the object whose motion you are analyzing, you must do your best to use an object that is in the plane of motion of your object being analyzed.

Follow the direction in the Instructions box and define the length of an object that you have measured for the computer. Once this is completed, input the scale length with proper units in Calibration Controls box (shown below). Read the directions in the Instructions box carefully. Enter the scal e length, and then use the arrows to select the units you are using.


Lastly, decide if you want to rotate your coordinate axes. If you choose not to rotate the axes, the computer will choose the lower left-hand corner of the video to be the origin with positive $x$ to the right and positivey up. If you choose to rotate your axis, follow the directions in the Instructions box carefully. Your chosen axes will appear under the Calibration Controls box. This option may also be used to reposition the origin of the coordinate system, should you require it.

Once you have completed this process, select "OK" from the Calibration C ontrols box.

## ANALYSIS PREDICTIONS

This video analysis relies on your graphical skills to interpret the data from the videos. Before doing your analysis, you should be familiar with both Appendix C: Graphing and Appendix B: Uncertainties.

Before analyzing the data, enter your prediction of how you expect the data to behave. This pattern of making predictions before obtaining results is the only reliable way to take data. How else can you know if something has gone wrong? This happens so often that it is given a name (M urphy's Law). It is also a good way to make sure you have learned something, but only if you stop to think about the discrepancies or similarities between your prediction and the results.

In order to enter your prediction into the computer, you first need to decide on your coordinate axes, origin, and scale(units) for your motion. Record these in your lab journal.

Next you will need to select the generic equation, $u(t)$, which describes the graph you expect for the motion al ong your x-axis seen in your video. You must choose the appropriate function that matches the predicted curve. The analysis program is equipped with several equations, which are accessible using the pull-down menu on the equation line (shown to the right).

You can change the equation to one you would like to use by clicking on the arrows to the left of the equation in the Prediction Equation command box, shown to the right. Holding down the mouse button will give you the menu also shown to the right.

After selecting your generic equation, you next need to enter your best approximation for the parameters $A$ and $B$ and $C$ and $D$ where you need them. If you took good notes of these values during the filming of your video, inputting these values should

| Prediction Equation |  |
| :---: | :---: |
| 2) $\mathrm{u}(\mathrm{t})=\mathrm{A}+\mathrm{B}$ t |  |
| त 00.00 A $\frac{1}{5} 0.00$ | 0.00 D |
| $\frac{7}{5} 17.00$ B $\frac{2}{5} 0.00$ | 7 0.00 E |
| $\frac{2}{5} 0.00$ c $\frac{2}{5} 0.00$ | \% 00.00 F Predictions |
| $\checkmark u[t]=A+B t$ |  |
| $u(t)=A+B t+C t^{\wedge} 2+D t^{\wedge} 3$ |  |
| $u(t)=A+B t+C t^{\wedge} 2+D t^{\wedge} 3+E \wedge^{\wedge} 4$ |  |
| $u(t)=A+B \sin \left(C+D t+E t^{\wedge} 2\right)$ |  |
| $\left.u[t]=A+B \cos (C+D)+E t^{\wedge} 2\right)$ |  |
| $u(t)=A+B \exp (-C t)$ |  |
| $u[t]=A+B(1-\exp (-C t)]$ |  |
| $u(t)=A+(B+C t) \sin \left(D+E t+F t^{\wedge} 2\right)$ |  |
| $u(t)=A+(B+C$ t $) \cos$ | t) $\cos (\mathrm{D}+\mathrm{Et}+\mathrm{Ft} 2)$ | be straightforward. You will also need to decide on the units for these constants at thistime.

Once you are satisfied that the equation you selected for your motion and the values of the constants are correct, click 'Predictions" in the Prediction Equation command box. Your prediction equation will then show up on the graph on the computer screen. If you wish to change your prediction simply repeat the above procedure. When you are satisfied, select theA ccept $x$ - (or $y$-) prediction option from theP rogram Controls panel. Once you have done this you cannot change your prediction except by starting over. Repeat this procedurefor the $Y$ direction.

## DATA COLLECTION

To collect data, you first need to identify a very specific point on the object whose motion you are analyzing. Next move the cursor over this point and click the green A ccept D ata Point button in VideoPLAYER window. The computer records this position and time. The computer will automatically advance the video to the next frame leaving a mark on the point you have just selected. Then move the cursor back to the same place on the object and click Accept Data Point button again. So long as you always use the same point on the object, you will get reliable data from your analysis. This process is not always so easy especially if the object is moving rapidly. Because the camera has an interlaced scan of the image, it actually gives you two images. For a rapidly moving object, these images split apart. You need to keep track of which image you are measuring for each picture frame. The data will automatically appear on the appropriate graph on your computer screen each time you accept a data point. If you don't seethe data on the graph, you will need to change the scale of the axes. If you are satisfied with your data, choose A nalyze D ata from the Program Controls panel.

## FITTING YOUR DATA

Deciding which equation best represents your data is the most important part of your data analysis. The actual mechanics of choosing the equation and constants is similar to what you did for your predictions.

First you must find your data on your graphs. Usually, you can find your full data set by adjusting the scales of your $X$-motion and $Y$ motion plots. This scaling is accomplished by entering the appropriate maximum and minimum values on the vertical axis (as shown to the right) as well as adjusting the time scale.


Secondly, after you find your data, you need to determine the best possible equation to describe this data. After you have decided on the appropriate equation, you need to determine the constants of this equation so that it best fits the data. Although this can be done by trial and error, it is much more efficient to think of how the behavior of the equation you have chosen depends on each parameter. Calculus can be a great help here.


As an example of a completed determination of the equation, the X-motion plot above shows both the predicted line (down) and the line that best fits the data (through the circles). Be sure to record the values of your parameters in your journal before you go on to the next stage.

Lastly, you need to estimate the uncertainty in your fit by deciding the range of other lines that could also fit your data. This method of estimating your uncertainty is described in Appendix C. Slightly changing the values for each constant in turn will allow you to do this quickly. For example, the Xmotion plots below show both the predicted line (down) and two other lines that also fit the data (near the circles).


After you have found the uncertainties in your constants, return to your best-fit line and use it as your fit by selecting A ccept $x$ - (or $y-$ ) fit in the Program Controls panel.

## LAST WORDS

These directions are not meant to be exhaustive. You will discover more features of the video analysis program as you use it. Be sure to record these features in your lab journal.

## Appendix E: Sample Laboratory Report

There is no set length for a problem report but experience shows good reports are typically four pages long. Graphs and photocopies of your lab journal make up additional pages. Complete reports will include the terminology and the mathematics relevant to the problem at hand. Your report should be a clear, concise, logical, and honest interpretation of your experience. You will be graded based on how well you demonstrate your understanding of the physics. Because technical communication is so important, neatness, and correct grammar and spelling are required and will be reflected on your grade.
||Note: As with Problem 1 of Lab 1, the double vertical bars indicate an explanation of that part of the report. These comments are not part of the actual report.

Usually a lab report consists of the following parts:

- Title,
- Statement of the Problem,
- Prediction,
- Experiment and Results,
- Conclusions,
- References.

In this appendix there are three sample lab reports, which are based on the actual lab reports written by students who took this course before. Our main goal of putting them here is to give you some information about writing lab reports. Basically, any lab report is a simplified version of a research paper or technical report. Therefore, it is written in a scientific style and it has the same main parts as a research paper/ technical report. As you go from \#1 to \#3, you'll notice the improvement in the quality of the samples. This is typical level of improvement of the students taking this course. Your goal is to be able to write such lab reports as sample \#3 after completing this course.

It's useful to read the sample lab reports after completing the following laboratories in class:

- Sample \# 1 after Projectile Motion;
- Sample \#2 after Conservation of Energy;
- Sample \#3 after Rotational Motion.


## Sample Lab Report \#1

## Title

|| Write a descriptive title with your name, names of partners, date performed and TA name.

Projectile M otion
September 27, 2003

Performed by: Roman Ivanov, Tom Johnson and Mun Tiang
TA name: Ken Spillner

## Statement of the problem

|In a sentence or two, state the problem you are trying to solve. List the equipment you will use and the reasons for selecting such equipment.

The problem was to determine the dependence of the time of flight of a projectile on its initial horizontal velocity. We rolled an aluminum ball down a ramp and off the edge of a table starting from rest at two different positions along the ramp. Starting from the greater height up the ramp meant the ball had a larger horizontal velocity when it rolled al ong the table. Since the table was horizontal, that was the horizontal velocity when it entered the air. See Figure 1 from my lab journal for a picture of the set-up.

We made two movies with the video equipment provided, one for a fast rolling ball and one for a slower one. These movies were analyzed with LabVIEWTM to study the projectile's motion in the horizontal and vertical directions.

## Prediction

This is the part of the lab where you try to predict the outcome of the experiment based on your general knowledge of Physics. If your predictions were wrong and you understood it during the lab, write correct ones in your lab report. Also, attach initial predictions to your lab report and explain what was wrong. If you still have problems with the prediction, ask your TA or go to TA office hours for some help. Generally, predictions are based on the fundamental laws or principles. Therefore, refer to these laws as a starting point of your predictions.

Our group predicted that the time the ball took to hit the ground once it left the table would be greater if the horizontal velocity were greater. We have observed that the faster a projectile goes initially, the longer its trajectory. Since the gravitational acceleration is constant, we reasoned that the ball would take more time to travel a larger distance. However, after completing the lab we understood that horizontal and vertical motion is independent. Therefore, for two given cases where the object had different initial horizontal velocity, the time of flight was the same. So, our initial predictions were wrong.
|Presentation of your lab report is an important part of the evaluation process. It has to be written in a clear and understandable way for your peers, TAs and Professors. We recommend using Microsoft Word for writing lab reports, especially for its handy tool - Equation Editor. Equation Editor allows you to type complicated mathematical expressions in a compact and elegant way. In order to use this tool go to Insert $\mathbf{M}$ enu $\rightarrow \mathbf{O}$ bject $\rightarrow \mathbf{M}$ icrosoft Equation 3.0.

M athematically, we start from the definition of acceleration:

$$
\mathbf{a}=\frac{d}{d t}\left(\frac{d y}{d t}\right)
$$

and integrate twice with respect to time to see how a change in time might be related to initial velocity. We found that:

$$
\begin{equation*}
y-y o=v o \Delta t+0.5 a \Delta t^{2} \tag{1}
\end{equation*}
$$

In this example, the student is explaining incorrect predictions. Although motion is twodimensional, he/she is using $\boldsymbol{V}_{0}$ while correct notation is $\boldsymbol{v}_{0 y}$ as it is a projection of velocity onto yaxis.

With the y-axis vertical and the positive direction up, we know the acceleration is -g. We also know that vo is the initial velocity, and yo-y ish, the height of the table. Solving for $\Delta$ t one finds:

$$
\begin{equation*}
\Delta t=\frac{\mathrm{vo} \pm \sqrt{\left(\mathrm{vo}^{2}+2 \mathrm{hg}\right)}}{\mathrm{g}} \tag{2}
\end{equation*}
$$

Faced with a choice in sign, our group chose the solution with the positive sign, deciding that a possible negative value for elapsed time does not correspond with our physical situation. From equation (2), we deduced that if vo increased, then the time of fall also increases. This coincided with our prediction that a projectile with fastest horizontal velocity would take the most time to fall to the ground. For a graph of our predicted time of flight versus initial horizontal velocity, see Graph A from the lab journal.

LabVIEW ${ }^{\text {TM }}$ generated graphs of $x$ and $y$ positions as functions of time. Our prediction for the vertical direction was equation (1). Since the ball only has one acceleration, we predicted that equation (1) would also betruefor the horizontal motion:

$$
\mathrm{x}-\mathrm{xo}=\mathrm{vo} \Delta \mathrm{t}+0.5 \mathrm{a} \Delta \mathrm{t}^{2}
$$

The dotted lines on the printed graphs represent these predictions.

[^1]Our TA asked us to compare a bullet fired horizontally from a gun to a bullet dropped vertically. Our group decided the bullet that is fired horizontally will takelonger to hit the ground than the one that is simply dropped from the same height.

## Experiment and results

|This section describes your experimental method, the data that you collected, any problems in gathering the data, and any crucial decisions you made. Your actual results should show you if your prediction was correct or not.

To ensure the ball's velocity was completely horizontal, we attached a flat plank at the end of the ramp. The ball rolls down the ramp and then goes onto the horizontal plank. After going a distance ( 75 cm ) al ong the plank, the ball leaves the edge of the table and enters projectile motion.

We measured the time of flight by simply counting the number of video frames that the ball was in the air. The time between frames is $1 / 30$ of a second since this is the rate a video camera takes data. This also corresponds to the time scale on the LabVIEWTM graphs. We decided to compare the times of flight between a ball with a fast initial velocity and one with a slow initial velocity. To get a fast velocity we started the ball at the top of the ramp. A slower velocity was achieved by starting the ball almost at the bottom of the ramp.

During the time the ball was in the air, the horizontal velocity was a constant, as shown by the velocity in the $x$-direction graphs for slow and fast rolling balls. From these graphs, the slowest velocity we used was $1.30 \mathrm{~m} / \mathrm{s}$, and the fastest was $2.51 \mathrm{~m} / \mathrm{s}$.

After making four measurements of the time of flight for these two situations, we could not see any correspondence between time of flight and initial horizontal velocity (seetable 1 from lab journal). As a final check, we measured the time of flight for a ball that was started approximately halfway up the ramp and found it was similar to thetimes of flight for both the fast and the slow horizontal velocities (seetable 2 from lab journal).

A discussion of uncertainty should follow all measurements. No measurement is exact. Uncertainty must be included to indicate the reliability of your data.

Most of the uncertainty in recording time of flight came from deciding the time for the first data point when the ball is in the air and the last data point before it hit the ground. We estimated that we could be off by one frame, which is $1 / 30$ of a second. To get a better estimate of this uncertainty, we repeated each measurement four times. The average deviation served as our experimental uncertainty (see Table 1 from lab journal). This uncertainty matched our estimate of how well we could determine the first and the last frame of the projectile trajectory.

## Conclusions

|This section summarizes your results. In the most concise manner possible, it answers the original question of the lab.

Our graph indicates that the time of flight is independent of the ball's initial horizontal velocity (see lab journal, Graph A). We conclude that there is no relationship between these two quantities.
||A good conclusion will always compare actual results with the predictions. If your prediction was incorrect, then you must discuss where your reasoning went wrong. If your prediction was correct, then you should review your reasoning and discuss how this lab served to confirm your knowledge of the basic physical concepts.

Our prediction is contradicted by the apparent independence of the time of flight and initial horizontal velocity. We thought that the ball would take longer to fall to the floor if it had a greater initial horizontal velocity. After some discussion, we determined the uncertainty in our prediction. We did not understand that the vertical motion is completely independent of the horizontal motion. Thus, in the vertical direction the equation

$$
y-y o=v o \Delta t+0.5 a \Delta t^{2}
$$

means that the vo is the only the $y$-component of initial velocity. Since the ball rolls horizontally at the start of its flight, vo in this equation always equals zero.

The correct equation for the time of flight, with no initial vertical component of velocity, is actually:

$$
\mathrm{y}-\mathrm{yo}=0.5 \mathrm{a} \Delta \mathrm{t}^{2}
$$

In this equation, there is no relationship between time of flight and initial horizontal velocity.
Furthermore, the graphs we generated with LabVIEWтм showed us that velocity in the $y$-direction did not change when the initial horizontal velocity changed. Velocity in the ydirection is always approximately zero at the beginning of the trajectory. It is not exactly zero because of the difficulty our camera had determining the position when the projectile motion begins. We observed that the $y$ velocity changed at the same rate (slope of $v_{y}$ plots, graphs 1 and 2 ) regardless of the horizontal velocity. In other words, the acceleration in the $y$-direction is constant, a fact that confirms the independence of vertical and horizontal motion.

After you have compared your predictions to your measured results, it is helpful to use an alternative measurement to check your theory with the actual data. This should be a short exercise demonstrating to yourself and to your TA that you understand the basic physics behind the problem. Most of the problems in lab are written to include alternative measurements. In this case, using the time of fall and the gravitational constant, you can cal culate the height of thetable.

The correct equation for the horizontal motion is

$$
x-x_{0}=v_{0} \Delta t
$$

The horizontal acceleration is always zero, but the horizontal distance that the ball covers before striking the ground does depend on initial velocity.

```
**Alternative A nalysis**
```

Since yo $-\mathrm{y}=\mathrm{h}$ and $\mathrm{a}=-\mathrm{g}$ we can check to see if our measured time of flight gives us the height of the table. From our graph, we see that the data overlaps in a region of about 0.41 sec . With this as our time of flight, the height of the table is calculated to be 82.3 cm . Using a meter stick, we found the height of the table to be 80.25 cm . This helped convince us that our final reasoning was correct.

The example of the two bullets discussed in the Prediction section was interpreted incorrectly by our group. Actually, both bullets hit the ground at the same time. One bullet travels at a greater speed, but both have the same time of flight. Although this seems to violate "common sense" it is an example of the independence of the horizontal and vertical components of motion.

## References

||List books, journals or any other resources that you used to write your lab report..

1. Tipler, Paul A. Physics for Scientists and Engineers. 4th, W. H. Freeman: 1999.

The following are pages photocopied from my lab journal:


Equipment: ramp, aluminum ball, video camera, computer, meterstick

Purpose: Determine if Time of flight depends on initial horizontal velocity
Method: One person releases ball, another operates vided camera. Count frames with ball in the air to find time of flight.
Exploration: Larger $H$ results in larger horizontal $\vec{v}$.

Table 1
Fast Ball, $H \simeq 35 \mathrm{~cm}, v_{0}=2.51 \mathrm{~m} / \mathrm{s}$

| Trial | Frames with | Deviation |
| :---: | :---: | :---: |
|  | ball in air | from are. |
| 1 | 13 | 0.25 |
| 2 | 13 | 0.25 |
| 3 | 12 | 0.75 |
| 4 | 13 | 0.25 |
| Average | 12.75 | 0.4 |

Time of flight:

$$
12.75 \text { frames } \times \frac{1}{30} \frac{\mathrm{sec}}{\text { frame }}=
$$

$$
0.42 \mathrm{sec}
$$

Uncertainty:

$$
\pm 0.4 \text { frames } \times \frac{1}{30} \frac{\mathrm{sec}}{\text { frame }}=
$$

$$
\pm 0.014 \mathrm{sec}
$$

Slow Ball, $H \simeq 10 \mathrm{~cm}, v_{0}=1.3 \mathrm{~m} / \mathrm{s}$

| 1 | 12 | 0.5 |
| :---: | :---: | :---: |
| 2 | 13 | 0.5 |
| 3 | 13 | 0.5 |
| 4 | 12 | 0.5 |
| Average | 12.5 | 0.5 |

Time of flight:

$$
12.5 \text { frames } \times \frac{1}{30} \frac{\text { sec }}{\text { frame }}=
$$

0.41 sec

Uncertainty

$$
\begin{array}{r} 
\pm 0.5 \times 1 / 30 \frac{\mathrm{sec}}{\text { frame }}= \\
\pm 0.018 \mathrm{sec}
\end{array}
$$

Table 2
Medium Ball, $H \simeq 20, v_{0}=1.8 \mathrm{~m} / \mathrm{s}$

| Trial | $\#$ frames | Deviation |
| :---: | :---: | :---: |
| 1 | 12 | 0.5 |
| 2 | 12 | 0.5 |
| 3 | 13 | 0.5 |
| 4 | 13 | 0.5 |
| Average | 12.5 | 0.5 |

Time of flight:

$$
12.5 \text { frames } \times \frac{1}{30} \frac{\text { see }}{\text { frames }}=
$$

$$
0.41 \mathrm{sec}
$$

$U_{\text {neertainty }}= \pm 0.5 \times \frac{1}{30} \frac{\mathrm{sec}}{\text { frame }}=$

$$
\pm 0.018 \mathrm{sec}
$$










|  | 2wos'6- $+7090+920=(1) N$ |
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## Title

|| Write a descriptive title with your name, names of partners, date performed and TA name.

# Efficiency of the bumper derived using inclined track O ctober 16, 2003 

Performed by: Roman Ivanov, Tom Johnson and Mun Tiang

TA name: Ken Spillner

## Statement of the problem

This is an introduction to the problem. In a paragraph or two, state the problem you are trying to solve and what you expect to learn from it. List the equipment you will use and reasons for selecting such equipment.

In this lab our goal was to estimate the efficiency of the magnetic bumper. To do so we used an inclined track experiment. Our group released the cart from certain height and took a video of the carts motion before and after collision. The acceleration of the cart up and down the ramp was determined using video analysis. Using this data we were able to calculate efficiency of the magnetic bumper.

## Prediction

This is the part of the lab where you try to predict the outcome of the experiment based on your general knowledge of Physics. If your predictions were wrong and you understood it during the lab, write correct ones in your lab report. Also, attach initial predictions to your lab report and explain what was wrong. If you still have problems with the prediction, ask your TA or go to TA office hours for some help.

Generally, predictions are based on thefundamental laws or principles. Therefore, refer to theselaws as a starting point of your predictions (For example, if you are dealing with dynamics and forces, you can mention N ewton's Second Law as a starting point).

Presentation of your lab report is an important part of the evaluation process. It has to be written in a clear and understandable way for your peers, TAs and Professors. We recommend using Microsoft Word for writing lab reports, especially for its handy tool - Equation Editor. Equation Editor allows you to type complicated mathematical expressions in a compact and elegant way. In order to use this tool go to Insert M enu $\rightarrow \mathbf{O}$ bject $\rightarrow \mathbf{M}$ icrosoft Equation 3.0.

To find the efficiency of magnetic bumper we used conservation of energy:

$$
E_{\text {before }}=E_{\text {affer }}+E_{\text {bumper }}
$$

Kinetic energy before ( $E_{\text {before }}$ ) and after ( $E_{\text {after }}$ ) collision is determined by potential energy and work done by the frictional force: $E_{\text {before }}=m g h_{i}-W_{\text {before }}, E_{\text {after }}=m g h_{f}+W_{\text {after }}$, where $W_{\text {before }}$ and $W_{\text {after }}$ is work done by the frictional force before and after collision, $m$ is mass of the cart, $h_{i}, h_{f}$ are initial and final heights (see Fig. 1 below). The efficiency of the bumper is calculated using the following formula

$$
e f f=\frac{E_{\text {after }}}{E_{\text {before }}} .
$$



Fig. 1. Cart going down the track, bounces with the bumper and going back.
Initial and final potential energies can be determined experimentally by measuring the initial and final heights. Work done by the friction is found assuming that the frictional force is constant up and down the ramp: $W_{\text {before }}=F_{\text {friction }} L_{\text {down }}, W_{\text {after }}=F_{\text {friction }} L_{\text {after }}$, where $L_{\text {down }}, L_{u p}$ are distances down (before collision) and up (after collision) the ramp. The distances are known, so we have to derive the expression for the force of friction in terms of the measured quantities.
Let's apply Newton's Second Law to two cases: when the cart is moving down the track and up. See Fig. 2 for the Force diagrams.

$$
\sum_{i} \vec{F}_{i}=m \vec{a}
$$



Fig. 2. Force diagram for two cases: cart going down and up. Notice the difference in the force of friction.

In rotated system of coordinates $\sum_{i} F_{i y}=0$ and $\sum_{i} F_{i x}=m a_{x}$. From herewe concluded that we can find force of friction in terms of the measured accelerations. Taking into account that the force of friction always opposes the motion, we find the following relations for the motion up and down the ramp:

$$
\left\{\begin{array}{l}
m a_{u p}=m g \sin \theta+F_{\text {friction }} \\
m a_{\text {down }}=m g \sin \theta-F_{\text {friction }}
\end{array} \Rightarrow F_{\text {friction }}=m\left(a_{u p}-a_{\text {down }}\right) / 2\right.
$$

Acceleration up and down the ramp can be determined from video analysis. Substituting above expressions for $E_{\text {after }}$ and $E_{\text {before }}$, efficiency of the magnetic bumper is

$$
e f f=\frac{m g h_{f}+\frac{m}{2}\left(a_{u p}-a_{d o w n}\right)^{*} L_{u p}}{m g h_{i}-\frac{m}{2}\left(a_{u p}-a_{d o w n}\right)^{*} L_{\text {down }}}
$$

After simplifying our group got the following expression:

$$
\text { eff }=\frac{L_{u p}}{L_{\text {down }}} * \frac{g \sin \theta+\left(a_{u p}-a_{\text {down }}\right) / 2}{g \sin \theta-\left(a_{u p}-a_{\text {down }}\right) / 2}
$$

## Experiment and results

This section describes your experimental method, the data that you collected, any problems in gathering the data, and any crucial decisions you made. Briefly discuss your setup and explain how you collected your data. Present information in a clear way either in tables or graphs. Make sure you have correct units shown on the graphs. Include all information that you used in the lab to calculate some final results so that we can repeat the calculations and see whether this step is correct or not. In order to arrive at a valid conclusion in testing a theory or hypothesis it is necessary to understand the underlying concepts of measurement uncertainties. Calculate your uncertainties and indicate the
||largest contribution to uncertainty. Finally, compare the experimental results and theoretical prediction. Discuss any agreement or disagreement between them.

In order to find the efficiency of the bumper we released the cart from initial height $h_{i}$ and took the video of the motion. Also, we determined the final height the cart reached. For practical reasons it is easier to measure the distances from the bumper which are related to the height $h=L \sin \theta$. Then we analyzed the video and figured out the acceleration before and after collision by fitting the position versus time curve. Experimental data is given in Table 1 and Table 2:

| Before collision | After collision |
| :--- | :--- |
| $L_{i}=80 \mathrm{~cm}$ | $L_{f}=64 \mathrm{~cm}$ |
| $a_{\text {down }}=39 \mathrm{~cm} / \mathrm{s}^{2}$ | $a_{u p}=44 \mathrm{~cm} / \mathrm{s}^{2}$ |
| $\theta=3^{\circ}$ | $\theta=3^{\circ}$ |

Table. 1. Summary of experimental results.

Having necessary information from our experiment we are ready to calculate the efficiency:

$$
\text { eff }=\frac{0.64 \mathrm{~m}}{0.8 \mathrm{~m}} * \frac{9.88 \mathrm{~m} / \mathrm{s}^{2} * \sin 3^{\circ}+\frac{1}{2}\left(0.44 \mathrm{~m} / \mathrm{s}^{2}-0.39 \mathrm{~m} / \mathrm{s}^{2}\right)}{9.88 \mathrm{~m} / \mathrm{s}^{2} * \sin 3^{\circ}-\frac{1}{2}\left(0.44 \mathrm{~m} / \mathrm{s}^{2}-0.39 \mathrm{~m} / \mathrm{s}^{2}\right)}=0.85
$$

So the efficiency of the bumper is $85 \%$. The uncertainty in this experiment basically comes from measuring the distance (uncertainty of the meter $\pm 0.5 \mathrm{~cm}$ ), from analyzing the motion (uncertainty related to the video analysis can beestimated by clicking on the same point on the car's image and recording its position) and fitting the experimental curve (uncertainty caused by the fitting of experimental points can be estimated by finding the largest deviation of the experimental point from the fitted curve or by varying the constants, for example acceleration, so that your equation still fits the data). Our group estimated uncertainty to be around $10 \%$.
|For more information on uncertainty see A ppendix B.

## Conclusions

|This section summarizes your results. In the most concise manner possible, it answers the original question of the lab. A good conclusion will always compare actual results with the predictions. If your prediction was incorrect, then you must discuss where your reasoning went wrong. If your prediction was correct, then you should review your reasoning and discuss how this lab served to confirm your knowledge of the basic physical concepts.

In this lab we determined the efficiency of a magnetic bumper. After completing the experiment we concluded that magnetic bumper is very efficient ( $85 \%$ ). Our conclusion is consistent with the previous lab results. Results check - efficiency of the bumper is indeed less than $100 \%$, so our results make sense in terms of energy conservation.

## References

List books, journals or any other resources that you used to write your lab report.

1. Tipler, Paul A. Physics for Scientists and Engineers. 4th, W. H. Freeman: 1999.


Table 2. Experimental results from video analysis.

## Title

|| Write a descriptive title with your name, names of partners, date performed and TA name.

# O scillation Frequency with Two Springs 

June 7, 2004

Performed by: Roman Ivanov, Tom Johnson and Mun Tiang
TA name: Ken Spillner

## Statement of the problem

This is an introduction to the problem. In a paragraph or two, state the problem you are trying to solve and what you expect to learn from it. List the equipment you will use and reasons for selecting such equipment.

The problem was to determine the frequency of oscillation of the cart attached to two springs with different spring constants. Our group built a laboratory model as shown below:


Fig. 1. Experimental setup: cart attached to two springs with different spring constants.

We displaced the cart from equilibrium and then gently released it. The period of the oscillation was determined using a stop watch and video analysis. The cart was selected because it rolls with low friction; neglecting friction simplified our analysis. Video analysis provides precise measurements of the period, and the stopwatch provides an alternative method of checking the period.

## Prediction

This is the part of the lab where you try to predict the outcome of the experiment based on your general knowledge of Physics. If your predictions were wrong and you understood it during the lab, write correct ones in your lab report. Also, attach initial predictions to your lab report and explain what was wrong. If you still have problems with the prediction, ask your TA or go to TA office hours for some help.

Generally, predictions are based on the fundamental laws or principles. Therefore, refer to these laws as a starting point of your predictions (For example, if you are dealing with dynamics and forces, you can mention N ewton's Second Law as a starting point).

Presentation of your lab report is an important part of the evaluation process. It has to be written in a clear and understandable way for your peers, TAs and Professors. We recommend using Microsoft Word for writing lab reports, especially for its handy tool - Equation Editor. Equation Editor allows you to type complicated mathematical expressions in a compact and elegant way. In order to use this tool go to Insert $\mathbf{M}$ enu $\rightarrow \mathbf{O}$ bject $\rightarrow \mathbf{M}$ icrosoft Equation 3.0.
To find the frequency of oscillation we have to determine equation that governs the dynamics of the system. Let's start with Newton's Second Law and find forces acting on the cart.

$$
\begin{equation*}
\sum_{i} \vec{F}_{i}=m \vec{a} \tag{1}
\end{equation*}
$$

The cart only moves horizontally, so we can ignore vertical forces. There are two forces acting on the cart in the horizontal direction: $\vec{F}_{1}$ and $\vec{F}_{2}$ (seeFig. 2), where $\vec{F}_{1}$ and $\vec{F}_{2}$ are restoring forces obeying Hooke's Law: $F=-k \Delta x, k$-spring constant, $\Delta x-$ stretch of spring.


Fig. 2. Forces acting on the cart attached to two springs, $x$ being position of the cart. Friction is ignored since the cart rolls nearly without friction.

At the equilibrium position $x_{0}$ forces are equal: $F_{2}^{e q}=F_{1}^{e q}$. As the cart is displaced from the equilibrium position forces change, which determines the motion of the cart. Therefore, from now on we are concerned with the change in forces with respect to equilibrium ones (here it's useful to make analogy with potential energy - only change in potential energy matters).

Let's consider the situation when the cart is displaced to the right from equilibrium (see Fig. 3) and let's write N ewton's Second Law:

$$
\begin{align*}
& \left(\vec{F}_{1}^{e q}+\Delta \vec{F}_{1}\right)+\left(\vec{F}_{2}^{e q}+\Delta \vec{F}_{2}\right)=m \vec{a} \\
& \quad \vec{F}_{1}^{e q}+\vec{F}_{2}^{e q}=0 \Rightarrow \Delta \vec{F}_{1}+\Delta \vec{F}_{2}=m \vec{a} \tag{2}
\end{align*}
$$

where $\vec{F}_{1}^{\text {eq }}$ and $\vec{F}_{2}^{\text {eq }}$ are forces exerted by the springs at the equilibrium, $\Delta \vec{F}_{1}$ and $\Delta \vec{F}_{2}$ are changes in forces with respect to equilibrium.


Fig. 3. Cart at equilibrium position a) and cart displaced from equilibrium position b).
By projecting equation (2) onto $x$-axes at the moment when cart is displaced to the right, we get

$$
\begin{equation*}
\Delta F_{1 x}+\Delta F_{2 x}=m \frac{d^{2} x}{d t^{2}} \tag{3}
\end{equation*}
$$

The changes in forces $\Delta F_{1_{x}}$ and $\Delta F_{2 x}$ can befound using Hook's Law
$\Delta F_{1 x}=F_{1 x}-F_{1 x}^{e q}=-k_{1}\left(x-x_{0}\right), \Delta F_{2}=F_{2 x}-F_{2 x}^{e q}=-k_{2}\left(x-L_{2}\right)+k_{2}\left(x_{0}-L_{2}\right)=-k_{2}\left(x-x_{0}\right)$, where $L_{2}$ is the relaxed length of the spring.

Finally we got equation that describes the motion of the cart:

$$
\begin{equation*}
\frac{d^{2} x}{d t^{2}}+\frac{\left(k_{2}+k_{1}\right)}{m}\left(x-x_{0}\right)=0 \tag{4}
\end{equation*}
$$

Since we know that motion of the cart is periodic around its equilibrium position, equation (4) should describe periodic motion. We can guess a solution of Eq. (4) as a periodic function: $x(t)=A \sin (\omega t+\delta)+x_{0}$. If this solution works, we know that we can use it to find the oscillation frequency f , because $\omega=2 \pi f$. For this to be a solution, it must describe motion of the cart and also satisfy Eq. 4 for any moment of time. To compare with equation (4), take derivatives
$x(t)=x_{0}+A \sin (\omega t+\delta) \Rightarrow \frac{d x}{d t}=A \omega \cos (\omega t+\delta) \Rightarrow \frac{d^{2} x}{d t^{2}}=-A \omega^{2} \sin (\omega t+\delta)$
and notice that:

$$
\begin{equation*}
\frac{d^{2} x}{d t^{2}}+\omega^{2}\left(x-x_{0}\right)=0 \tag{5}
\end{equation*}
$$

Comparing Eq. 5 with Eq. 4 , it will work if $\omega^{2}=\frac{k_{1}+k_{1}}{m}$. Therefore we have a solution of Eq. 4: $x=A \sin \left(\sqrt{\frac{k_{2}+k_{1}}{m}} t+\delta\right)$ with oscillation frequency:

$$
\omega=2 \pi f=\sqrt{\frac{k_{2}+k_{1}}{m}}
$$

To compare with experiment, it is useful to note the period: $T=\frac{2 \pi}{\omega}=2 \pi \sqrt{\frac{m}{k_{2}+k_{1}}}$.
So, based on our predictions, period is inversely proportional to the sum of two spring constants. If we attach two identical springs to the cart, period of oscillations should decrease (be multiplied by a factor of $\frac{1}{\sqrt{2}}$ ) with respect to the period of one spring attached.

## Experiment and results

This section describes your experimental method, the data that you collected, any problems in gathering the data, and any crucial decisions you made. Briefly discuss your setup and explain how you collected your data. Present information in a clear way either in tables or graphs. Make sure you have correct units shown on the graphs. Include all information that you used in the lab to calculate some final results so that we can repeat the calculations and see whether this step is correct or not. In order to arrive at a valid conclusion in testing a theory or hypothesis it is necessary to understand the underlying concepts of measurement uncertainties. Calculate your uncertainties and indicate the largest contribution to uncertainty. Finally, compare the experimental results and theoretical prediction and discuss the agreement between them.

Our group started from a simple experiment: we took measurements of the period of the oscillating cart with a stop watch and got $T=1.5 \mathrm{~s}$. However, our measurements with the stop watch have large uncertainty and therefore can be used as an estimate only. Since there is a delay in time due to human reaction, we estimated uncertainty to be $\pm 0.5 \mathrm{~s}$. As we can see, there is large uncertainty involved in this simple experiment.
A discussion of uncertainty should follow all measurements. No measurement is exact. Uncertainty must be included to indicate the reliability of your data.
We decided to take another approach then. Our group made a video of the motion and analyzed it with the help of LabView software. Using video analysis we can substantially reduce uncertainty and get better results. See attached Fig. 5 with results of video analysis. Uncertainty in LabView program is hard to estimate. Mainly, it comes from fitting the experimental curve and some displacement of
pointing dot during video analysis. One can estimate the uncertainty for this experiment by looking at the variation of the period on the experimental graph.
UUncertainty of the experimental data is specific to the experiment performed. In general, uncertainty related to the video analysis can be estimated by clicking on the same point on the car's image and recording its position. Uncertainty caused by the fitting of experimental points can be estimated by finding the largest deviation of the experimental point from the fitted curve or by varying the constants, for example acceleration, so that your equation still fits the data.

Our group estimated uncertainty to be $\pm 10 \%$. After analyzing the video, we found the experimental frequency to be $f=0.745 \pm 0.08 \mathrm{~Hz}$.

To be able to compare theoretical results with experimental, we had to get the spring constants. In order to do so we attached a 50-gram weight to each of the springs and measured the displacement from relaxed lengths ( $L_{1}$ and $L_{2}$ were equal to 6 cm ). SeeFig 4 . The uncertainty in the measurements of the spring lengths is $\pm 0.5 \mathrm{~cm}$.

## Spring 1:

Spring 2:
$\Delta x_{1}=17 \pm 0.5 \mathrm{~cm}$
$\Delta x_{2}=18 \pm 0.5 \mathrm{~cm}$
$k_{1}=\frac{m g}{\Delta x_{1}} \Rightarrow k_{1}=2.88 \mathrm{~N} / \mathrm{m}$

$$
k_{2}=\frac{m g}{\Delta x_{2}} \Rightarrow k_{2}=2.72 \mathrm{~N} / \mathrm{m}
$$



Fig. 4. Diagram for calculation of the spring constants.
Based on the information gathered, we calculated the theoretical frequency using formula

$$
f=\frac{1}{2 \pi} \sqrt{\frac{k_{2}+k_{1}}{m}}
$$

where $k_{1}$ and $k_{2}$ are spring constants, $m=251.7 \pm 10 \mathrm{~g}$ is mass of the cart. Predicted frequency is $f=0.751 \mathrm{~Hz} \pm 0.03 \mathrm{~Hz}$. Calculated frequency is within uncertainty of our experiment, so we conclude that our prediction adequately describe experimental results.

During experiment we noticed that frequency of oscillations is slightly changing with time and it can be explained by effect of friction on the motion of the cart.

## Conclusions

This section summarizes your results. In the concise manner, it answers the original question of the lab. A good conclusion will always compare actual results with the predictions. If your prediction was incorrect, then you must discuss where your reasoning went wrong. If your prediction was correct, then you should review your reasoning and discuss how this lab served to confirm your knowledge of the basic physical concepts.

In this lab, we determined frequency of oscillations of the cart attached to two different springs. The calculated results agree with experimental results, within our range of uncertainty. We concluded that the theoretical prediction based on Newton's Second Law and Hook's Law adequately describes the experimental situation. We also found some small effect of friction. However, for initial times, friction can be neglected.
After you have compared your predictions to your measured results, it is helpful to use an alternative measurement to check your theory with the actual data. This should be a short exercise demonstrating to yourself and to your TA that you understand the basic physics behind the problem. Most of the lab problems are written to include alternative measurements.

Our obtained results also agree with stop watch measurement of oscillation period: $\mathrm{T}=1.5 \mathrm{~s} \Rightarrow f=0.67 \mathrm{~Hz}$. This alternative measurement is within experimental uncertainty of our other experimental and predicted results. Finally, we noticed that theoretical predictions of above experiment coincide with side-by-side configuration.

## References

|| List books, journals or any other resources that you used to write your lab report.

1. Tipler, Paul A. Physics for Scientists and Engineers. 4th, W. H. Freeman: 1999. p 180, 928, 930.


Fig. 5. Experimental results from video analysis.

# Appendix F: Simulation Programs (LabSims) 

N ote: U p-to-date information on using the LabSims can be found by pressing the "Sim H elp" button at the lower left corner of a simulation window.

A LabSim program is a computer simulation of some of the situations you encounter in the lab. Simulations let you do things you can't do in the real world, in order to see what happens in those circumstances. That may sound silly (why would anyone care about what happens in an unreal world), but is actually very useful. If your data doesn't match your predictions, a simulation can help you find out what is causing the difference by letting you look at the consequences of different potential causes, and seeing what effects they make in isolation, without getting confused with something else.

The LabSims are meant to let you "explore the experiment", and to see the effects of different physical interactions. For example, suppose you thought your real experiment didn't match your predictions because of air resistance (which is present in the real world, but not in your predictions). A simulation lets you investigate the effects of air resistance by itself, without getting confused with other kinds of friction. Simulations also let you "turn up" air resistance to ridiculous levels, so you can see the form of its effects very clearly. If simulated air resistance does reproduce the problems you see in your data, then it might be the cause, if it fails to reproduce them, you should look elsewhere.

## USING THE LABSIMS

Once you get a LabSim program going, the easiest way to see what it does is to push the R un button, which is right under the 3D window (it's the black button with the " $>$ " label). "Run" makes the LabSim go, using the values in the yellow windows to the left. You can change the length of a run by changing the number of frames (the current frame number is shown to the right of the run button). The " $\mid<$ " button is a"Rewind", which places all objects in their initial positions. The "||" button is "P ause", which stops everything. The buttons are meant to look like those on a DVD player or VCR.

## 3D NAVIGATION

You can "walk" around in the 3D window by using the arrow keys (but first you M UST put the mouse in the 3D window). The arrows move you around rather like in a video game, with which you may have experience. Holding down ALT while you push the arrows lets you move up and down or back and forth (gamers call it a "strafe" button) and CTRL lets you tip up and down. Experiment with these.

## WHEN YOU GET LOST

If you get lost in the 3D space, click the "H oriz View", "Vert View" or "Reset All" buttons. H oriz View brings you back to your starting point, V ert V iew puts you over the table looking down, and Reset All resets everything to where it was when the program started.


## PARAMETERS

The panel to the left of the 3D view has names and values of all the things you can vary in the experiment. For example, in the simulation pictured below you can adjust the cart's initial speed or position, change the ramp angle, change the cart's mass, or create friction,. You change them by typing in new values, then see what happens by pushing Rewind and then Run. If you change so many things you don't know where you are anymore, and you just want to get back to some reasonable defaults, click on "Reset All." in the lower left panel.

## GRAPHS

A Powerful way to visualize motion using the LabSims is with real time graphs. If you push one of the red graph buttons at the bottom right, a separatewindow will pop up. The new window will be rather empty until you do a run in the 3D window, after which it will have graphs of position and speed. Thetop graph is the position, and the bottom one is speed (which component of position and speed depends on the button). You can change the limits on the graphs, redraw the plot and so on with the boxes on the left side of the graph window.

Sometimes a Graph window may appear to lose part of its information. Press the Redraw button to fix the problem.

Graphs are extremely useful for comparing different runs and checking for differences. Explore this by doing one run, then changing something and doing it again (click on the new color button after the first run).

Graphs also let you simulate the effects of MEASUREMENT UNCERTAINTY. You can never get perfect data in the laboratory. With the simulations y ou can see the difference between "perfect" data and what you get with imprecise"position clicks" in VideoTOOL. You may discover that it is worth your time to take VideoTOOL data very carefully.

To see the effect of measurement uncertainty, do a run. Then simulate uncertainty on the graph by pressing the "A dd error" button in the graph window. This adds randomly distributed errors to the position measurements. Experiment with different measurement uncertainties by changing the "error" parameter in the pink box, or by adding error several times (just press A dd Error several times). The vel ocity values are recal culated when you add error to the positions, so you can see what happens to velocity if position measurements arenot madeprecisely.

To compare the effects of measurement uncertainty to other effects (air resistance, for example) go through the process of adding error to a clean run. Change Color on the graph, and then do another run with the other effect (air resistance, for example). N ow you have two sets of graphs to compare.

## MAKING MOVIES

Click the "M ovieH elp" button in any simulation for up-to-date information on this function.

Possibly the most useful, but currently the slowest, way to use the LabSims is to make a movie with them, and then to analyze the simulation movie in the same way you analyze real video data.

To make a movie, first you should clean out any old frames by clicking the "Cleanup" button on the computer desktop. Then you should play around with the LabSim until you have a run and a camera position you like. Click on the yellow "Save" button, which writes a littlefile to disk with the positions of the apparatus in every frame. N ow click on the "Make Frames for Lab x" button on the desktop, which will start up a program called PoVRay. PoVRay makes high quality movie frames of the experiment (it will take a couple minutes). Finally you can turn the frames into a movie (which will be in c:\ labSim\ frames $\backslash$ simM ovie.avi) by clicking on the"Make movie from frames" button. Then you can read the movie into VideoTOOL and analyze it with that.


[^0]:    * An " R " in the points column means to rewrite that section only and return it to your lab instructor within two days of the return of the report to you.

[^1]:    **The Example of Two Bullets**

